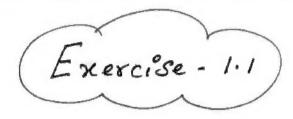
## Chapter - 1

## SET LANGUAGE



- 1. Which of the following are Sets?

  (i) The collection of prime numbers

  upto 100.

  Sol:- Set.
- (ii) The collection of rich people in India.

  Sol:- Not Set.
- liii) The collection of all rivers in India

(iv) The Collection of good Hockey Players. Sol! - Not Set.

2) List the Set of letters of the following words in Roster form.

(i) INDIA = {I, N, D, A}

(ii) PARALLELOGRAM = {P,A,R,L,E,O,G,M}

(iii) MISSISSIPPI = {M,1, S, P}

(I'V) CZECHOSLOVAKIA = {C,Z,E,H,O,S,L,V,A,K,I}

(3) Consider the following Sets  $A = \{0,3,5,8\}, B = \{2,4,6,10\} \text{ and } C = \{12,14,18,20\}$ 

(a) State Whether True or False:

(i) 18 € C -> True

(ii) 6 € A -> True

(iii) 14 ¢ c -> False

(iv) 10 eB -> True.

- (v) 5EB -> False
- (vi) OEB -> False.
- (b) Fill Pn the blanks: -
  - (i)  $3 \in A$
  - (ii) 4 E C
  - (iii) 18 <u>€</u> B
  - (iv) 4 <u>e</u> B
- (4) Represent the following sets in Roster =
  - (i) A = The Set of all even natural numbers less than 20.
- $Sol:-A = \{2,4,6,8,10,12,14,16,18\}$ 
  - (ii) B = { y: y = \frac{1}{20}, nen, ne 5}
  - SOI:- D=1,2, 3,4,5

(iii) 
$$C = \{x: x \text{ is Perfect Cube}, 27 < x < 216\}$$
  
 $Sol! - C = \{64, 125\}$ 

(iv) 
$$D = \{x: x \in Z, -5 < x \le 2\}$$
  
 $SOI: D = \{-4, -3, -2, -1, 0, 1, 2\}$ 

- (5) Represent the following sets in Set builder form.
  - (i) B = The Set of all Cricket players
    in India who Scored double

    Centuries in One Day Internationals.
- Sol:- B= [x:x is all Indian Cricket

  Players who Scored double

  Centuries in One Day International)
  - (ii) C= {立,章,章,·---}
- Sol:- C = {x:x = n ; n e N}
- (iii) D = The Set of all tomil months in a year.
- Sol! D = {x:x is all tamil months in a year }

- (iv) E = The Set of odd whole numbers less than 9.
- Sol:- E = {x:x is odd whole numbers less than 9 }.
- 6 Represent the following sets in descriptive form.
- (i) P= { January, June, July }
  Sol:- P= The Set of Months Starting
  with 'J'.
  - (ii) Q = {7, 11, 13, 17, 19, 23, 29}
- Sol:- Q = The Set of all Prime numbers between 5 and 31.
- (iii) R = {x:xEN, x<5}
- Sol: R= The Set of all natural number less than

(iv) 
$$S = \{x : x \text{ is a consonants in English alphabets } \}$$

Sol: -  $S = \text{The Set of all Consonants}$ 

in English alphabets.

O Find the Cardinal number of the following Sets.

(i) M = {P, 9, 8, 6, U}

Sol: (n(M) = 6

(ii)  $P = \{ \chi : \chi = 3n+2, n \in \omega \text{ and } \chi < 15 \}$   $Sol : - n \in \omega = \} n = 0, 1, 2, 3, ...$  D = 0 ;  $\chi = 3(0) + 2 = 0 + 2 = 2$ D = 1 ;  $\chi = 3(1) + 2 = 3 + 2 = 5$ 

$$n = 2; \quad \chi = 3(2) + 2 = 6 + 2 = 8$$

$$n = 3; \quad \chi = 3(3) + 2 = 9 + 2 = 11$$

$$n = 4; \quad \chi = 3(4) + 2 = 12 + 2 = 14$$

$$\chi < 15$$

$$P = \{2, 5, 8, 11, 14\}$$

$$n(P) = 5$$

$$\ln \log = 3$$

iv) 
$$R = \{\chi: \chi \text{ is an integers, } \chi \in Z \}$$
  
and  $-5 \le \chi < 5\}$   
Sol:-  $R = \{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4\}$   
 $[n(R) = 10]$ 

(V) S = The Set of all leap years between 1882 and 1906.

Sol: - A leap year comes four years Once.

$$S = \begin{cases} 1884, 1888, 1892, 1896, 1900, 1904 \end{cases} = \frac{45}{1882}$$

$$\ln(s) = 6$$

- 2) Identify the following sets as finite or Infinite.
  - (i) X = The Set of all districts in Tamilnadu.

Sol: - Finite Sets

$$\frac{Sol!}{(x-3)(x-2)=0}$$

$$\frac{50!}{(x-3)(x-2)=0}$$

$$\chi - 3 = 0$$
  $\chi - 2 = 0$ 

$$\chi = 3$$
  $\chi = 2$ 

$$x = 3, 2$$

Frnite Set

(3) Which of the following sets are equivalent or unequal or equal sets?

(i) A = The set of Vowels in English alphabets.

B = The set of all letters in the Word "Vowel".

Sol  $A = \{a, e, i, o, o\}$   $B = \{v, o, \omega, e, l\}$   $\therefore D(A) = D(B) = 5$  Equivalent Sets

(ii)  $C = \{2, 3, 4, 5\}$ ,  $D = \{x : x \in W, | x < 5\}$ Sol:-  $C = \{2, 3, 4, 5\}$   $D = \{2, 3, 4\}$ Un equal Sets.

(iii)  $X = \{x: x \text{ is the letter in the Word "Life"}\}$  $Y = \{F, I, L, E\}$ 

Sol: - 
$$X = \{L, I, F, E\}$$
  
 $Y = \{F, I, I, E\}$   
Equal Sets

$$H = \{1, 2, 3, 6, 9, 18\}$$

$$n(G) = n(H) = 6$$

(ii) B= The Set of all even natural numbers which are not divisible by 2.

Sol: - B= { } => Null sets

Liii) C = {0}

Sol: - Singleton Sets

(iv) D= The Set of all triangles having four sides

Sol:- "Null Sets.

(i) A = {f, i, a, s}; B = {a, n, f, h, s}

Sol Overlapping.

[element f, a, s are Common in Set A + B.]

(iii) 
$$E = \{x: x \text{ is a factor of 24}\}$$
 $F = \{x: x \text{ is a multiple of 3, } x < 30\}$ 
 $Sol! - E = \{1, 2, 3, 4, 6, 8, 12, 24\}$ 
 $F = \{3, 6, 9, 12, 15, 18, 21, 24, 27\}$ 

Overlapping

- 6. If S= { Square, rectangle, Circle, shombus, triangley, list the elements of the following Subsets of S.
- (i) The Set of Shapes which have 4 equal Sides.

  Sol! { Square, shombus}
- (ii) The Set of Shapes which have radius. Sol: - { Circle }.
- (iii) The Set-of Shapes in which the Sum of all interior angles is 180.

  Sol!- [Triangle]
- sol! { Set of Shapes which have 5 sides.

- 1) It A = {a, {a, b}}, write all the Subsets of A.
- Sol! Subsets of A are { 3, {a}, {a,b}, {a,64,b}}
- 8. Write down the power set of the following sets:-
  - (i) A = {a,b}
- $Sol: P(A) = \{ \phi, \{a\}, \{b\}, \{a,b\} \}$
- (11)  $B = \{1,2,3\}$
- $SOI :- P(B) = \{ \phi, \{1\}, \{2\}, \{3\}, \{1,2\}, \{2,3\}, \{3,1\}, \{1,2,3\} \}$
- (iii) D = {P,q,r,s}
- Sol:  $-P(D) = \{\phi, \{P\}, \{q\}, \{s\}, \{s\}, \{S\}, \{P,q\}, \{q,s\}, \{s,s\}, \{s,q\}, \{P,r\}, \{p,q,s\}, \{p,q,$

(iv) 
$$E = \phi$$
  
Sol! - P(E) = { }

(9) Find the number of Subsets and the number of proper Subsets of the following Sets.

$$Sol! - n(N) = 3$$

Number of Subsets = n[p(w)] = 2 = 8 Number of proper Subsets = n[p(w)]-1

$$= 2^{3}$$

(1i) 
$$X = \{x^2 : x \in \mathbb{N}; x^2 \leq 100\}$$
  
 $\mathbf{x} = 1, 2, 3, \dots$ 

$$\chi^2 = \{1, 4, 9, 16, 25, 36, 49, 64, 81, 100\}$$

$$X = \{1, 4, 9, 16, 25, 36, 49, 64, 81, 100\}$$

$$P(x) = 10$$

Number of Subsets =  $P(x) = 2 = 1024$ 

Number of Proper Subsets =  $P(x) = 1024$ 
 $P(x) = 1024 = 1024$ 
 $P(x) = 1023$ 

(i) If 
$$n(A) = 4$$
; find  $n[p(A)]$   
Sol:-  $n(A) = 4$   
 $n[p(A)] = 2^{n(A)}$   
 $= 2^{\frac{1}{4}}$   
 $n[p(A)] = 16$ 

(ii) If 
$$n(A) = 0$$
; find  $n[P(A)]$   
Sol:-
$$n[P(A)] = 0$$

$$n[P(A)] = 2^{n(A)}$$

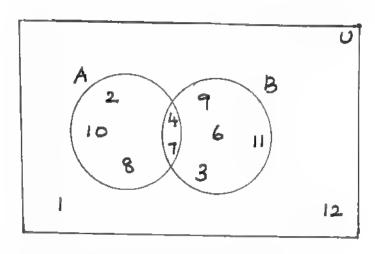
$$= 2^{0}$$

$$n[P(A)] = 1$$

$$D[P(A)] = 2$$
 $2 = 2 = 56$ 
 $D[P(A)] = 2^{n(A)}$ 
 $2 = 128$ 
 $2 = 64$ 
 $2 = 64$ 
 $2 = 16$ 
 $2 = 8$ 
 $2 = 16$ 
 $2 = 8$ 
 $2 = 4$ 
 $2 = 4$ 
 $2 = 4$ 



1) Using the given Venn diagram, write the elements of



(i) 
$$A = \{2, 10, 8, 4, 7\}$$

(ii) 
$$B = \{4,7,9,6,3,11\}$$

$$(v) A - B = \{2, 10, 8\}$$

(M) 
$$A' = \{9,6,3,11,1,12\}$$

$$(x)$$
  $U = \{2, 10, 8, 4, 7, 9, 6, 311, 1, 12\}$ 

2) Find AUB, ADB, A-B and B-A for the following Sets.

(i) 
$$A = \{2,6,10,14\}, B = \{2,5,14,16\}$$
  
 $Sol: - \text{B}AUB = \{2,6,10,14\}, U\{2,5,14,16\}$   
 $AUB = \{2,6,10,14,5,16\}$ 

(A) ANB = (2, 6, 10, 4) (25, 4)ANB = (2, 14)

\* 
$$B-A = \{ \neq, 5, | \neq, | b \} - \{ \neq, 6, | 0, | \neq \} \}$$
  
 $B-A = \{ 5, | b \}$ 

- $+ AUB = \{a, b, c, e, v\} \cup \{a, e, i, o, v\}$  $AUB = \{a, b, c, e, v, i, o\}$
- \* Ans = {a, b, c,e, w}n{a,e,i,0,w} Ans = {a, e, v}

# A-B = 
$$\{ \phi, b, c, k, V \} - \{ \phi, \psi, i, 0, V \}$$
  
A-B =  $\{ b, c \}$ 

- (iii)  $A = \{x: x \in \mathbb{N}, x \leq 10\}$  and  $B = \{x: x \in \mathbb{N}, x \leq 6\}$ Sol:  $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$  $B = \{0, 1, 2, 3, 4, 5\}$
- #  $AUB = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\} \cup \{0, 1, 2, 3, 4, 5\}$  $AUB = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
- \* And =  $\{1, 2, 3, 4, 5\}$ And =  $\{1, 2, 3, 4, 5\}$
- $+ A B = \{ 1, 1, 3, 4, 5, 6, 7, 8, 9, 10 \} \{ 0, 1, 1, 3, 4, 5 \}$   $A B = \{ 6, 7, 8, 9, 10 \}$
- $B-A = \{0, X, X, 3, 4, 5\} \{Y, X, 3, 4, 5, 6, 7, 8, 9, 10\}$   $B-A = \{0\}$

- (iv) A = The Set of all letters in the Word
  "Mathematics"
  - B = The Set of all Letters in the Word "Geometry"
- Sol:-  $A = \{m, a, t, h, e, l, c, s\}$  $B = \{g, e, o, m, t, r, y\}$ .
- \*AUB = [m,a,t,h,e,i,c,s]U{g,e,o,m,t,r,y} AUB = [m,a,t,h,e,i,c,s,g,o,r,y]
- # ANB = {m, a, t, b, e, i, c, s} n {q, e, o, m, t, e}
  ANB = {m, t, e}
- \*  $A-B = \{ph, a, k, h, k, i, c, s\} \{q, k, 0, m, k, r, y\}$  $A-B = \{a, h, i, c, s\}$
- \*  $B-A = \{g, e, o, m, k, r, y\} \{rh, a, k, h, e, i, c, s\}$  $B-A = \{g, o, r, y\}$

(i) 
$$A^{\prime}$$
  
Sol  $A^{\prime} = U - A$ 

$$A' = \{a, k, c, d, e, f, g, k\} - \{k, d, f, k\}$$
 $A' = \{a, c, e, g\}$ 

Gi) B'  
SOI 
$$B' = U - B$$
  
B' =  $\{a, b, c, a, x, f, q, k\} - \{a, a, x, k\}$   
B' =  $\{b, c, f, q\}$ 

(iii) 
$$A' \cup B'$$
  
 $Sol! - A' \cup B' = \{a, c, e, g\} \cup \{b, c, f, g\}$   
 $A' \cup B' = \{a, c, e, g, b, f\}$   
 $[A' \text{ and } B' \text{ from (i) and (ii)}]$ 

(iv) 
$$A' \cap B'$$
  
 $SOI :- A' \cap B' = \{a, C, e, 9\} \cap \{b, C, f, 9\}$   
 $A' \cap B' = \{c, 9\}$ .

$$(A \cup B) = \{ b, d, f, h \} \cup \{a, d, e, h \}$$
  
 $(A \cup B) = \{b, d, f, h, a, e \}$   
 $(A \cup B)' = \{a, k, c, a, e, f, g, k \} - \{k, a, f, k, g, e \}$   
 $(A \cup B)' = \{c, g \}$ 

$$A \cap B = \{b, \emptyset, f, \emptyset\} \cap \{a, \emptyset, e, \emptyset\}$$

$$A \cap B = \{d, h\}$$

$$(A \cap B)' = \{a, b, c, q', e, f, g, k\} - \{q', k\}$$

$$(A \cap B)' = \{a, b, c, e, f, g\}$$

$$(A \cap B)' = \{a, b, c, e, f, g\}$$

(vii) 
$$(A')'$$

Sol:  $-(A')' = U - A'$ 

[The Value of  $A'$  is in (i)]

 $(A')' = \{a, b, a, d, a, f, g, b\} - \{a, a, a, g\}$ 
 $(A')' = \{b, d, f, b\}$ 
 $ie, (A')' = A$ 

(viii) (B') '

Sol:- 
$$(B')' = U - B'$$

[The Value of B' is in (ii)]

 $(B')' = \{a, b, x, d, e, x, y, b\} - \{b, x, x, y\}$ 
 $(B')' = \{a, d, e, b\}$ 
 $ie, (B')' = B$ 

$$\frac{Sol! - A' = \{0, x, 2, 3, 4, 5, 6, 7\} - \{x, 3, 5, 7\}}{A' = \{0, 2, 4, 6\}}$$

Sol 
$$B' = \{ \emptyset, 1, 2, 3, 4, 7, 6, 7 \} - \{ \emptyset, 2, 3, 7, 7 \}$$
  
 $B' = \{ 1, 4, 6 \}$ 

$$\frac{Sol! - A'UB'}{A'UB'} = \{0, 2, 4, 6\} \cup \{1, 4, 6\}$$

$$A'UB' = \{0, 2, 4, 6, 1\}$$

Sol:- A'nB' = 
$$\{0,2,4,6\} \cap \{1,4,6\}$$
  
A'nB' =  $\{4,6\}$ 

(v) 
$$(A \cup B)'$$
  
Sol  $A \cup B = \{1,3,5,7\} \cup \{0,2,3,5,7\}$   
 $A \cup B = \{1,3,5,7,0,2\}$   
 $(A \cup B)' = \{\emptyset, X, X, 3, 4, 5, 6, 7\} - \{Y, 3, 5, 7, 0, 2\}$   
 $(A \cup B)' = \{4,6\}$ 

(vi) 
$$(A \cap B)'$$
  
Soi  $A \cap B = \{1, 3, 5, 7\} \cap \{0, 2, 3, 6, 7\}$   
 $A \cap B = \{3, 5, 7\}$   
 $(A \cap B)' = \{0, 1, 2, 3, 4, 7, 6, 7\} - \{3, 7, 7\}$   
 $(A \cap B)' = \{0, 1, 2, 4, 6\}$ 

(vii) 
$$(A')'$$

Sol:-  $(A')' = U - A'$ 
 $= \{ \emptyset, 1, 1, 2, 3, 1, 5, 5, 7 \} - \{ \emptyset, 1, 1, 1, 1 \}$ 
 $(A')' = \{ 1, 3, 5, 7 \}$ 

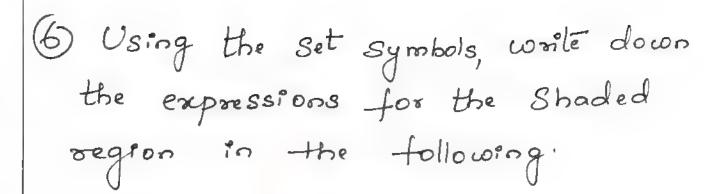
(viii) (B') 
$$= Sol := (B')' = U - B'$$
  
 $= \{0, 1/2, 3, 1/3, 5, 1/3\} - \{1/3, 1/4, 1/4\}$   
(B')  $= \{0, 2, 3, 5, 7\}$ 

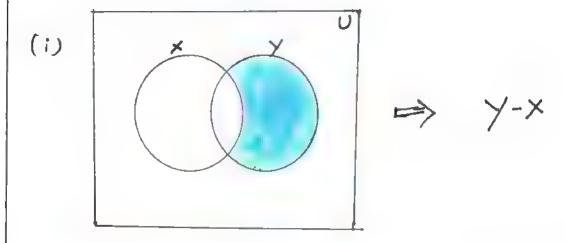
$$Q - P = \{1, 3, 5, 11\} - \{2, 3, 5, 7, 11\}$$

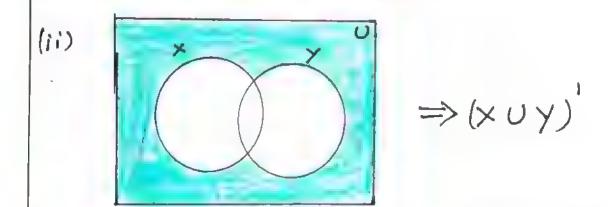
$$Q - P = \{1, 3, 5, 11\}$$

(ii) 
$$R = \{l, m, n, o, P\}$$
 and  $S = \{i, l, n, q\}$   
 $S = \{i, m, o, o, P\}$  and  $S = \{i, l, q, q\}$   
 $R - S = \{i, m, o, p\}$  -  $\{i, l, q, q\}$   
 $R - S = \{i, l, q, q\}$  -  $\{l, m, q, o, P\}$   
 $S - R = \{i, l, q, q\}$  -  $\{l, m, q, o, P\}$   
 $S - R = \{i, q\}$   
 $R = \{i,$ 

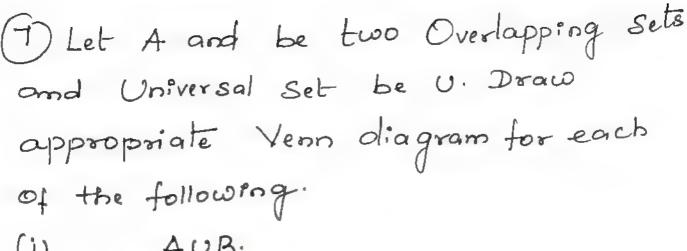
 $Y-X = \{9, 10\}$   $X \Delta Y = \{6\} \cup \{9, 10\}$  $X \Delta Y = \{6, 9, 10\}$ 



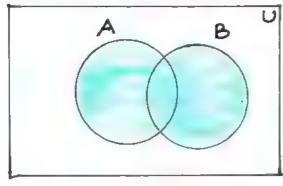


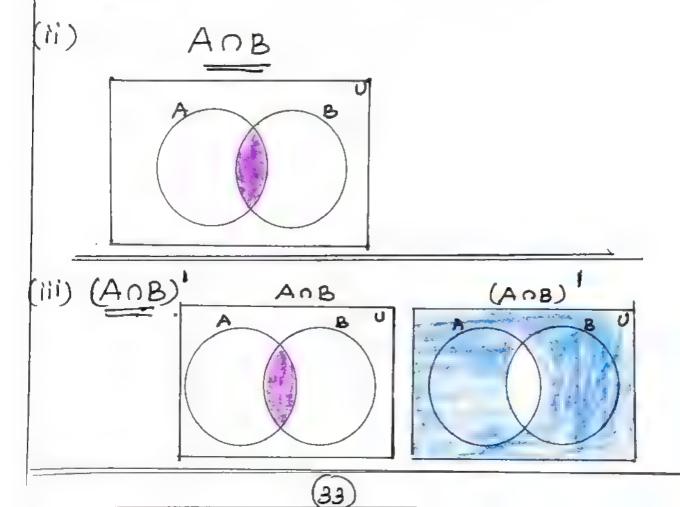


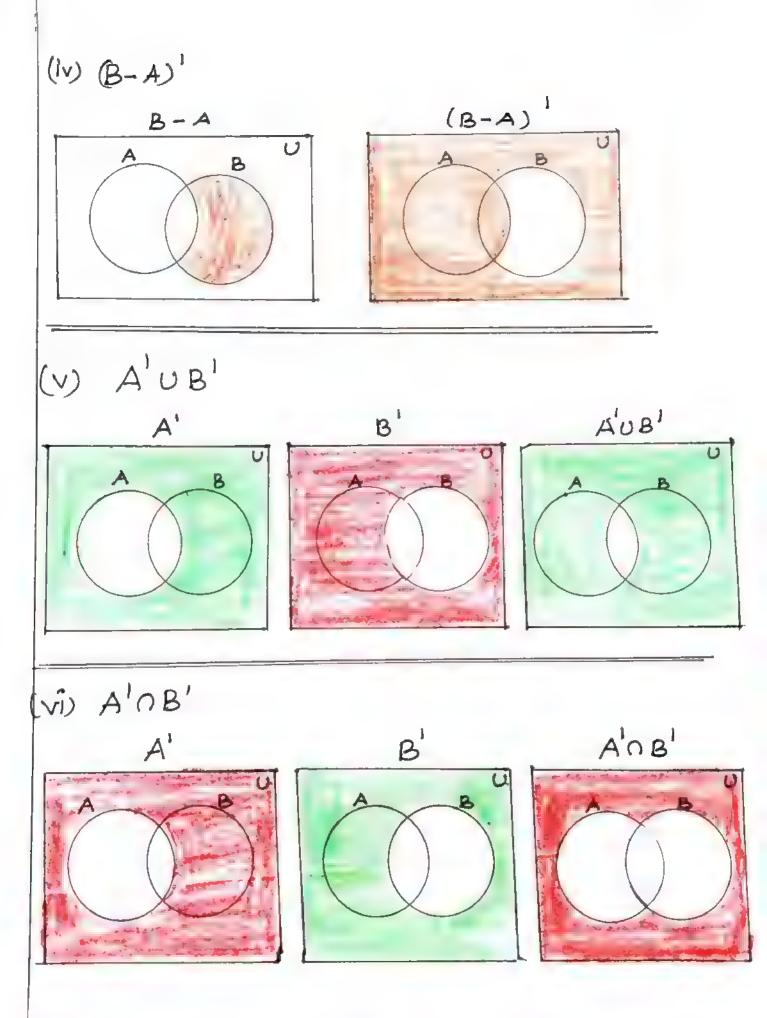
$$(iii) \Rightarrow (x \cap y)^{1}$$











(vii) what do you Observe from the Yenn diagram (iii) and (v)?

Sol!
Venn diagram (iii) and (v)

ie, (A OB) = A'UB'

Exercise - 1.4

1. If  $P = \{1, 2, 5, 7, 9\}$ ,  $Q = \{2, 3, 5, 9, 11\}$  $R = \{3, 4, 5, 7, 9\}$  and  $S = \{2, 3, 4, 5, 8\}$  then find.

(i) (PUQ) UR

SOI PUR =  $\{1, 2, 5, 7, 9\}$   $U\{2, 3, 5, 9, 11\}$ PUR =  $\{1, 2, 5, 7, 9, 3, 11\}$   $(PUR)UR = \{1, 2, 5, 7, 9, 3, 11\}$   $(PUR)UR = \{1, 2, 5, 7, 9, 3, 11\}$  $(PUR)UR = \{1, 2, 5, 7, 9, 3, 11, 4\}$ 

(ii) 
$$(PnQ) nS$$
  
 $SOI (PnQ) = \{1, 2, 5, 7, 9\} n \{2,3,5, 9, 11\}$   
 $PnQ = \{2,5,9\}$   
 $(PnQ) nS = \{2,5,9\} n \{2,3,4,5,8\}$   
 $(PnQ) nS = \{2,5\}$ 

(iv) (Qns) 
$$\cap R$$
  
 $Sol :-$   
 $Qns = \{2,3,5\}$   
 $Qns = \{2,3,5\}$   
 $(Qns) \cap R = \{2,3,5\}$   
 $(Qns) \cap R = \{3,5\}$ 

Test for the Commutative Property of Union and intersection of the Sets: -P= {x:x is a real number between 2 and 7} Q = {x:x is a rational number between 2 and 7}

C. CONTRACTOR OF THE CONTRACTO
Sol! Real Number = Rational no + Irrational
149
P= The Set of all Rational No and
P= The Set of all Rational No and Prophional No between 2 and 7
Q = The Set of only rational No
between 2 and 7
(is Commutative [union])
(PUR) = (QUP)
PUQ = The Set of all rational No and for a tional No between 2 and ]
QUP = The Set of all rational No and I sational No and I
irrational No between 2 and 7
PUQ = QUP
(ii) Commutative [intersection]
(POQ = QOP)
POR = The Set of Only rational No between 24 OOP = The Set of Only rational No between 24 POR = QOP
(37) - POQ = QOP

3) It A= {P,q,r,s}, B={m,n,q,s,t} and C= {m,n,p,q,s}, then Verify the associative Property of Union of Sets. (Associative Property [union]) Sol: -(AUCBUC) = (AUB)UC LHS: - AU (BUC) Buc = 1mi, n, q, s, ty U {m, n, p, q, s} = {m, n, q, s, t, p} AU(BUC) = 2P,q,r,s} U {m,n,q,s,t,p} AU(BUC) = {P,2,x,s,m,n,t} RHS! - (AUB) UC

 $(AUB) = \{P, q, r, s\} \cup \{m, n, q, s, t\}$   $= \{P, q, r, s, m, n, t\}$   $(AUB)UC = \{P, q, r, s, m, n, t\} \cup \{m, n, p, q, s\}$   $(AUB)UC = \{P, q, r, s, m, n, t\} \cup \{m, n, p, q, s\}$   $(AUB)UC = \{P, q, r, s, m, n, t\}$   $(AUB)UC = \{AUB\}UC$ 

(4) Verify the associative property of Intersection of Sets. for  $A = \{-11, 12, 15, 7\}$   $B = \{\sqrt{3}, \sqrt{5}, 6, 13\}$  and  $C = \{\sqrt{2}, \sqrt{3}, \sqrt{5}, 9\}$ Sol! - Associative property [intersection]

An(Bnc) = (AnB)nc

LHS! - An(Bnc)

Bnc = \{\overline{13}, \overline{15}, 6, 13\} \nabla \{\sigma\_2, \overline{15}, \overline{15}, 9\}

- \{\sigma\_1, \overline{15}, 6, 13\} \nabla \{\sigma\_2, \overline{15}, \overline{15}, 9\}

 $= \{ \sqrt{3}, \sqrt{5} \}$   $= \{ -11, \sqrt{2}, \sqrt{5}, 7 \} \cap \{ \sqrt{3}, \sqrt{5} \}$ 

An(Bnc) = { 5}

RHS: - (AOB) OC

ADB =  $\{-11, \sqrt{2}, \sqrt{6}, 7\} \cap \{\sqrt{3}, \sqrt{6}, 6, 13\}$ =  $\{\sqrt{5}\}$ 

(AnB)nc = { (3) 1 (2, 13, 15), 9}

(AOB) OC = { 5}

.. An(Bnc) = (ADB)nc

5) If 
$$A = \{x : x = 2^n, n \in W \text{ and } n < 4\}$$
 $B = \{x : x = 2n, n \in N \text{ and } n < 4\}$  and

 $C = \{0,1,2,5,6\}$ , then Verify the associative

Property of intersection of Sets.

$$n=0 \Rightarrow \chi = 2^0 = 1$$
  
 $n=1 \Rightarrow \chi = 2^1 = 2$   
 $n=2 \Rightarrow \chi = 2^2 = 4$   
 $n=3 \Rightarrow \chi = 2^3 = 8$   
 $A = \{1, 2, 4, 8\}$ 

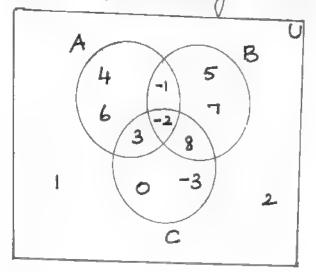
For 
$$B: -n \in \mathbb{N}$$
,  $n \le 4 \Rightarrow \boxed{n_{21,2,3,4}}$ 
 $n=1 \Rightarrow \chi = 2(1) = 2$ 
 $n=2 \Rightarrow \chi = 2(2) = 4$ 
 $n=3 \Rightarrow \chi = 2(3) = 6$ 
 $n=4 \Rightarrow \chi = 2(4) = 8$ 
 $\therefore B = \{2,4,6,8\}$ 

Bnc = 
$$\{2,4,6,8\}$$
  $\cap \{0,1,2,5,6\}$   
=  $\{2,6\}$   
An (Bnc) =  $\{1,2,4,8\}$   $\cap \{2,6\}$   
An (Bnc) =  $\{2\}$ 

Anb = 
$$\{1, 2, 4, 8\}$$
  $\cap \{2, 4, 6, 8\}$   
=  $\{2, 4, 8\}$   
(Anb)nc =  $\{2, 4, 8\}$   $\cap \{0, 1, 2, 5, 6\}$   
(Anb)nc =  $\{2, 4, 8\}$   $\cap \{0, 1, 2, 5, 6\}$ 



O Using the adjacent Venn diagram, Frod the following sets.



(i) 
$$A - B$$
  
Sol!  $A - B = \{4, 6, 3\}$ 

$$B' = \{4, 6, 3, 0, -3, 1, 2\}$$
[The Values apart from  $B' = \{5, 7, 8, 0, -3, 1, 2, 4, 6, 3\}$ 
: AUB' =  $\{5, 7, 8, 0, -3, 1, 2, 4, 6, 3\}$ 

(iv) 
$$A' \cap B' = \{5,7,8,6,3,0,3,0,2\} \cap \{4,6,3,6,3,0,3,0,2\}$$
  
 $A' \cap B' = \{6,-3,1,2\}$ 

2) If 
$$K = \{a,b,d,e,f\}$$
,  $L = \{b,c,d,g\}$   
and  $M = \{a,b,c,d,h\}$  then find the  
following!

$$\underbrace{Sol} (L DM) = \{ \underline{G}, \underline{G}, \underline{G}, \underline{g} \} \cap \{ \underline{a}, \underline{G}, \underline{G}, \underline{G}, \underline{h} \}$$

$$= \{ \underline{b}, \underline{c}, \underline{d} \}$$

$$KU(LDM) = \{ \underline{a}, \underline{b}, \underline{d}, \underline{e}, \underline{f} \} \cup \{ \underline{b}, \underline{c}, \underline{d} \}$$

$$KU(LDM) = \{ \underline{a}, \underline{b}, \underline{d}, \underline{e}, \underline{f}, \underline{c} \}$$

Sol:- Lum = { b, c, d, g} U [a, b, c, d, h]   
= {b, c, d, g, a, h}   

$$k \cap (Lum) = \{\Theta, B, Q, e, f\} \cap \{B, c, Q, g, \Theta, h\}$$
  
 $k \cap (Lum) = \{a, b, d\}$ 

$$Sol:= kul = \{a,b,d,e,f\} \cup \{b,c,d,g\}$$
  
=  $\{a,b,d,e,f,c,g\}$ 

(44)

$$kum = \{a, b, d, e, f\} \cup \{a, b, c, d, h\}$$
  
=  $\{a, b, d, e, f, c, h\}$ 

$$(KUL) \cap (KUM) = \{a, b, d, e, f, c\}$$

(iv) (knL) 
$$U(knM)$$
  
 $Sol := knL = \{a(D, 0), e, t\}, n\{D, c, 0, q\}$   
 $knL = \{b, d\}$   
 $knM = \{0, 0, 0, e, t\}, n\{0, 0, c, 0, h\}$   
 $knM = \{a, b, d\}$   
 $(knL) U(knM) = \{b, d\}, u\{a, b, d\}$   
 $(knL) U(knM) = \{b, d, a\}$ 

Distributive law Satisfies

ie, Ku(Lnm) = (kul)n(kum)

kn(Lum) = (knl)u(knm)

(3) If 
$$A = \{x: x \in Z, -2 < x \le 4\}$$
 $B = \{x: x \in W, x \le 5\}, C = \{-4, -1, 0, 2, 3, 4\}, \text{then}$ 

Verify  $AU(B \cap C) = (AUB) \cap (AUC)$ 

Sol!

 $A = \{-1, 0, 1, 2, 3, 4\}$ 
 $B = \{0, 1, 2, 3, 4, 5\}$ 
 $C = \{-4, -1, 0, 2, 3, 4\}$ 

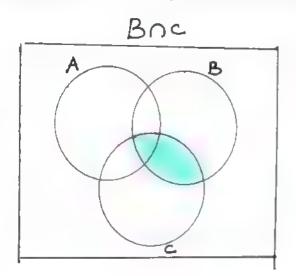
LHs!  $AU(B \cap C)$ 

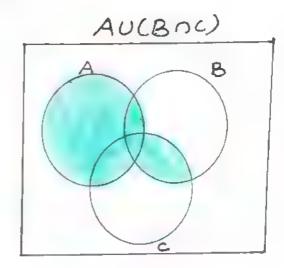
Boc  $AU(B \cap C)$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 2, 3, 4\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 2, 3, 4\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4, 5\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4, 5\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4\}$ 
 $AU(B \cap C) = \{-1, 0, 1, 2, 3, 4\}, U\{0, 1, 2, 3, 4\}$ 

(46)

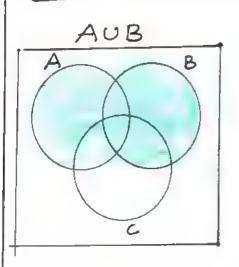
Sol! - AU(BOL) = (AUB) O(AUL)

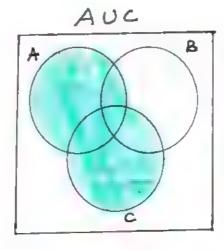
Litts: - AU(BOC)

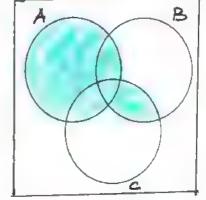




RHS: - (AUB) O (AUC)







(AUB) (AUL)

LHS = R.H.S

(a) It 
$$A = \{b, c, e, g, h\}$$
,  $B = \{a, c, d, g, i\}$   
and  $C = \{a, d, e, g, h\}$ , then show that  
 $A - (B \cap C) = (A - B) \cup (A - C)$   
Sol:  $A - (B \cap C) = (A - B) \cup (A - C)$   
Lits:  $A - (B \cap C)$   
Bnc  $= \{\emptyset, c, \emptyset, \emptyset, i\}$   $\cap \{\emptyset, \emptyset, e, \emptyset, h\}$   
 $= \{a, d, g\}$   
 $A - (B \cap C) = \{b, c, e, g, h\} - \{a, d, g\}$   
 $A - (B \cap C) = \{b, c, e, h\}$   
RHs:  $- (A - B) \cup (A - C)$   
 $A - B = \{b, f, e, g, h\} - \{a, f, d, g, i\}$   
 $= \{b, e, h\}$   
 $A - C = \{b, c, f, g, h\} - \{a, d, f, f, h\}$   
 $= \{b, c\}$   
 $A - B \cup (A - C) = \{b, e, h\} \cup \{b, c\}$ 

(48)

LHS = RHS.

A-B) U (A-c) = {b, e, h, c}

6 If 
$$A = \{x: x = 6n, n \in W \text{ and } n < 6\}$$
 $B = \{x: x = 2n, n \in N \text{ and } 2 < n \le 9\}$  and

 $C = \{x: x = 3n, n \in N \text{ and } 4 \le n < 10\}$  then

Show that  $A - \{B \cap C\} = (A - B) \cup (A - C)$ 

Sol!  $For A : n \in W, n < 6 \Rightarrow n = 0, 1, 2, 3, 4, 5$ 
 $n = 0 \Rightarrow x = 6(0) = 0$ 
 $n = 1 \Rightarrow x = 6(1) = 6$ 
 $n = 2 \Rightarrow x = 6(2) = 12$ 
 $n = 3 \Rightarrow x = 6(3) = 18$ 
 $n = 4 \Rightarrow x = 6(4) = 24$ 
 $n = 5 \Rightarrow x = 6(5) = 30$ 

Then  $A = \{0, 6, 12, 18, 24, 30\}$ 

For  $B : n \in N = 3$ 
 $A = \{0, 6, 12, 18, 24, 30\}$ 
 $A = \{0, 6, 12, 18, 24, 30\}$ 

$$A = \{0,6,12,18,24,30\}$$

$$B = \{6,8,10,12,14,16,18\}$$

$$C = \{12,15,18,21,24,27\}$$

$$A - (Bnc) = (A-B)U(A-c)$$

$$LiH5 !- A - (Bnc)$$

$$Bnc = \{6,8,10,2,14,6,16\} \cap \{2,15,6,21,24,27\}$$

$$= \{12,18\}$$

$$A - (Bnc) = \{0,6,12,18,24,30\} - \{12,18\}$$

$$A - (Bnc) = \{0,6,24,30\}$$

$$Right : - (A-B)U(A-c)$$

$$A - B = \{0,6,12,18,24,30\} - \{16,8,10,12,14,16,18\}$$

$$= \{0,24,30\}$$

$$A - C = \{0,6,12,18,24,30\} - \{12,15,18,21,24,27\}$$

$$= \{0,6,30\}$$

$$(A-B)U(A-c) = \{0,24,30\}U\{0,6,30\}$$

$$(A-B)U(A-c) = \{0,24,30,6\}$$

LH.S = RHS

$$\begin{array}{lll}
\text{TIf } A = \{-2,0,1,3,5\}, B = \{-1,0,2,5,6\}, and \\
C = \{-1,2,5,6,7\}, then Show that \\
A - (BUL) = (A-B) \cap (A-L)
\end{aligned}$$

$$\begin{array}{lll}
\text{Sol} : A - (BUL) = (A-B) \cap (A-L)
\end{aligned}$$

$$\begin{array}{lll}
\text{Sol} : A - (BUL) = (A-B) \cap (A-L)
\end{aligned}$$

$$\begin{array}{lll}
\text{LHS} : - A - (BUL)
\end{aligned}$$

$$\begin{array}{lll}
BUL = \{-1,0,2,5,6\}, U\{-1,2,5,6,7\}
\end{aligned}$$

$$\begin{array}{lll}
= \{-1,0,2,5,6,7\}
\end{aligned}$$

$$\begin{array}{lll}
A - (BUL) = \{-2,0,1,3,5\} - \{-1,0,2,5,6,7\}
\end{aligned}$$

$$\begin{array}{lll}
A - (BUL) = \{-2,0,1,3,5\} - \{-1,0,2,5,6,7\}
\end{aligned}$$

$$\begin{array}{lll}
A - (BUL) = \{-2,1,3\}
\end{aligned}$$

$$\begin{array}{lll}
\text{RH:S} : - (A-B) \cap (A-L)
\end{aligned}$$

$$\begin{array}{lll}
A - B = \{-2,0,1,3,5\} - \{-1,0,2,5,6,7\}
\end{aligned}$$

$$\begin{array}{lll}
= \{-2,0,1,3,5\}
\end{aligned}$$

$$\begin{array}{lll}
A - C = \{-2,0,1,3,5\} - \{-1,2,5,6,7\}
\end{aligned}$$

$$\begin{array}{llll}
= \{-2,0,1,3,5\}$$

$$(A-B)\cap (A-C) = \{ (2), (1), (3) \} \cap \{ (2), (0), (3) \}$$
  
 $(A-B)\cap (A-C) = \{ -2, -1, 3 \}$ 

: LHS = RHS.

$$a=0, y=\frac{0+1}{2}=\frac{1}{2}$$

$$a=1$$
 ;  $y=\frac{1+1}{2}=\frac{2}{2}=1$ 

$$a=2$$
;  $y=\frac{2+1}{2}=\frac{3}{2}$ 

$$a=3$$
;  $y=\frac{3+1}{2}=\frac{4}{2}=2$ 

$$a = 5$$
;  $y = 5 \pm 1 = \frac{6}{2} = 3$ 

(53)

$$A = \{\frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{3}{2}\}$$

$$b=0$$
,  $y=\frac{2[0)-1}{2}=\frac{0-1}{2}=-\frac{1}{2}$ 

$$n=1$$
;  $y=\frac{2(1)-1}{2}=\frac{2^{-1}}{2}=\frac{1}{2}$ 

$$n=2$$
;  $y=\frac{2(2)-1}{2}=\frac{4-1}{2}=\frac{3}{2}$ 

$$n=3$$
;  $y=\frac{2(3)-1}{2}=\frac{6-1}{2}=\frac{5}{2}$ 

$$n=4$$
;  $y=\frac{2(4)-1}{2}=\frac{8-1}{2}=\frac{7}{2}$ 

$$A - (BUC) = (A - B) \cap (A - C)$$

$$\frac{LH5}{L} - A - (BUC)$$

$$BUC = \{ \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{7}{2} \} \cup \{ \frac{1}{2}, \frac{3}{2}, \frac{3}{2} \}$$

$$= \{ \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{7}{2}, -1, \frac{1}{2} \}$$

$$A - (BUC) = \{ \frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{7}{2}, -1, \frac{1}{2} \}$$

$$A - (BUC) = \{ 3 \}$$

$$R + 5 : - (A - B) \cap (A - C)$$

$$(A - B) = \{ \frac{1}{2}, \frac{3}{2}, \frac{7}{2}, \frac{7}{2}, \frac{7}{2} \} - \{ \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{7}{2} \}$$

$$= \{ 1, 2, 3 \}$$

$$A - C = \{ \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{7}{2}, \frac{7}{2}, \frac{7}{2} \}$$

$$= \{ \frac{1}{2}, \frac{5}{2}, \frac{3}{2} \}$$

$$A - B \cap (A - C) = \{ 1, 2, 3 \} \cap \{ \frac{1}{2}, \frac{5}{2}, \frac{3}{2} \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

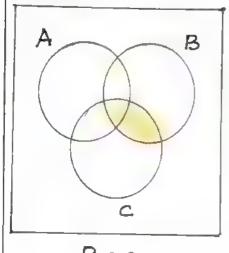
$$A - B \cap (A - C) = \{ 3 \}$$

$$A - B \cap (A - C) = \{ 3 \}$$

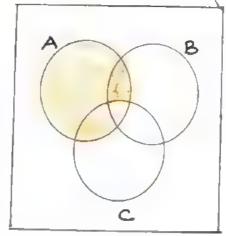
$$A - B \cap (A - C) = \{ 3 \}$$

9 Verify A-(Bnc) = (A-B)U(A-c) Using Venn diagram: -

LHS: - A- (Boc)

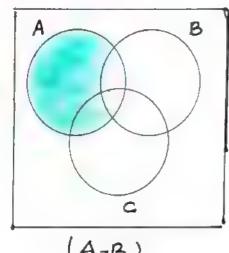




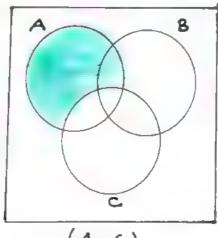


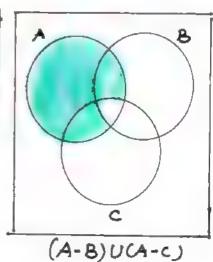
A-(BAC)

RHS: (A-B) U (A-C)



(A-B)





$$B' = \{A,7,8,10,11,14,18,16\} - \{A,8,14,18\}$$

$$= \{7,10,11,16\}$$

$$\therefore A' \cap B' = \{4,0,16\}$$

$$- \begin{bmatrix} LHs = RHs \end{bmatrix}$$

$$(ii)(A \cap B)' = A' \cup B'$$

$$LHs :- (A \cap B)'$$

$$A \cap B = \{7,8,10,11,12,15,16\} - \{8,12\}$$

$$= \{8,12\}$$

$$(A \cap B)' = \{4,7,8,10,11,12,15,16\} - \{8,12\}$$

$$A \cap B = \{4,7,10,11,15,16\}$$

$$RHs :- A' \cup B'$$

$$A' = \{4,10,15,16\} \quad [found in (i))$$

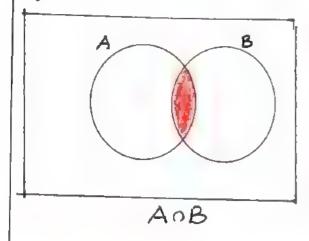
$$B' = \{7,10,11,16\} \quad [found in (i))$$

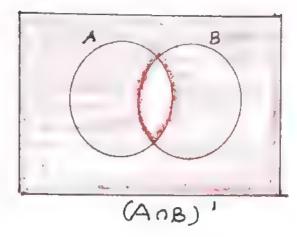
$$A' \cup B' = \{4,10,15,16\} \cup \{7,10,11,16\}$$

$$A' \cup B' = \{4,10,15,16,7,11\}$$

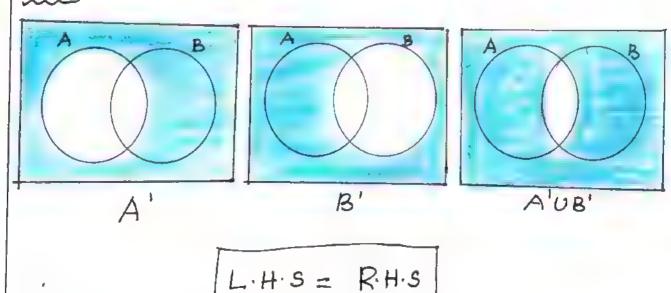
$$LHs = RHs$$

(1) Verify (AnB) = AUB Using Venn diagram: -LHS: - (AnB)





RHS: - A'UB'



① (i) If 
$$n(A) = 25$$
,  $n(B) = 40$ ,  $n(A \cup B) = 50$   
and  $n(B') = 25$ , find  $n(A \cap B)$  and  $n(U)$   
Sol!-

\* 
$$n(AUB) = n(A) + n(B) - n(ADB)$$

$$n(0) = 65$$

(ii) If 
$$n(A) = 300$$
,  $n(AUB) = 500$ ,  $n(AnB) = 50$   
and  $n(B') = 350$ ,  $find n(B)$  and  $n(U)$   
 $Sol:- (P) n(B) = ?$   
 $n(AUB) = n(A) + n(B) - n(AnB)$   
 $500 = 300 + n(B) - 50$   
 $500 = 250 + n(B)$   
 $500 - 250 = n(B)$   
 $n(B) = 250$ 

2) If 
$$U = \{x : x \in \mathbb{N}, x \leq 10\}$$
,  $A = \{2,3,4,8,10\}$   
and  $B = \{1,2,5,8,10\}$ , then Verify that  $h(AUB) = h(A) + h(B) - h(ADB)$ 

$$SOI :- A = \{2, 3, 4, 8, 10\} \Rightarrow n(A) = 5$$

$$B = \{1, 2, 5, 8, 10\} \Rightarrow n(B) = 5$$

$$A \cup B = \{2, 3, 4, 8, 10, 1, 5\} \Rightarrow n(A \cup B) = 7$$

$$A \cap B = \{2, 8, 10\} \Rightarrow n(A \cap B) = 3$$

: 
$$n(AUB) = n(A) + n(B) - n(AnB)$$
 $7 = 5 + 5 - 3$ 
 $7 = 10 - 3$ 
 $7 = 7$ 

Hence Verified.

3) Verify 
$$n(AUBUC) = n(A) + n(B) + n(C) - n(AnB)$$

$$-n(BnC) - n(CnA) + n(AnBnC)$$
for the following Sets.

(i) 
$$A = \{a, c, e, f, h\}$$
  
 $B = \{c, d, e, f\}$   
 $C = \{a, b, c, f\}$ 

$$\frac{Sol}{A} = \{a,c,e,f,h\} \Rightarrow n(A) = 5$$

$$B = \{c,d,e,f\} \Rightarrow n(B) = 4$$

$$C = \{a,b,c,f\} \Rightarrow n(C) = 4$$

$$AnB = \{a,C,e,f\} \Rightarrow n(C) = 4$$

$$AnB = \{a,C,e,f\} \Rightarrow n(AnB) = 3$$

$$BnC = \{C,d,e,f\} \Rightarrow n(BnC) = 2$$

$$BnC = \{C,f\} \Rightarrow n(BnC) = 2$$

$$AnC = \{a,c,f\} \Rightarrow n(AnC) = 3$$

$$AnBnC = \{a,c,f\} \Rightarrow n(AnBnC) = 2$$

$$AnBnC = \{a,c,f\} \Rightarrow n(AnBnC) = 2$$

$$AuBuC = \{a,c,e,f,h\} \cup \{c,d,e,f\} \cup \{a,b,c,f\}$$

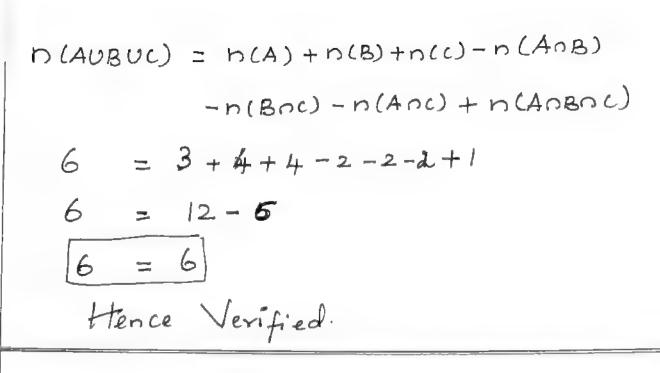
$$AuBuC = \{a,c,e,f,h,d,b\} \Rightarrow n(AuBuC) = 7$$

$$h(AuBuC) = n(A) + n(B) + n(C) - n(AnB)$$

$$h(BnC) - n(AnC) + n(AnBnC)$$

7 = 5+4+4-3-2-3+2

(ii) 
$$A = \{1, 3, 5\}$$
,  $B = \{2, 3, 5, 6\}$ ,  $C = \{1, 5, 6, 7\}$   
 $Sol := A = \{1, 3, 5\} = \}$   $n(A) = 3$   
 $B = \{2, 3, 5, 6\} = \}$   $n(B) = 4$   
 $C = \{1, 5, 6, 7\} = \}$   $n(C) = 4$   
 $Anb = \{1, 3, 5\}$   $n(2, 3, 5, 6) \Rightarrow \{3, 5\} \Rightarrow n(Anb) = 2$ 



4) In a class, all students take part in either music or drama or both. 25 Students take part in music, 30 Students take part in drama and 8 Students take part in both music and drama. Find.

(i) The number of Students who take part in Only music.

(ii) The number of Students who take Part in Only drama.

(iii) The total number of Students in the

Sol! - Given! -Number of Students take part) Number of Students take part)
in Drama = 30 Number of students take part) = 8 (i) No of Students take part in Only Music D (30) 25-8 8

(ii) No of Students take part in Only Drama

30-8

22

(iii) Total number of students

17+8+22

17+8+22

5 In a party of 45 People, each One likes tea or coffee or both.

35 People like tea and 20 people like Coffee. Find the number of people who (1) like both tea and coffee (ii) do not like Tea.

(iii) do not like Coffee.

Sol: - Given: - n(u) = n(Tuc) = 45

Total number of people => n(Tuc) = 45

Number of people like Tea => n(T) = 35

Number of people like Coffee => n(c) = 20

i) No of people who like both

tea and coffee => n(Tnc) = ?

$$P(TUL) = n(T) + n(L) - n(TDL)$$
 $45 = 35 + 20 - n(TDL)$ 
 $45 = 55 - n(TDL)$ 
 $n(TDL) = 55 - 45$ 
 $n(TDL) = 10$ 

No of people who like both tea and coffee = 10

$$= 45 - 35$$
 $n(7') = 10$ 

(iii) No of people who do not like coffee =>n(c')=?

$$n(c') = n(u) - n(c)$$
  
=  $45 - 20$   
 $n(c') = 25$ 

6. In an examination 50% of the Students passed in Mathematics and 70% of Students passed in Science while 10%. Students failed in both Subjects. 300 students passed in both both the Subjects. Find the total number of students who appeared in the examination, If they took the examination in Only two Subjects.

Sol! - Given! 
Percentage of Students passed in ? = 50%

Mathematics

Percentage of Students passed?

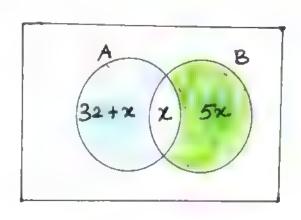
Po Science J= 70% Percentage of Students failed ? = 10%.
in both Subjects): Number of Students passed }=300 in both the Subjects : / of Students failed in } = 100/- 50/. n(M) = 50% 7. of Students failed ) in Science ) = 100% - 70%. n(s) = 30%. · · n(MUS) = n(M) +n(S) - n(MOS) = 50% + 30% -10%. Students passed in } = 100%-70%.
at least one Subject ] = 30% = 30 = 30%. = 300 . 100% = 100 x 300 = 1000 -: No of Students appeared } = 1000

the Examination J = 1000

(T) A and B are two sets Such that n(A-B) = 32+x; n(B-A) = 5x and n(AnB) = x. Illustrate the Potermation by means of a Venn diagram.

Given that n(A) = n(B), calculate the Value of x.

Sol:-



From the Venn diagram n(A) = 32+x+x = 32+2x n(B) = x+5x = 6x Given! - n(A) = n(B) 32+2x = 6x 32 = 6x-2x

$$32 = 4x$$

$$4x = 32$$

$$x = \frac{32}{4}$$

$$x = 8$$

$$\therefore \text{ n(AnB)} = 8$$

8 Out of 500 Car Owners investigated, 400 Owned Car A and 200 Owned Car B, 50 Owned both A and B cars. Is this data correct?

Sol: - Given: 
No of Owners of Car A => n(A) = 400

No of Owners of Car B => n(B) = 200

No of Owners of both Cars => n(AnB) = 50

Total no of Owners Provestigated

=> n(AUB) = 500

n(AUB) = n(A) + n(B) - n(AnB) 500 = 400 + 200 - 50 500 = 600 - 50  $500 \neq 550$ The Given data is incorrect.

9 In a colony, 275 families buy Tamil newspaper, 150 families buy English newspaper, 45 families bug Hindi newspaper, 125 families buy Tomil and English newspapers, 17 families buy English and Hindi newspapers, 5 families buy Tamil and Hindi newspapers and 3 framilies been all the three newspapers. If each family buy atleast One of these newspapers then find (i) Number of families buy Only One newspaper

- (ii) Number of families buy atleast two newspapers.
- (iii) Total number of families in the

Sol: - Given:

No of families buy

Tamil newspaper => n(A) = 275 English newspaper => n(B) = 150 Hend: newspaper => n(1) = 45

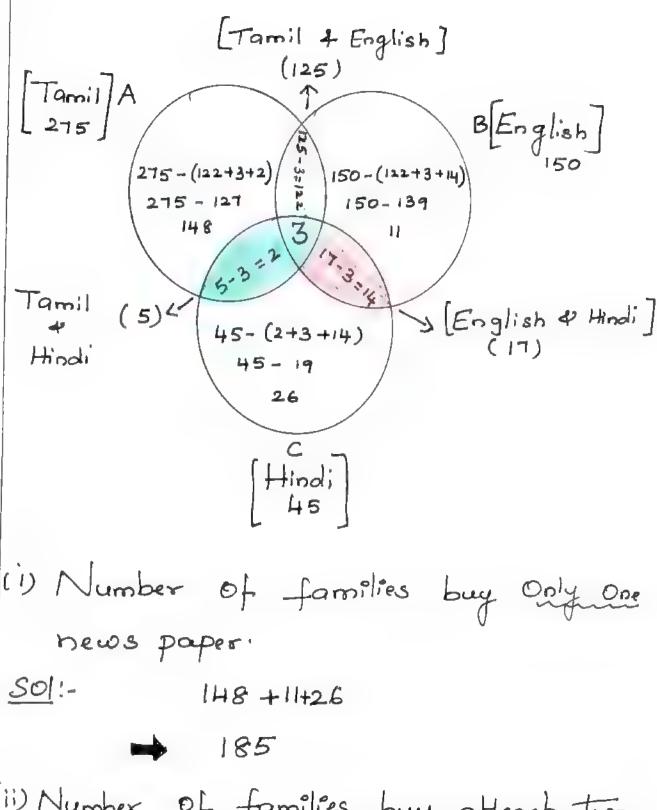
Tamil and English newspaper => n(AnB) = 125

English and Hindi newspaper => n(Bnc) = 17

Tamil and Hindi newspaper => n(Anc) = 5

Tamil, English and Hindi => n(AnBnc) = 3

newspaper



(ii) Number of families buy atteast two newspaper.



(iii) Total number of families in the colony 148+122+11+14+26+2+3

**→** 326

10 A Survey of 1000 farmers found that 600 grew paddy, 350 grew ragi, 280 grew Corn, 120 grew paddy and ragi, 100 grew ragi and Corn, 80 grew paddy and corn. It each farmer grew atleast any one of the above three, then find the number of farmers who grew all the three.

Sol! -

No of farmers Surveyed => n(AUBUC) = 1000

No of farmers grew paddy => n(A) = 600

No of farmers grew rago => n(B) = 350

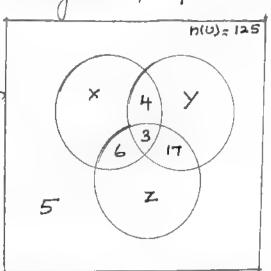
No of farmers grew corn => n(C) = 280

$$D(AUBUC) = D(A) + D(B) + D(C) - D(ADB) - D(BDC)$$
  
-  $D(ADC) + D(ADBDC)$ 

$$1000 = 600 + 350 + 280 - 120 - 100 + 80 + h(AnBox)$$

$$1000 = 1230 - 300 + h(AnBac)$$

(1) In the adjacent diagram, if n(v)=125, y is two times of x and Z is 10 more than (x 4 x, then find the Value of x, y, and Z. 5



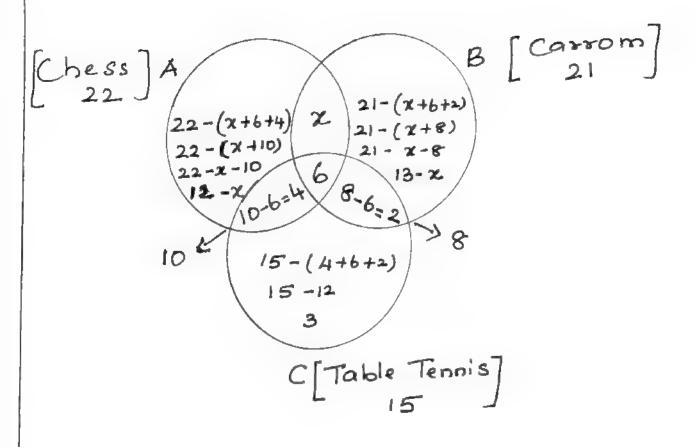
Sol! - Given! y is two times of x - | y=2x Z is 10 more than x = Z=x+10

x+y+z+4+17+6+3+5=n(U) 2+2x+x+10+35 = 125 4x + 45 = 125

Z = 30

12) Each Student in a class of 35 plays atteast one game among chess Carron and table tennis. 22 play Chess 21 play carron, 15 play table tennis, 10 play chess and table tennis, 8 play Carron and table Tennis and 6 play all the three games. Find the number of Students who play (i) Chess and Carron but not table tennis. (ii) Only Chass

(111) Only Carron. [Henit: Use Venn diagram]



(i) No q Students play chess and Carrons but not table tennis

: Students play chess and Carrom, not table tinnis=5

(ii) Student play Only Chess.

12-x

12-5

(iii) Student play only carson

13-x

13-5

13) In a class of 50 Students, each One Come to School by bus or by bicycle Or on foot. 25 by bus, 20 by bicycle, 30 on foot and 10 Students by all the three. Now how many Students Come to School exactly by two modes of toomsport?

$$n(AuBuc) = n(A) + n(B) + n(C) - n(A \cap B)$$

$$- n(BnC) - n(AnC) + n(A \cap BnC)$$

$$50 = 25 + 20 + 30 - (x + 10) - (y + 10) - (z + 10) + 10$$

$$50 = 85 - x - 10 - y - 10 - z - 10$$

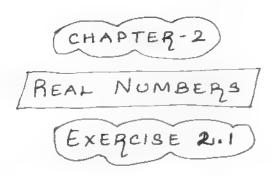
$$50 = 85 - 30 - (x + y + z)$$

$$50 = 55 - (x + y + z)$$

$$x + y + z = 55 - 50$$

$$x + y + z = 5$$

: Total number of Students Come to School exactly by two modes of Earnsports = 5



1) Which arrow best shows the position of 11 on the number line?



Position of 11 on the number line.

2) Find any throe rational numbers between -7 and 2

$$-10-9-8$$
  $-\frac{1}{11}$   $-\frac{6}{11}$   $-\frac{5}{11}$   $-\frac{4}{11}$   $-\frac{3}{11}$   $-\frac{2}{11}$   $-\frac{1}{11}$   $-\frac{2}{11}$   $-\frac{3}{11}$   $-\frac{4}{11}$   $-\frac{4}{$ 

=> Ihraa Rational numbers between

$$-\frac{1}{11}$$
 and  $\frac{2}{11}$  are  $\left(-\frac{5}{11}, -\frac{3}{11}\right)$  and  $\frac{1}{11}$ 

- 3) Find any five national numbers between
- (i) 1 and 1 5

$$\begin{array}{c}
a = 1, b = \frac{1}{5} \\
4
\end{array}$$

Five Rational numbers

$$9,=\frac{1}{2}(a+b)$$

$$=\frac{1}{2}\left(\frac{1}{4}+\frac{1}{5}\right)$$

$$=\frac{1}{2}\left(\frac{1\times5}{4\times5}+\frac{1\times4}{5\times4}\right)$$

$$=\frac{1}{2}\left(\frac{5+1+1}{20}\right)$$

$$=\frac{1}{2}\left(\frac{q}{20}\right)$$

$$9_3 = \frac{1}{2}(a+9_2)$$

$$=\frac{1}{2}\left(\frac{1}{4}+\frac{19}{80}\right)$$

$$= \frac{1}{2} \left( \frac{1 \times 20}{4 \times 20} + \frac{19 \times 1}{80 \times 1} \right)$$

$$=\frac{1}{2}\left(\frac{20+19}{80}\right)$$

$$=\frac{1}{2}\left(\frac{39}{80}\right)$$

(92= 19 80

=> Aire Plational numbers and 9, 19, 39, 79 and 159 640

1. Aire Rational numbers are 0.102, 0.103, 0.105, 0.107, 0.108

Five Rational numbers are

$$a_{1} = \frac{1}{2} (a+b)$$

$$= \frac{1}{2} (-1-2)$$

$$= \frac{1}{2} (-1-2)$$

$$= \frac{1}{2} (a+q_{1})$$

$$= \frac{1}{2} (a+q_{1})$$

$$= \frac{1}{2} (a+q_{2})$$

$$=$$

 $9_4 = \frac{1}{2} (a + 9_3)$ 

$$q_{4} = \frac{1}{2} \left( -\frac{9}{8} \right)$$

$$= \frac{1}{2} \left( -\frac{8}{8} - \frac{9}{8} \right)$$

$$= \frac{1}{2} \left( -\frac{17}{8} \right)$$

$$q_{4} = \frac{17}{16}$$

$$q_{5} = \frac{1}{2} \left( -\frac{17}{16} \right)$$

$$= \frac{1}{2} \left( -\frac{17}{16} \right)$$

$$= \frac{1}{2} \left( -\frac{33}{16} \right)$$

$$q_{5} = \frac{-33}{32}$$

$$= \frac{1}{2} \left( -\frac{33}{16} \right)$$

$$q_{5} = \frac{-33}{32}$$

$$= \frac{1}{2} \left( -\frac{33}{16} \right)$$

$$q_{5} = \frac{-33}{32}$$

$$= \frac{17}{16}$$

$$q_{6} = \frac{-33}{32}$$

$$= \frac{17}{16}$$

$$q_{7} = \frac{-33}{32}$$

1) Exposess the following national numbers into decimal and state the Kind of decimal expansion.

$$(ii) - 5\frac{3}{11}$$

$$\sqrt{-5\frac{3}{11}} = -\frac{58}{11}$$

$$\frac{22}{3} = 7.\overline{3}$$

=) It is non-terminating and
Recurring decimal.

2) Exposess 1 in decimal form. Find the length of the period of decimal.

$$\frac{1}{13} = 0.076923$$
100

=) The length of period of decimal is 6.

26

40

3) Exposess the national number  $\frac{1}{33}$  in necessing decimal expansion of  $\frac{1}{11}$ .

Hence white  $\frac{71}{33}$  in necessing decimal form.

$$\begin{array}{c|c}
1 & 0.09090... \\
11 & 100 \\
99 & \\
\hline
100 & \\
99 & \\
\hline
100 & \\
\hline
11 & 0.09 & \\
\hline
\end{array}$$

$$\frac{1}{33} = \frac{1}{3 \times 11} = \frac{0.0909...}{3} = 0.0303...$$

$$=$$
)  $\frac{1}{33} = 0.03$ 

$$\frac{71}{33} = 2\frac{5}{33}$$
$$= 2 + \left(\frac{5}{33}\right)$$

$$= 2 + \left(5 \times \frac{1}{33}\right)$$

$$= 2 + \left(5 \times 0.0303....\right)$$

$$\frac{71}{33} = 2.15$$

4) Express the following decimal expression into rational numbers. (i) 0,24 Let x = 0, 242424 - . . . . → ① (Here period of decimal, is 2) : Multiply by 100 on both Sides of 1 100x = 24, 242424···· → ②  $x = 0.242424 \cdots$ (-) 99x = 24 $x = \frac{24}{99} \Rightarrow \boxed{x = \frac{8}{33}} (\div 3)$ (1) 2.327 Let x = 2.327327.... → ① ( Period 67 decimal is 3 Multiply by 1000 on both sides of 1 1000 x = 2327, 327327...→②  $x = 2.327327 - - \rightarrow 0$ (-)999 x = 2325x = 2325999  $x = \frac{775}{333} \quad (\div 3)$ 

(iii) -5.132

Let 
$$x = -5.132$$

$$x = -5132$$
1000

$$\Rightarrow x = -1283$$
250

(÷4)

Here the repeating digit is '7' which is the second digit after decimal Point.

:. Moltiply by 10 on bis 07 10 10 x = 31.7777.... → 2

: Multiply by 10 on bis of 2

(-) 
$$100x = 317, 7777 - \cdots \rightarrow \boxed{3}$$
  $\boxed{3} - \boxed{2}$   $\boxed{90x = 286}$ 

$$\begin{array}{c}
x = 143 \\
45
\end{array} (+2)$$

Here the seperating digit is 15 which is the second digit after the decimal point.

Multiply by 10 on bis of (1)  $10x = 172.151515... \rightarrow ②$ 

Period of decimal is 2

: Multiply by 100 on bis 07 3

 $1000 \times = 17215.151515... \rightarrow 3$ (-)  $10 \times = 172.151515... \rightarrow 2$  3-2

990x = 17043

 $x = \frac{17043}{990}$ 

 $x = \frac{5681}{330} (+3)$ 

(Vi) -21, 2137

Let x=-21,2137777...→)

Home the onepeating digit is 7 which is the founth digit after the decimal Point.

... Multiply by 1000 on b.s 07 ①

1000 x = -21213.7777 .... → ②

(Period of decimal is 1)

· Multiply by 10 on b.s of 1

$$9000 x = -190924$$

$$x = -190924$$

$$x = -47731$$
2250

5) Without actual division, find which of the following sational numbers have terminating decimal expansion.

$$=\frac{7}{21\times50}$$

=) It is a terminating decimal.

$$\frac{217}{155} = \frac{7}{5^{'} \times 2^{\circ}} = \frac{7}{2^{\circ} \times 5^{'}}$$

This is of the form pm, -n

$$4\frac{9}{35} = \frac{149}{35} = \frac{149}{5\times7}$$

2 2200

2 1100

2 550

5/275

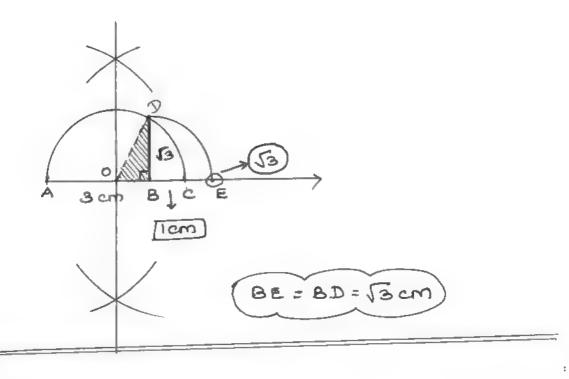
5 55

$$\frac{219}{2200} = \frac{219}{2^3 \times 5^2 \times 11}$$

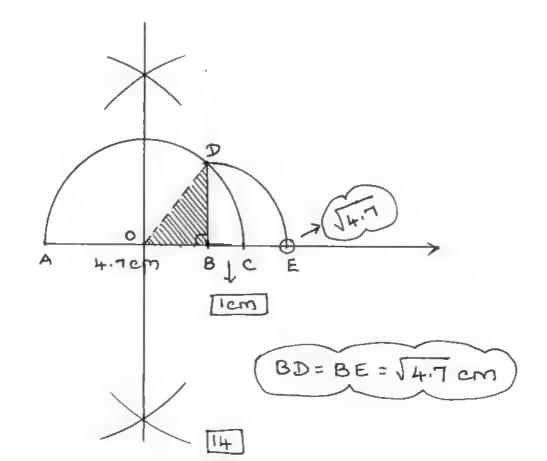


numbers on the number line.

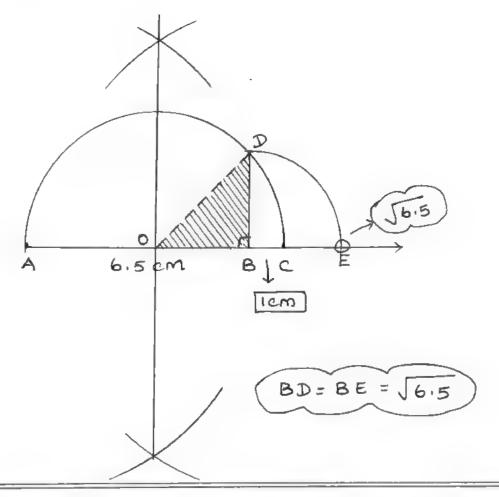
(i) \J3



(ii) J4.7



(iii) 16.5



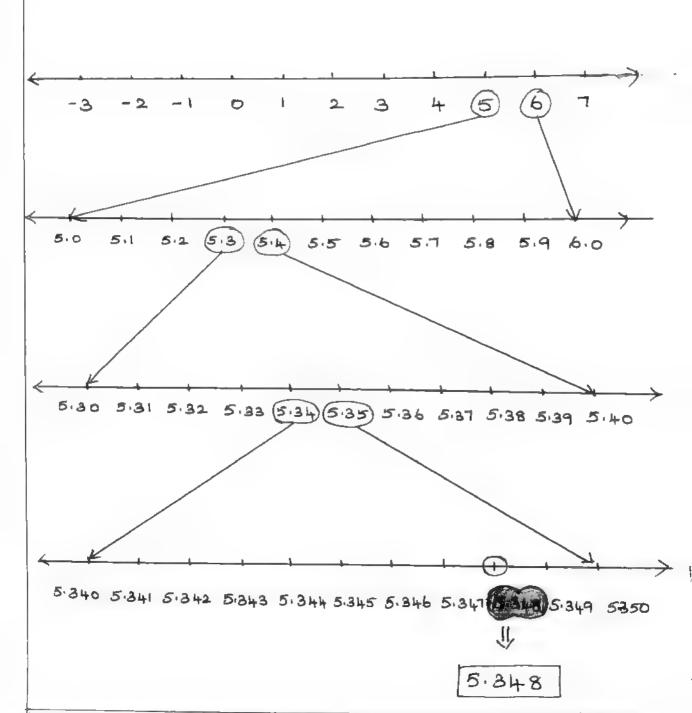
- 2) Find any two istrational numbers between
- (i) 0.3000011000111..... and
- .. Two isnational numbers are 0.30 (1)01100011.... and 0.30 (2)020002....
- (11) 6 and 12 7 13

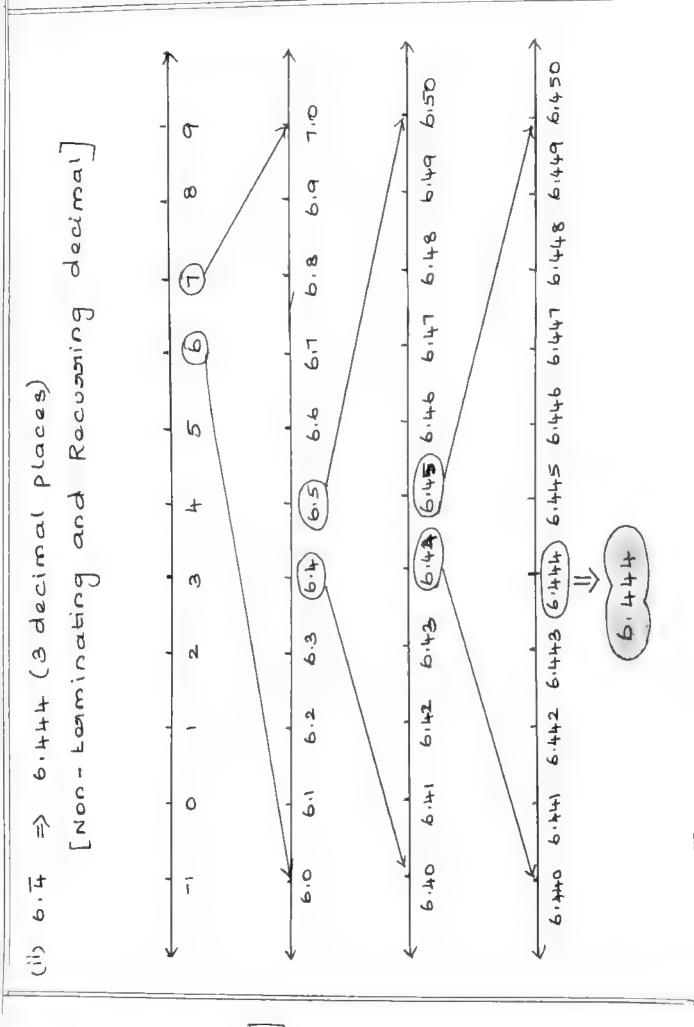
$$\frac{6}{7} = 0.85714 \cdots$$

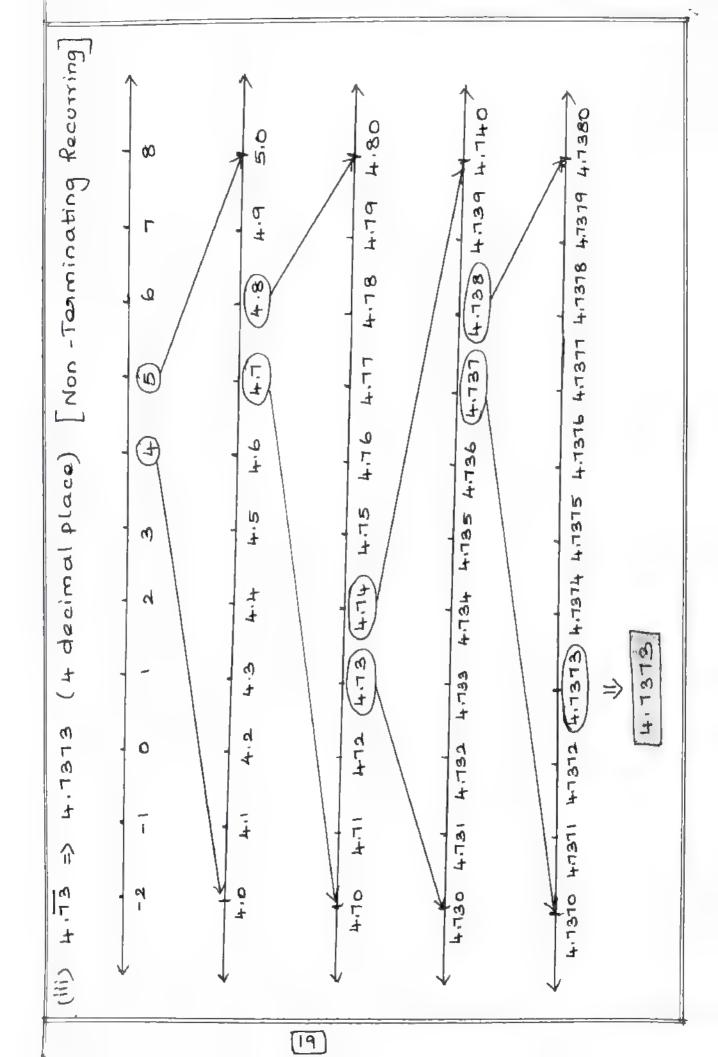
:. Two imational numbers are 0.86714 ..., 0.88230...

3) Find any two national numbers between 2.2360679.... and 2.236505500.....

- Two Rational numbers one 2,2362.... and 2,2364....
  - EXERCISE 2.4
- i) Represent the numbers on the number line.
- (i) 5.348 => [Terminating decimal]







- 1) Write the following in the form of
- (i) 625

(ii) 1/5

$$\frac{1}{5} = \frac{1}{5!} = \frac{5}{5!}$$

(iii) \[ \sqrt{5} \]

(V) J125

$$(125)^{1/2} = (5^3)^{1/2}$$

- 2) Write the following in the form of
- (i) 16

4 116

(i) 8

1-418

(iii) 32

- 1+4132
  - 4 (8

3) Find the value of:

(i) 
$$(49)^{1/2}$$
  
 $(49)^{1/2} = \sqrt{49} = \sqrt{7} \times 7 = 7$   
 $(07)$   
 $(49)^{1/2} = (7^2)^{1/2} = 7^{2\times \frac{1}{2}} = 7$ 

(ii) 
$$(243)^{2/5}$$
  
 $(243)^{2/5} = (3^5)^{2/5}$   
 $= 3^{2/3}$   
 $= 3^2$   
 $= 3^2$   
 $(243)^{2/5} = 9$ 

(9) 
$$\frac{3}{2} = (3^2)^{-\frac{3}{2}} = (3)^{\frac{2}{3}} = (3)^{-\frac{3}{2}} = (3)^{-\frac{3}{2}} = (3)^{-\frac{3}{2}} = \frac{1}{(3)^3} = \frac{1}{27}$$

(iv) 
$$\left(\frac{64}{125}\right)^{-2/3}$$

$$\left(\frac{64}{125}\right)^{-2/3} = \left(\frac{4^3}{5^3}\right)^{-2/3} = \left(\frac{4}{5}\right)^{2/3} = \left(\frac{4}{5}\right)^{-2/3} = \left(\frac{5}{4}\right)^{-2/3} = \left(\frac{5}{4}\right)^{-2/3} = \frac{25}{16}$$

4) Use a fractional index to write:

$$2 = (7)^{1/2}$$

$$\left( \frac{3\sqrt{49}}{5} \right)^{5} = \left( \frac{49}{3} \right)^{3} = \left( \frac{49}{3} \right)^{3} = \left( \frac{49}{3} \right)^{5/3} = \left( \frac{7^{2}}{3} \right)^{5/3}$$

$$= \left( \frac{3\sqrt{49}}{5} \right)^{5} = \left( \frac{7}{3} \right)^{10/3}$$

$$= \left( \frac{3\sqrt{49}}{5} \right)^{5} = \left( \frac{7}{3} \right)^{10/3}$$

$$= \left( \frac{3\sqrt{49}}{5} \right)^{5} = \left( \frac{7}{3} \right)^{10/3}$$

$$(iv) \left(\frac{1}{3\sqrt{100}}\right)^{7}$$

$$\left(\frac{1}{3\sqrt{100}}\right)^{7} = \left[\frac{1}{(100)^{1/3}}\right]^{7} = \left[\frac{1}{(100)^{1/3}}\right]^{7} = \left(\frac{1}{100}\right)^{-\frac{1}{3}} \times 7$$

$$= \sqrt{\left(\frac{1}{3\sqrt{100}}\right)^7 = \left(10\right)^{-\frac{14}{3}}}$$

$$= (100)^{-\frac{1}{3}}$$

$$= (10^{2})^{-\frac{1}{3}}$$

$$= (10)^{\frac{11}{3}}$$

(i) 32

$$32 = \sqrt[5]{32} = \sqrt[5]{2 \times 2 \times 2 \times 2 \times 2} = 2$$

$$(i) 2+3$$

$$2+3 = \sqrt[5]{2+3} = \sqrt[5]{3 \times 3 \times 3 \times 3 \times 3} = 3$$

$$(iii) 100000 = \sqrt[5]{10 \times 10 \times 10 \times 10} = 10$$

$$(iv) 1024$$

$$3125$$

$$5 \sqrt[5]{1024} = \sqrt[5]{4 \times 4 \times 4 \times 4} = \frac{1}{4}$$

$$2 \sqrt[5]{1024}$$

- 1) Simplify using addition and Subtraction properties of surds.
- (i) 5 J3 + 18 J3 2 J3
  - = 23/3-2/3
  - = 2153

(ii)  $4\sqrt{5} + 2\sqrt{5} - 3\sqrt{5}$ =  $6\sqrt[3]{5} - 3\sqrt[3]{5}$ 

3 175

5 25

2/48

2/12

= 3 5

$$=3\sqrt{3\times5\times5}+5\sqrt{2\times2\times2\times2\times3}$$

- $-3\times3\times3\times3\times3$
- $= (3 \times 5) \sqrt{3} + (5 \times 2 \times 2) \sqrt{3} (3 \times 3) \sqrt{3}$ 
  - = 15/3 + 20/3 9/3
  - = 35 \sqrt{3} -9 \sqrt{3}
  - = 26 \( \sqrt{3} \)

$$9\sqrt{3}$$
 $9\sqrt{3}$ 
 $3|2+3$ 
 $3|8|$ 
 $3|27$ 
 $3|9$ 

(iv)  $5\sqrt{40+2\sqrt{625-3\sqrt{320}}}$ 

$$= 5 \int_{2 \times 2 \times 2}^{3} \times 5 + 2 \int_{5 \times 5 \times 5}^{3} \times 5$$

$$- 3 \int_{2 \times 2 \times 2}^{3} \times 2 \times 2 \times 2 \times 2 \times 5$$

$$= (5 \times 2)^{3} \int_{5}^{5} + (2 \times 5)^{3} \int_{5}^{5} - (3 \times 2 \times 2)^{3} \int_{5}^{5}$$

$$= 10^{3} \int_{5}^{5} + 10^{3} \int_{5}^{5} - 12^{3} \int_{5}^{5}$$

$$= 8^{3} \int_{5}^{5}$$

- 2) Simplify the following using multiplication and division property of sunds:
- (i) 13×15×12

$$=\frac{\sqrt{35}}{\sqrt{7}}=\frac{355}{7}=\frac{5}{5}$$

(iii) 
$$\sqrt[3]{27} \times \sqrt[3]{8} \times \sqrt[3]{125}$$
  
=  $\sqrt[3]{3 \times 3 \times 3} \times \sqrt[3]{2 \times 2 \times 2} \times \sqrt[3]{5 \times 5 \times 5}$   
=  $3 \times 2 \times 5$   
=  $3 \times 2 \times 5$ 

$$a + b$$

25)

We know, 
$$(a-b)(a+b) = a^2 - b^2$$
  
=)  $(1\sqrt{a})^2 - (5\sqrt{b})^2$   
=  $(1\times7\times\sqrt{a}\times\sqrt{a}) - (5\times5\times\sqrt{b}\times\sqrt{b})$   
=  $49a - 25b$ 

$$(V) \begin{bmatrix} 225 \\ 729 \end{bmatrix} - \begin{bmatrix} 25 \\ 144 \end{bmatrix} \div \begin{bmatrix} 16 \\ 81 \end{bmatrix}$$

$$= \left[ \int \frac{15 \times 15}{27 \times 27} - \sqrt{\frac{5 \times 5}{12 \times 12}} \right] \div \left[ \frac{4 \times 4}{9 \times 9} \right]$$

3314

2 (1,4

= 36

3x3x2x2

$$= \left[ \frac{18}{27} - \frac{5}{12} \right) \div \left( \frac{4}{9} \right)$$

$$= \left( \frac{5}{9} - \frac{5}{12} \right) \div \left( \frac{4}{9} \right)$$

$$= \left(\frac{5\times4}{9\times4} - \frac{5\times3}{12\times3}\right) \div \left(\frac{4}{9}\right)$$

$$=\left(\frac{20-15}{36}\right)+\left(\frac{4}{9}\right)$$

$$=\left(\frac{5}{36}\right)\div\left(\frac{4}{9}\right)$$

$$=\frac{5}{3k}\times\frac{9}{4}$$

3) It  $\sqrt{2} = 1.414$ ,  $\sqrt{3} = 1.732$ ,  $\sqrt{5} = 2.236$ ,  $\sqrt{10} = 3.162$ , then find the values of the following, correct it to 3 places of decimals.

(i) 
$$\sqrt{40} - \sqrt{20}$$
  
=  $\sqrt{2 \times 2 \times 2 \times 5} - \sqrt{2 \times 2 \times 5}$ 

2 40 2 20 2 10 5	2 20 2 10 5	
2 115 12 3 147 2 2 2 3 6 (-)		

$$= \sqrt{2 \times 2 \times 3 \times 5 \times 5} + \sqrt{2 \times 3 \times 3 \times 5} - \sqrt{2 \times 2 \times 2}$$

$$=(2\times5)\sqrt{3}+3\sqrt{10}-2\sqrt{2}$$

4) Assange in descending order:

(i) 
$$\sqrt[3]{5}$$
,  $\sqrt[9]{4}$ ,  $\sqrt[6]{3}$ 
 $\sqrt[3]{5}$ ,  $\sqrt[9]{4}$ ,  $\sqrt[6]{3}$ 
 $\sqrt[3]{5}$ ,  $\sqrt[9]{4}$ ,  $\sqrt[6]{3}$ 
 $\sqrt[3]{5}$ ,  $\sqrt[3]{4}$ ,  $\sqrt[6]{5}$ 
 $\sqrt[3]{5}$ ,  $\sqrt[3]{4}$ ,  $\sqrt[3]{5}$ 
 $\sqrt[3]{5}$ ,  $\sqrt[3]{5}$ 
 $\sqrt[3]{$ 

$$= \frac{6}{5} \int_{5}^{12} \int_{7}^{12} \int_{7}^{13} \int_{8}^{12} \int_{9}^{12} \int_{9}^{12}$$

=12

5) Can you get a pune Sund when you find is the sum of two Sunds

(i) the difference of two Sunds

(ii) the product of two Sunds

(v) the quotient of two Sunds.

Justify each answer with an example.

example:  

$$4\sqrt{21} + (-3\sqrt{21})$$
  
 $= 4\sqrt{21} - 3\sqrt{21}$   
 $= \sqrt{21} \left[4-3\right]$ 

$$(eg) = 7\sqrt{25} - 6\sqrt{25}$$

$$= \sqrt[4]{25} \left[7 - 6\right]$$

$$= \sqrt[4]{25}$$

= \[ 21

$$(eq) = 3\sqrt{5} \times 3\sqrt{4}$$

$$= 3\sqrt{20}$$

$$\begin{array}{c}
(Q) = ) & \sqrt{10} = \sqrt{2 \times 5} = \sqrt{2} \times \sqrt{5} \\
\sqrt{2} & \sqrt{2} & \sqrt{2}
\end{array} = \sqrt{5}$$

- 6) can you get a rational number when you compute
  - (i) the sum of two sords
- (ii) the difference of two Boads
- (iii) the product of two surds
- (iv) the quotient of two Bunds.

Justity each answer with an example.

$$(29) =) (5-\sqrt{3})+(5+\sqrt{3})$$
  
= 5- $\sqrt{3}+5+\sqrt{3}$ 

= 10, a rational number

$$eg = (5+3\sqrt{7})-(-6+3\sqrt{7})$$
  
=  $5+3\sqrt{7}+6-3\sqrt{7}$ 

=11, a national number

$$(29) = (5+\sqrt{3})(5-\sqrt{3})$$

$$= (5)^{2} - (\sqrt{3})^{2}$$

$$= (5)^2 - (\sqrt{3})^2$$

$$(29) = ) \frac{5\sqrt{3}}{\sqrt{3}} = 5$$
, a rational number.

1) Rationalise the Denominator:

(i) 
$$\frac{1}{\sqrt{50}} = \frac{1}{\sqrt{2 \times 5 \times 5}}$$

$$= \frac{1}{5\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}$$

$$= \frac{\sqrt{2}}{5 \times 2}$$

$$= \frac{\sqrt{2}}{10}$$

$$\frac{5}{3\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{5\sqrt{5}}{3\times 5} = \frac{\sqrt{5}}{3}$$

$$\frac{\text{(iii)}}{\sqrt{18}} = \frac{\sqrt{3\times5\times5}}{\sqrt{2\times3\times3}}$$

$$= \frac{5\sqrt{3}}{3\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}$$

$$=\frac{5\sqrt{6}}{3\times 2}=\frac{5\sqrt{6}}{6}$$

(i) 
$$\sqrt{48 + \sqrt{32}}$$
  $\sqrt{27 - \sqrt{18}}$ 

$$= \frac{\sqrt{48+\sqrt{32}} \times \sqrt{527+\sqrt{18}}}{\sqrt{27}-\sqrt{18}} \times \frac{\sqrt{27}+\sqrt{18}}{\sqrt{27}+\sqrt{18}} \times \frac{(a+b)}{(a+b)}$$

$$(a+b)(a-b) = a^2 - b^2$$

$$(\sqrt{21})^2 - (\sqrt{18})^2$$

$$\sqrt{48\times27} + \sqrt{48\times18} + \sqrt{32\times27} + \sqrt{32\times18}$$

2/48

2/12

3 127

2/18

$$(2\times2\times3\times3)+(2\times2\times3)\sqrt{6}+(2\times2\times3)\sqrt{6}$$

$$= \frac{20}{90} + \frac{2456}{973}$$

$$= 20 + 856$$

$$= \frac{5\sqrt{3}+\sqrt{2}}{\sqrt{3}+\sqrt{2}} \times \frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}-\sqrt{2}}$$
(a+b) (a-b)

$$(3+12)(13-12)$$

$$(\sqrt{3})^2 - (\sqrt{2})^2$$

$$(\sqrt{3})^{2} - (\sqrt{2})^{2}$$

$$= (5\sqrt{3} \times \sqrt{3}) - (5\sqrt{3} \times \sqrt{2}) + (\sqrt{2} \times \sqrt{3}) - (\sqrt{2} \times \sqrt{2})$$

$$(5\times3) - 5\sqrt{6} + \sqrt{6} - 2$$

(iii) 256-55

$$= \frac{2\sqrt{6} - \sqrt{5}}{3\sqrt{5} + 2\sqrt{6}} \times \frac{3\sqrt{5} + 2\sqrt{6}}{3\sqrt{5} + 2\sqrt{6}}$$

$$= \frac{(2\sqrt{6}-\sqrt{5})(3\sqrt{5}+2\sqrt{6})}{(3\sqrt{5})^2 - (2\sqrt{6})^2}$$

$$= \frac{(2\sqrt{6}\times3\sqrt{5}) + (2\sqrt{6}\times2\sqrt{6}) - (\sqrt{5}\times3\sqrt{5}) - (\sqrt{5}\times2\sqrt{6})}{(9\times5) - (4\times6)}$$

$$= \frac{(\sqrt{5}\times2\sqrt{6})}{(\sqrt{5}\times2\sqrt{6})}$$

$$= \frac{\sqrt{5}}{\sqrt{5}}$$

$$= \frac{\sqrt{5}}{\sqrt{6}+2}$$

$$= \sqrt{5}$$

$$= \frac{15(\sqrt{6}-2)}{(\sqrt{6}+2)} (\sqrt{6}-2)$$

$$= \sqrt{3}6 - 2\sqrt{5} - \sqrt{3}6 - 2\sqrt{5}$$

$$= \sqrt{6} - 2\sqrt{5} - \sqrt{3}6 - 2\sqrt{5}$$

$$= -4\sqrt{5} = -4\sqrt{5} = -2\sqrt{5}$$

3) Find the value of a and b' if  $\frac{\sqrt{7}-2}{\sqrt{7}+2} = a\sqrt{7}+b$ 

LH3 J7-2 V7+2

34

$$= \frac{\sqrt{7} - 2}{\sqrt{7} + 2} \times \sqrt{7} - 2$$

$$= \frac{(\sqrt{7} - 2)^{2}}{(\sqrt{7})^{2} - (2)^{2}}$$

$$= \frac{(\sqrt{7})^{2} + (2)^{2} - 2\sqrt{7}}{(2)^{2}}$$

$$= \frac{11 - 4\sqrt{7}}{3}$$

$$= \frac{11$$

H) If  $x = \sqrt{5} + 2$ , then find the value of  $x^2 + \frac{1}{x^2}$ 

$$x = \sqrt{5+2}$$

$$x^2 = (\sqrt{5}+2)^2$$

$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$= 5+4+4\sqrt{5}$$

$$x^{2} = 9+4\sqrt{5}$$

$$= (9+4\sqrt{5}) + \frac{1}{(9+4\sqrt{5})}$$

$$= (9+4\sqrt{5})^{2} + 1$$

$$= (9)^{2} + (4\sqrt{5})^{2} + 2(9)(4\sqrt{5}) + 1$$

$$= 9+4\sqrt{5}$$

$$= 81 + (16\times5) + 72\sqrt{5} + 1$$

$$= 9+4\sqrt{5}$$

$$= 81+80+72\sqrt{5} + 1$$

$$= 9+4\sqrt{5}$$

$$= 9+4\sqrt{5}$$

$$= 9 (9+9+8\sqrt{5})$$

$$= 9+4\sqrt{5}$$

$$= 9(18+8\sqrt{5})$$

$$= 9+4\sqrt{5}$$

$$= 9\times 2(9+4\sqrt{5})$$

$$= 9+4\sqrt{5}$$

36

= 9x2

= 18

5) Given 
$$\sqrt{2} = 1.414$$
. Find the value of  $\frac{8-5\sqrt{2}}{3-2\sqrt{2}}$  in 3 decimal places.

$$\frac{8-5\sqrt{2}}{3-2\sqrt{2}} = \frac{8-5\sqrt{2}}{3-2\sqrt{2}} \times \frac{3+2\sqrt{2}}{3+2\sqrt{2}}$$

$$= (8-5\sqrt{2})(3+2\sqrt{2})$$

$$(3-2\sqrt{2})(3+2\sqrt{2})$$

$$= (8\times3) + (8\times2\sqrt{2}) - (5\sqrt{2}\times3) - (5\sqrt{2}\times2\sqrt{2})$$
$$(3)^{2} - (2\sqrt{2})^{2}$$

$$= 24 + 16\sqrt{2} - 15\sqrt{2} - (10 \times 2)$$

$$9 - (4 \times 2)$$

$$= 24 + 16\sqrt{2} - 15\sqrt{2} - 20$$

$$= \frac{24-20+16\sqrt{2}-15\sqrt{2}}{1}$$

## EXERCISE 2.8

- 1) Represent the following numbers in the Scientific Notation:
- (i) 56943000000 = 5.6943 × 1011
- (ii) 2000,57 = 2,00057×10<sup>3</sup>
- (iii) 0.000006,000=  $6.0 \times 10^{-7}$
- (iv) 0.0009,00002 = 9.000002 x 10-4
- 2) Write the following numbers in decimal form.
- (1) 3.459×106
  - = 3,459000
  - = 3459000
- (1) 5.678×104
  - = 5,6780
  - = 56780
- (III) 1.00005 x 10
  - = ,00001.00005
  - = 0.0000100005

$$(iv) 2.530009 \times 10^{-7}$$

$$= k^{0.0000002}.530009$$

$$= 0.0000002530009$$

3) Represent the following numbers in scientific Notation.

1000

$$= (3)^2 \times 10^{10} \times (2)^4 \times 10^{16}$$

$$=\frac{(1)^{11}\times10^{-66}}{(5)^{3}\times10^{-9}}$$

(iii) 
$$\int (0.00009)^{6} \times (0.00005)^{4} \int \div \int (0.009)^{3} \times (0.05)^{3} \int \frac{1}{2} = \frac{(3.0 \times 10^{-5})^{6} \times (5.0 \times 10^{-5})^{4}}{(9.0 \times 10^{-3})^{3} \times (5.0 \times 10^{-2})^{2}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{4} \times 10^{-20}}{(9)^{3} \times 10^{-9} \times (5)^{2} \times 10^{-4}}$$

$$= \frac{(3)^{6} \times 10^{-50} \times (5)^{2}}{(3^{2})^{3} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-50} \times 25}{(3)^{6} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{2}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{2}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times (5)^{7} \times 10^{-14}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-30} \times 10^{-13}}{(3)^{7} \times 10^{-13}}$$

$$= \frac{(3)^{6} \times 10^{-13} \times 10^{-13}}{($$

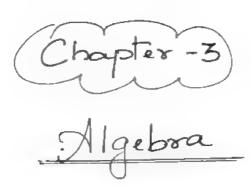
4) Represent the following information in Beientitic Notation.

(iii) 
$$(1.02 \times 10^{10}) \times (1.20 \times 10^{-3})$$
  
=  $1.02 \times 1.20 \times 10^{10-3}$   
=  $(1.22 + 0 \times 10^{7})$ 

$$= \frac{8.41 \times 10^{4}}{4.3 \times 10^{5}}$$

$$=\frac{841}{430}\times10^{4-5}$$

$$=\frac{841}{43}\times10^{-1-1}$$



1) Which of the following expressions are polynomials. It not give reason:

$$(i)$$
  $\frac{1}{x^2} + 3x - 4$ 

Sol: 
$$\frac{1}{\chi^2} + 3\chi - 4 = \chi^2 + 3\chi - 4$$

$$\underline{Sol}:=\frac{1}{2}J(x+5)=\sum_{i=1}^{n}(x+5)$$

\* One of the power of the Variable h

(iv) 
$$\frac{1}{x^{-2}} + \frac{1}{x^{-1}} + 7$$

$$\frac{S0!}{x^{-2}} - \frac{1}{x^{-1}} + \frac{1}{x^{-1}} + \frac{1}{x^{-1}} =$$
  $\chi^2 + \chi + \gamma$ 

- \* It is a polynomial.

  \* Non negative integral power.

- \* It is a polynomial.
- \* Non-negative integral power.

- \* It is not a polynomial.
- \* One of the power of Variable is fraction.
- 2) Write the coefficient of x2 and in each of the following Polynomials.

Polynomial	Coefficient of x2	coefficient
$4 + \frac{2}{5} x^2 - 3x$	2.5	-3
$6 - 2x^2 + 3x^3 - \sqrt{7}x$	-2	-19
$\pi^2 - x + 2$	T	-1
$\sqrt{3} x^2 + \sqrt{2} x + 0.5$	√3	√2
$\chi^2 - \frac{7}{2} \times + 8$		<u>-7</u>

3) Find the degree of the following polynomial Sol:

· ·		• 0
Polynomial	Degree	
1 - V2 y2+ y7	7	
$\frac{x^3 - x^4 + 6x^6}{x^2} \Rightarrow$	4	$= \frac{\left(\chi^{3} - \chi^{4} + 6\chi^{6}\right)\chi^{2}}{\chi - \chi^{2} + 6\chi^{4}}$
$\chi^3(\chi^2+\chi) \Rightarrow$	5	$\Rightarrow \chi^5 + \chi^4$
$3x^{4}+9x^{2}+27x^{6}$	6	
2 (5 p - 8 p 3 + 2 p 2 \(\frac{1}{3}\)	4	

3

(4) Rewrite the following polynomial

Sol:Polynomial Standard Form

 $x - 9 + \sqrt{7}x^3 + 6x^2$   $\sqrt{7}x^3 + 6x^2 + x - 9$ 

 $\sqrt{2} x^2 - \frac{7}{2} x^4 + x - 5 x^3 - \frac{7}{2} x^4 - 5 x^3 + \sqrt{2} x^2 + x$ 

 $7x^3 - \frac{6}{5}x^2 + 4x - 1$   $7x^3 - \frac{6}{5}x^2 + 4x - 1$ 

y2+ 55y3-11- 3y+9y4 9y4+55y3+y2-3y-11

5) Add the following polynomials and find the degree of the resultant Polynomial.

(i)  $P(x) = 6x^2 - 7x + 2$ ,  $q(x) = 6x^3 - 7x + 15$ 

 $\frac{Soli-}{P(x)+q(x)}=\frac{6x^2-7x+2}{3}$ 

 $+ \frac{6x^3+0-7x+15}{6x^3+6x^2-14x+17}$ 

Degree = 3

(ii) 
$$h(x) = 7x^3 - 6x + 1$$
,  $f(x) = 7x^2 + 17x - 9$   
Sol:-
$$h(x) + f(x) = 7x^3 + 6x^2 - 6x + 1$$

$$7x^2 + 17x - 9$$

$$7x^3 + 7x^2 + 11x - 8$$

$$\vdots$$
Degree = 3

(iii) 
$$f(x) = 16x^4 - 5x^2 + 9$$
,  $g(x) = -6x^3 + 7x - 15$   
Sol:-

$$f(x) + g(x) = 16x^{4} + 0x^{3} - 5x^{2} + 6x + 9$$

$$-6x^{3} + 0 + 7x - 15$$

(6) Subtract the Second polynomial from the first polynomial and find the degree of the resultant polynomial.

(i) 
$$P(x) = 7x^2 + 6x - 1$$
;  $q(x) = 6x - 9$ 

$$P(x) - q(x) = 7x^{2} + 6x - 1$$

$$- (+)$$

$$-7x^{2} + 8$$

(ii) 
$$f(y) = 6y^2 - 7y + 2$$
;  $g(y) = 7y + y^3$   
 $g(y) = y^3 + 7y$ 

$$f(y) - g(y) = 0 + 6y^2 - 7y + 2$$

$$-y^3 + 0 + 7y$$

$$=-y^3+6y^2-14y+2$$

Sol  

$$h(z) - f(z) = z^{5} - 6z^{4} + 0 + 0 + z + 0$$

$$-6z^{2} + 10z - 7$$

$$-7 + 7$$

$$-7 + 7 + 7$$

$$-7 + 7 + 7 + 7$$

$$-7 + 7 + 7 + 7$$

$$-7 + 7 + 7 + 7$$

$$-7 + 7 + 7 + 7$$

$$-7 + 7 + 7 + 7$$

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That Should be added to

$$2x^3 + 6x^2 - 5x + 8$$
 to get  $3x^3 - 2x^2 + 6x + 15$ ?

Sol:

Let the added polynomial = A

 $2x^3 + 6x^2 - 5x + 8 + A = 3x^3 - 2x^2 + 6x + 15$ 

$$A = (3x^3 - 2x^2 + 6x + 15) - (2x^3 + 6x^2 - 5x + 8)$$

$$= 3x^3 - 2x^2 + 6x + 15 - 2x^3 - 6x^2 + 5x - 8$$

$$A = x^3 - 8x^2 + 11x + 7$$

(8) What must be Subtracted from 2x4+4x2-3x+7 to get 3x3-x2+2x+1? Let the polynomial to be ? = B Subtracted ] = B  $\therefore 2x^{4} + 4x^{2} - 3x + 7 - B = 3x^{3} - x^{2} + 2x + 1$  $(2x^{4}+4x^{2}-3x+7)-(3x^{3}-x^{2}+2x+1)=B$  $2x^{4} + 4x^{2} - 3x + 7 - 3x^{3} + x^{2} - 2x - 1 = B$  $2x^4 - 3x^3 + 5x^2 - 5x + 6 = 8$ 

9 Multiply the following polynomials and tind the degree of the resultant Polynomial.

 $B = 2x^{4} - 3x^{3} + 5x^{2} - 5x + 6$ 

(i)  $P(x) = x^2 - 9$   $q(x) = 6x^2 + 7x - 2$ 

(10) The cost of a chocolate is Rs (x+y) and Amir bought (x+y) chocolates. Find the total amount paid by him in terms of x and y. If x=10, y=5 find the amount paid by him. <u>Sol:</u>cost of a chocolate = = = (x+y) No q chocolate Amir; = (x+y)
bought Total Amount paid = (x+y) (x+y)
by Amir = (x+y) 2  $= (10+5)^2$ Total Amount paidly by Amir

(11) The length of a rectangle is (3x+2) Units and its breadth is (3x-2) units Find its area interms of x. what will be the area if x=20 units. Sol Rectangle length = (3x+2) unils breadth = (3x-2) Units a2-62- (a+b)(a-b) Area = lxb =(3x+2)(3x-2)Given  $= (3x)^2 - 2^2$  $= 9x^2 - 4$ = 9(20) -4 = 9 (400) -4 = 3600 -4 Area = 3596 Sq. units

(12) P(x) is a polynomial of degree 1 and 9(x) is a polynomial of degree 2. What kind of the polynomial P(x) x 9(x) is ?

Sol:-Degree of P(x)=1 Degree of Q(x)=2

- Degree of P(x) x q(x) = 3

(1) Find the Value of the polynomial  $f(y) = 6y - 3y^2 + 3$  at

 $Sol:- f(y) = 6y - 3y^{2} + 3$   $f(1) = 6(1) - 3(1)^{2} + 3$  = 6 - 3 + 3 f(1) = 6

(ii) 
$$y=-1$$
  
Sol:  $-f(y) = 6y - 3y^2 + 3$   
 $f(-1) = 6(-1) - 3(-1)^2 + 3$   
 $= -6 - 3(1) + 3$   
 $= -6 - 3 + 3$   
 $f(-1) = -6$   
(1ii)  $y=0$ 

$$\frac{Sol!}{f(y)} = 6y - 3y^{2} + 3$$

$$f(0) = 6(0) - 3(0) + 3$$

$$= 0 - 0 + 3$$

(2) If 
$$P(x) = x^2 - 2\sqrt{2}x + 1$$
, Hend  $P(2\sqrt{2})$   
Sol:  $P(x) = x^2 - 2\sqrt{2}x + 1$   $(x = 2\sqrt{2})$   
 $P(2\sqrt{2}) = (2\sqrt{2})^2 - (2\sqrt{2})(2\sqrt{2}) + 1$   
 $= 4(2) - (4 \times 2) + 1$   
 $= 8 - 8 + 1$ 

$$P(2\sqrt{2}) = 1$$

(i) 
$$p(x) = x-3$$

Soll-  $p(x) = x-3$ 

Sol! 
$$P(x) = x-3$$

$$P(3) = 3-3$$

$$P(3) = 0$$

$$\frac{Sol}{p(x)} = 2x+5$$

$$p(x) = 2(x+\frac{5}{2})$$

(111) 
$$q(y) = 2y^{-3}$$

$$\frac{Sol}{}$$
:  $-2y-3$   
 $2(y) = 2(y-\frac{3}{2})$ 

$$9(\frac{3}{2}) = 2(\frac{3}{2} - \frac{3}{2})$$

$$9(\frac{3}{2}) = 2(0)$$

$$9(\frac{3}{2}) = 0$$

$$y = \frac{3}{2} \text{ is the Zero of } 9(x)$$

$$(iv) + (z) = 8z$$

$$Sol: - f(0) = 8(0)$$

$$f(0) = 0$$

$$\therefore z = 0 \text{ is the Zero of } f(z).$$

$$(v) p(x) = ax \text{ when } a \neq 0$$

$$Sol: - p(x) = ax$$

$$p(0) = a(0)$$

(vi) 
$$h(x) = ax + b$$
;  $a \neq 0$ ,  $a,b \in \mathbb{R}$   

$$\underbrace{Sol}: - h(x) = ax + b$$

$$h(x) = a(x + \frac{1}{2})$$
 $h(\frac{1}{2}) = a(\frac{1}{2} + \frac{1}{2})$ 
 $h(\frac{1}{2}) = a(0)$ 
 $h(\frac{1}{2}) = 0$ 
 $h(\frac{1}{2}) = 0$ 
 $\therefore x = -\frac{1}{2}$  is Zero of  $h(x)$ 

Sol!

Sol:

$$9x = 4$$

$$\chi = \frac{4}{9}$$

(i) 
$$P(x) = 2x-1, x = \frac{1}{2}$$

$$\underline{Sol}:-P(x)=2x-1$$

$$P(\frac{1}{2}) = 2(\frac{1}{2})^{-1}$$

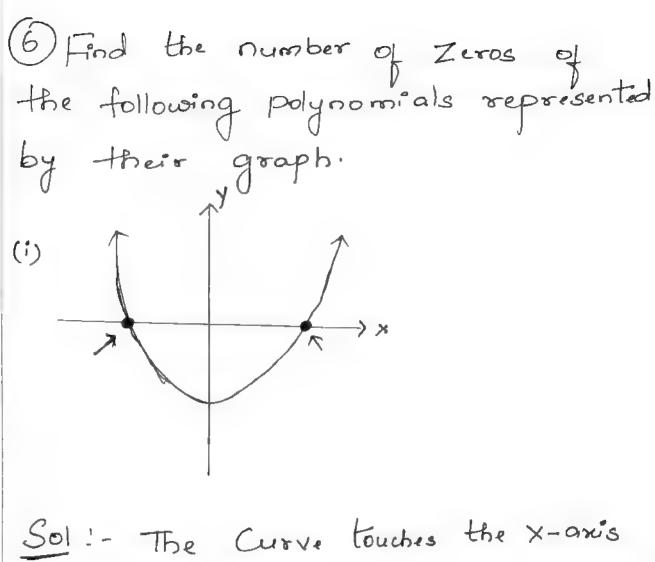
(i) 
$$P(x) = x^3 - 1$$
,  $x = 1$ 

$$p(1) = 1^3 - 1$$

Sol! 
$$P(x) = ax + b$$
 $P(-\frac{b}{a}) = a(-\frac{b}{a}) + b$ 
 $= -b + b$ 
 $P(-\frac{b}{a}) = 0$ 
 $\therefore x = -\frac{b}{a}$  is Zero of the Polynomial.

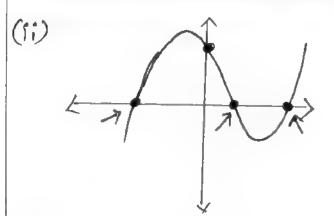
(iv)  $P(x) = (x+3)(x-4)$ ,  $x=4$ ,  $x=-3$ 
 $Sol! - P(x) = (x+3)(x-4)$ 
 $P(4) = (4+3)(4-4)$ 
 $= 7(0)$ 
 $P(4) = 0$ 
 $\Rightarrow x = 4$  is Zero of  $P(x)$ 
 $\Rightarrow x = -3$  is Zero of  $P(x)$ 

(8)



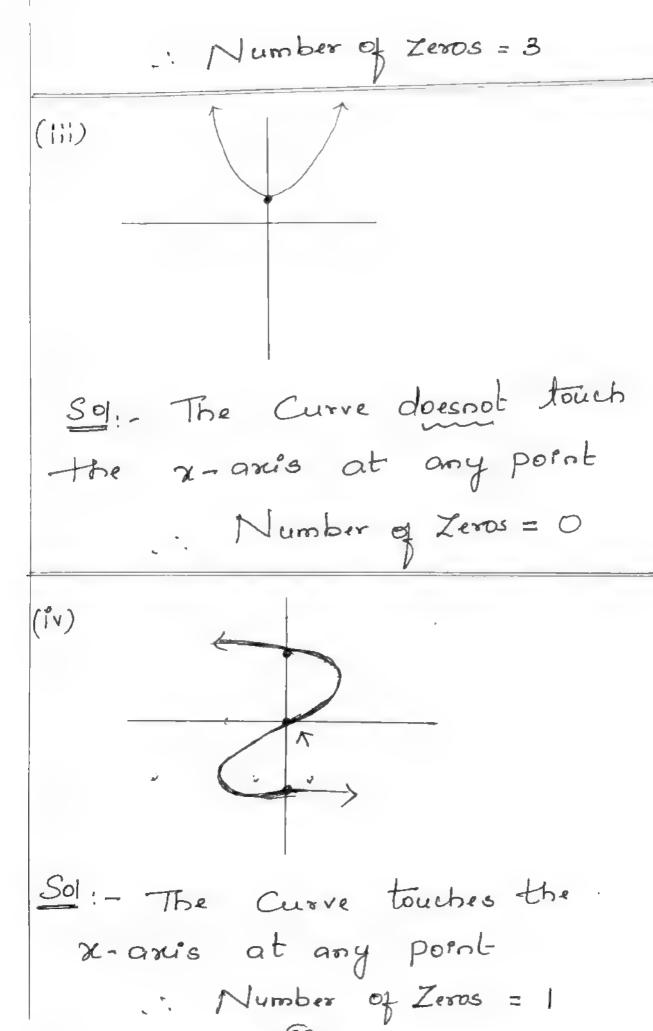
Sol! - The Curve touches the x-axis at 2 points

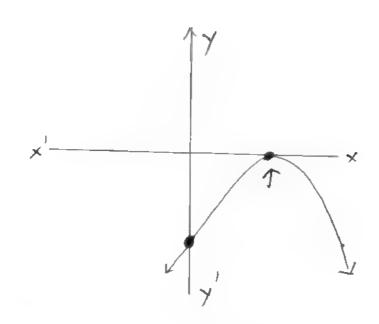
: Number of Zeros = 2



Sol: The Curve touches the x-axis at 3 points.

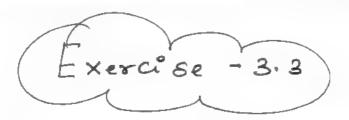
(19)





Sol: The curve touches the x-axis at One point

.. Number of Zeros = 1



of g(x) or not.

 $P(x) = x^3 - 5x^2 + 4x - 3; g(x) = x - 2$ 

 $\frac{Sol}{}$ : -  $P(x) = x^3 - 5x^2 + 4x - 3$ g(x) = x - 2

g(x) = 0

$$\chi - 2 = 0$$

$$\chi = 2$$

$$P(x) = x^{3} - 5x^{2} + 4x - 3$$

$$P(2) = 2^{3} - 5(2)^{2} + 4(2) - 3$$

$$= 8 - 5(4) + 8 - 3$$

$$= 8 - 20 + 8 - 3$$

$$= 16 - 23$$

$$P(2) = -7$$
  
-'.  $P(2) \neq 0$ 

· · · P(x) is not a multiple of g(x)

(2) By remainder theorem, find the remainder when, P(x) is divided by g(x) where

(i) P(x) = x²-2x²-4x-1; g(x) = x+1

$$\frac{Sol}{x+1} = 0$$

$$|x| = -1$$

$$P(x) = \chi^{3} - 2\chi^{2} - 4\chi - 1$$

$$P(-1) = (-1)^{3} - 2(-1)^{2} - 4(-1) - 1$$

$$= -1 - 2(1) + 4 - 1$$

$$= -1 - 2 + 4 - 1$$

$$= -4 + 4$$

$$P(-1) = 0$$

$$Remainder = 0$$

(ii) 
$$P(x) = 4x^3 - 12x^2 + 14x - 3$$
;  $g(x) = 2x - 1$   
Sol! -  $g(x) = 0$ 

$$\chi = \frac{1}{2}$$

$$P(x) = 4(\frac{1}{2})^{3} - 12(\frac{1}{2})^{2} + 14(\frac{1}{2}) - 3$$

$$= 4(\frac{1}{2})^{3} - 12(\frac{1}{2})^{2} + 14(\frac{1}{2}) - 3$$

$$= 4(\frac{1}{2})^{3} - 12(\frac{1}{2})^{2} + 14(\frac{1}{2}) - 3$$

$$= 4(\frac{1}{2})^{3} - 12(\frac{1}{2})^{2} + 14(\frac{1}{2})^{2} - 3$$

$$= \frac{1}{2} - 3 + 7 - 3$$

$$= \frac{1}{2} + 7 - 6$$

$$=\frac{1}{2}+\frac{1}{3}$$

$$=\frac{1+2}{2}$$

$$P(\frac{1}{2})=\frac{3}{2}$$

$$Permainder=\frac{3}{2}$$

(iii) 
$$P(x) = x^3 - 3x^2 + 4x + 50$$
;  $g(x) = x - 3$ 

$$g(x) = 0$$

$$x-3 = 0$$

$$\chi = 3$$

$$P(x) = x^3 - 3x^2 + 4x + 50$$

$$P(3) = (3)^3 - 3(3)^2 + 4(3) + 50$$

$$P(3) = 62$$

3) Find the remainder when 
$$3x^3-4x^2+7x-5$$
 is divided by (x+3)  $\frac{Sol}{3}$ 

Let 
$$P(x) = 3x^3 - 4x^2 + 7x - 5$$
  

$$\therefore x + 3 = 0$$

$$x = -3$$

$$- \cdot \cdot P(-3) = 3(-3)^{3} - 4(-3)^{2} + 7(-3) - 5$$

$$= 3(-27) - 4(9) - 21 - 5$$

$$= -81 - 36 - 26$$

$$\begin{array}{ccc} & & & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & \\ & & \\ &$$

$$Soli P(x) = 2x^3 - kx^2 + 3x + 10$$

$$P(x) = 0$$

$$2(2)^{3} - k(2)^{2} + 3(2) + 10 = 0$$

$$2(8) - k(4) + 6 + 10 = 0$$

$$16 - 4k + 16 = 0$$

$$32 - 4k = 0$$

$$4k = 432$$

$$k = 32$$

$$k = 8$$

6) If two polynomial  $2x^3 + ax^2 + 4x - 12$ and  $x^3 + x^2 - 2x + a$  leaves the Same remainder when divided by (x-3), find the value of a and also find the remainder.

Sol: - Let  $P(x) = 2x^3 + ax^2 + 4x - 12$  $q(x) = x^3 + x^2 - 2x + a$ 

P(x) and q(x) has Same remainder
When divided by x-3

Determine whether 
$$(x-1)$$
 is a factor of the following polynomials:

(i)  $x^3 + 5x^2 - 10x + 4$ 

Sol: -  $p(x) = x^3 + 5x^2 - 10x + 4$ 

To Check: -  $x-1$  is a factor

(è,  $p(1) = 0$ 

P(1) =  $1^3 + 5(1)^2 - 10(1) + 4$ 

=  $1 + 5(1) - 10 + 4$ 

=  $1 + 5(1) - 10 + 4$ 

=  $10 - 10$ 

·  $p(1) = 0$ 

Sol: - 
$$P(x) = x^4 + 5x^2 - 5x + 1$$

To Check:  $x-1$  is a factor  $x-1=1$ 
 $ie$ ,  $P(1) = 0$ 

$$P(1) = (1)^{4} + 5(1)^{2} - 5(1) + 1$$

$$= 1 + 5(1) - 5 + 1$$

$$= 2 + 5 - 5$$

$$P(1) = 2$$

$$Y(x-1) \text{ is not a factor.}$$

(8) Using factor theorem, Show that (x-5) is a factor of the Polynomial  $2x^{3} - 5x^{2} - 28x + 15$ 

$$P(5) = 0$$

9 Determine the Value of m, if

$$(x+3)$$
 is a factor of  $x^3-3x^2-mx+24$ 

Sol: To find:  $m=9$ 

Let;  $p(x) = x^3-3x^2-mx+24$ 

Given:  $-(x+3)$  is a factor

ie,  $p(x) = 0$ 
 $(x+3x)$ 0

 $(x+3x$ 

ID If both (x-2) and (x-\frac{1}{2}) and the factor of ax2+5x+b, then show that

$$a(2)^{2} + 5(2) + b = 0$$

$$\chi = \frac{1}{2}$$

$$a + 10 + 4b = 0$$

$$[a=b]$$

Hence Proved.

(1) If (x-1) divides the polynomial Kx3-2x2+25x-26 without Remainder then find the Value of k.  $P(x) = kx^3 - 2x^2 + 25x - 26$ ((x-1) divides p(x), Without) Remainder ) => P(1) = 0 [Without Remainder]  $K(1)^{3}-2(1)^{2}+25(1)-26=0$ K(1) - 2(1) +25-26 =0 K - 2 + 25 - 26 = 0 k-28+25 =0 K-3=0 | k = 3 |

(12) Check if (x+2) and (x-4) are the Sides of a rectangle whose area  $1\overline{s}$   $\chi^2 - 2x - 8$  by using factor theorem.

Sol: - To Check: - (21+2) and (x-4)

are Sides of Rectangle

Given: - Area =  $x^2 - 2x - 8$ ie,  $p(x) = x^2 - 2x - 8$ 

$$\chi + 2 = 0$$

$$\chi = -2$$

$$P(-2) = (-2)^2 - 2(-2) - 8$$

$$P(4) = (4)^{2} - 2(4) - 8$$

Algebraic Identities.

$$*(a+b)^2 = a^2+b^2+2ab$$

$$*(a-b)^2 = a^2 + b^2 - 2ab$$

$$*a^2-b^2=(a+b)(a-b)$$

\* 
$$(x+a)(x+b) = x^2 + (a+b)x + ab$$

\* 
$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$$

$$(x+a)(x+b)(x+c) = x^3 + (a+b+c)x^2 + (ab+bc+ca)x + abc$$

$$* (x+y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

$$(0*)$$

$$x^3 + y^3 + 3xy(x+y)$$

\* 
$$(x-y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$
  
 $(0x)$   
 $x^3 - y^3 - 3xy(x-y)$ 

\* 
$$\chi^{3} + \chi^{3} + z^{3} - 3xyz = (x+y+z)(x^{2}+y^{2}+z^{2}-xy)$$

If 
$$x+y+z=0$$
  
then;  $x^3+y^3+z^3=3xyz$ 

\* 
$$x^3 + y^3 = (x+y)^3 - 3xy(x+y)$$

\* 
$$x^3 - y^3 = (x - y)^3 + 3xy(x - y)$$

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$$

$$(x+2y+3z)^{2} = (x)^{2} + (2y)^{2} + (3z)^{2} + 2(x)(2y)$$
  
+2(2y)(3z)+2(3z)(x)

$$= 8p^{3} + (-6)4p^{2} + [20 - 24] + 2p + 60$$

$$(2p+3)(2p-4)(2p-5) = 8p^{3} - 24p^{2} + (-1)(2p) + 60$$

$$(2p+3)(2p-4)(2p-5) = 8p^{3} - 24p^{2} - 14p + 60$$

$$(3a+1)(3a-2)(3a+4)$$

$$= 801 - (2a+1)(3a-2)(3a+4)$$

$$= 801 - (2a+1)(3a-2)(3a+4)$$

$$= 801 - (2a+1)(3a-2)(3a+4) = (3a)^{2} + (a+b+c)x^{2} + (ab+bc+ca)x + abc$$

$$(3a+1)(3a-2)(3a+4) = (3a)^{2} + (1-2+4)(3a)^{2} + (1)(-2)(4)$$

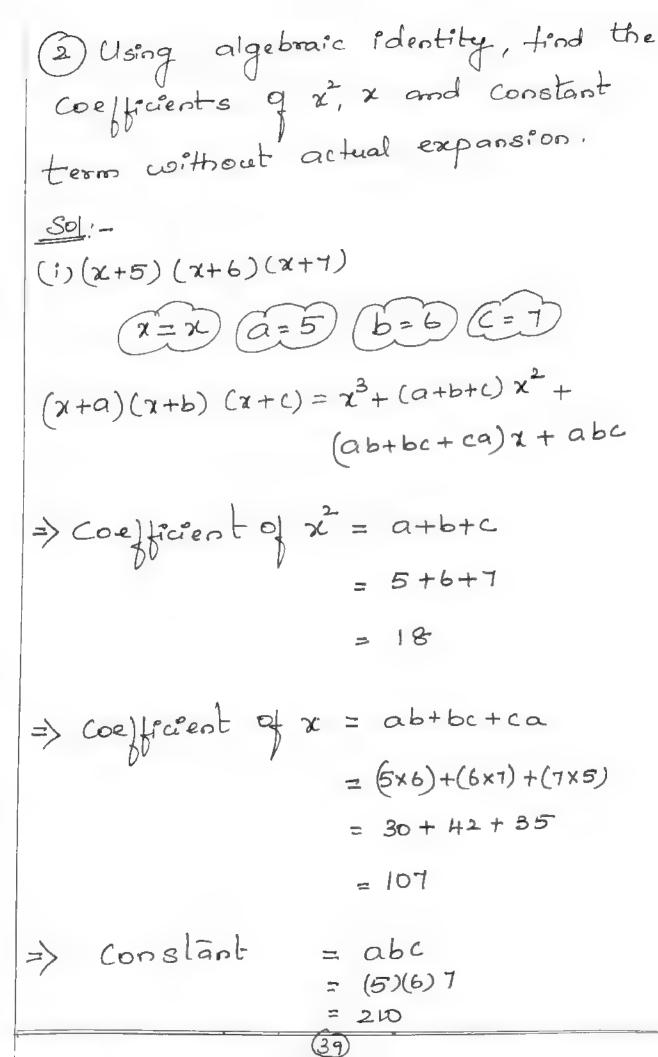
$$= 21a^{3} + (5-2)(4) + (4)(1)[3a)$$

$$+ (1)(-2)(4)$$

$$= 21a^{3} + 3(4a^{2}) + [-10+4](3a)$$

$$- 8$$

$$= 21a^{3} + 21a^{2} + (-6)(3a) - 8$$



(ii) 
$$(2x+3)(2x-5)(2x-6)$$

Sol:  $(x=2x)(a=3)(b=-5)(c=-6)$ 
 $(x+a)(x+b)(x+c)=x^3+(a+b+c)x^2+$ 
 $(ab+bc+ca)x+abc$ 

(coe) ficient of  $x^2=(3-5-6)2^2$ 
 $=(3-11)4$ 
 $=(-8)4$ 

(coe) ficient of  $x=[(3)(-5)+(-5)(-6)+(-6)(3)(2)$ 
 $=(-33+30)(2)$ 
 $=(-33+30)(2)$ 

(coe) ficient of  $x=(3)(-5)(-6)$ 

(constant = 90)

(40)

(3) If 
$$(x+a)(x+b)(x+c) = x^3 + 14x^2 + 59x + 70$$
  
find the Value of  
(i)  $a+b+c$ 

Sol: 
$$-(x+a)(x+b)(x+c) = x^3 + 4x^2 + 59x + 70$$
  
 $(x+a)(x+b)(x+c) = x^3 + (a+b+c)x^2 +$   
 $(ab+bc+ca)x+abc$ 

$$a+b+c = 14$$
 $ab+bc+bc = 59$ 
 $abc = 70$ 

(i) 
$$a + b + c = 14$$

(iii) 
$$a^2+b^2+c^2 = (a+b+c)^2 - 2(ab+bc+ca)$$
  
=  $(14)^2 - 2(5a)$   
=  $196 - 118$ 

$$(iv)$$
  $\frac{a}{bc} + \frac{b}{ac} + \frac{c}{ab}$ 

$$a^{2}+b^{2}+c^{2}=78$$

$$\frac{80! - a^{2} + b^{2} + c^{2}}{bc} = \frac{a^{2} + b^{2} + c^{2}}{abc}$$

$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$(3a-4b)^3=(3a)^3-(4b)^3-3(3a)(4b)(3a-4b)$$

$$(3a-4b)^3 = 27a^3 - 64b^3 - 108a^2b + 144ab^2$$

$$(a+b)^3 = a^3 + b^3 + 3ab (a+b)$$

$$(x+\frac{1}{y})^3 = x^3 + (\frac{1}{y})^3 + 3(x)(\frac{1}{y})(x+\frac{1}{y})$$

$$= x^{3} + \frac{1}{y^{3}} + \frac{3x}{y} (x + \frac{1}{y})$$

$$= x^{3} + \frac{1}{y^{3}} + \frac{3x^{2}}{y} + \frac{3x}{y^{2}}$$

$$= x^{3} + \frac{1}{y^{3}} + \frac{3x^{2}}{y} + \frac{3x}{y^{2}}$$

(i) 983

$$\frac{sol}{(a-b)^3} = (100-2)^3$$

$$b = 2$$

$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$98^{3} = 100^{3} - 2^{3} - 3(100)(2) (100 - 2)$$

1000000

$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

(6) If 
$$(x+y+z) = 9$$
 and  $(xy+yz+zx) = 26$ ,  
find the Value of  $x^2+y^2+z^2$ .

$$x^{2}+y^{2}+z^{2}=?$$

$$x^2 + y^2 + z^2 = (x + y + z)^2 - 2(xy + yz + zx)$$

$$=(9)^2-2(26)$$

$$\chi^2 + y^2 + z^2 = 29$$

(44)

Thind 
$$27a^3 + 64b^3$$
; If  $3a+4b=10$  and  $ab=2$ 

Sol:  $-3a+4b=10$  cubing on b.s.

$$(3a+4b)^3 = 10^3$$

$$(3a+4b)^3 = 3a+3a+3ab(a+b)$$

$$(3a)^3 + (4b)^3 + 3(3a)(4b)[3a+4b] = 1000$$

$$27a^3 + 64b^3 + 36ab[3a+4b] = 1000$$

$$27a^3 + 64b^3 + 72(10) = 1000$$

$$27a^3 + 64b^3 + 72(10) = 1000$$

$$27a^3 + 64b^3 + 720 = 1000$$

$$27a^3 + 64b^3 = 1000 - 720$$

$$27a^3 + 64b^3 = 280$$
8 Find  $x^3 - y^3$ , if  $x-y=5$  and  $xy=14$ 

8) Find 
$$x^3 - y^3$$
, if  $x - y = 5$  and  $xy = 14$ 

Sol:-
$$(x - y)^3 = 5^3$$

$$(a - b)^3 = a^3 - b^3 - 3ab(a - b)$$
(45)

$$\chi^{3} - y^{3} - 3\chi y (\chi - y) = 125$$

$$\chi^{3} - y^{3} - 3(14)(5) = 125$$

$$\chi^{3} - y^{3} - 210 = 125$$

$$\chi^{3} - y^{3} = 125 + 210$$

$$\chi^{3} - y^{3} = 335$$

9 If 
$$a+\frac{1}{a}=6$$
, then fend the Value of  $a^3+\frac{1}{a^3}$ 

$$(a+\frac{1}{a})^3 = 6^3$$
  
 $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$ 

$$a^{3} + \left(\frac{1}{a}\right)^{3} + 3(9)\left(\frac{1}{a}\right)\left[a + \frac{1}{a}\right] = 216$$

$$a^{3} + \frac{1}{a^{3}} + 3(6) = 216$$

$$a^3 + \frac{1}{a^3} + 18 = 216$$

(46)

$$a^3 + \frac{1}{a^3} = 216 - 18$$

$$a^3 + \frac{1}{a^3} = 198$$

(10) If 
$$\chi^2 + \frac{1}{\chi^2} = 23$$
, then find the Value

of 
$$x + \frac{1}{x}$$
 and  $x^3 + \frac{1}{x^3}$ 

$$\frac{Sol!}{\chi^2 + \frac{1}{\chi^2}} = 23 \implies 0$$

$$\left(\chi + \frac{1}{\chi}\right)^2 = \chi^2 + \frac{1}{\chi^2} + 2(\chi)(\frac{1}{\chi})$$

$$= \chi^{2} + \perp + 2 \qquad \text{from } 0$$

$$= \chi^{2} + \perp + 2 \qquad \text{from } 0$$

$$\left(\chi + \frac{1}{\chi}\right)^2 = 25$$

$$\chi + \frac{1}{\chi} = \sqrt{25}$$

$$\longrightarrow$$
  $\stackrel{(2)}{=}$ 

(47)

$$(x+\frac{1}{x})^3 = x^3 + \frac{1}{x^3} + 3(x)(\frac{1}{x})(x+\frac{1}{x})$$

$$\left(\chi + \frac{1}{\chi}\right)^3 = \chi^3 + \frac{1}{\chi^3} + 3\left(\chi + \frac{1}{\chi}\right)$$
 Put 2

$$(5)^3 = \chi^3 + \frac{1}{\chi^3} + 3(5)$$

$$125 = \chi^3 + \frac{1}{\chi^3} + 15$$

$$125 - 15 = \chi^3 + \frac{1}{\chi^3}$$

$$110 = \chi^3 + \frac{1}{\chi^3}$$

$$\frac{1}{x^3} + \frac{1}{x^3} = 110$$

1 If 
$$(y-\frac{1}{y})^3 = 27$$
, then find the Value

$$(y - \frac{1}{y})^{3} = 27 \rightarrow 0$$

$$(a - b)^{3} = a^{3} - b^{3} - 3ab(a - b)$$

$$y^{3} - \frac{1}{y^{3}} - 3(y)(\frac{1}{y})(y - \frac{1}{y}) = 27$$

$$y^{3} - \frac{1}{y^{3}} - 3(y - \frac{1}{y}) = 27$$

$$(y - \frac{1}{y})^{3} = 27$$

$$y^{3} - \frac{1}{y^{3}} - 3(3) = 27$$

$$y^{3} - \frac{1}{y^{3}} - 9 = 27$$

$$y^{3} - \frac{1}{y^{3}} = 27 + 9 \Rightarrow y^{3} - \frac{1}{y^{3}} = 36$$

(i) 
$$(2a+3b+4c)(4a^2+ab^2+16c^2-6ab-12bc-8ca)$$
  
Sq:-
$$(x+y+z)(x^2+y^2+z^2-xy-yz-zx)=$$

$$x^3+y^3+z^3-3xyz$$

$$\Rightarrow)(2a+3b+4c)(4a^2+qb^2+16c^2-6ab-12bc-8ca)$$

$$\therefore x=2a$$

$$y=3b$$

$$z=4c$$

$$\Rightarrow)(2a)^3+(3b)^3+(4c)^3-3(2a)(3b)(4c)$$

$$\Rightarrow)(2a)^3+(3b)^3+(4c)^3-3(2a)(3b)(4c)$$

$$\Rightarrow)(2a)^3+(3b)^3+(4c)^3-3(2a)(3b)(4c)$$

$$\Rightarrow)(3a)^3+(3b)^3+(4c)^3-3(2a)(3b)(4c)$$

$$\Rightarrow)(3a)^3+(3b$$

Z = 3Z

$$\Rightarrow \chi^{3} + y^{3} + z^{3} - 3\chi yz$$

$$\Rightarrow \chi^{3} + (-2y)^{3} + (3z)^{3} - 3(\chi)(-2y)(3z)$$

$$\Rightarrow \chi^{3} + (8y^{3}) + 27z^{3} + 18\chi yz$$

$$=> \chi^3 - 8y^3 + 27z^3 + 18xyz$$

$$a = 7$$
 $b = -10$ 
 $c = 3$ 

$$-1 + (-10)^3 + 3^3 = 3(-1)(-10)(3)$$

$$7^3 - 10^3 + 3^3 = -630$$

If 
$$a+b+c=0$$
, then  $a^3+b^3+c^3=3abc$ 

$$\Rightarrow |^{3} + \left(\frac{1}{2}\right)^{3} + \left(\frac{-3}{2}\right)^{3}$$

$$a = 1$$

$$b = \frac{1}{2}$$

$$C = -\frac{3}{2}$$

$$\left(\frac{1}{2}\right)^{3} + \left(\frac{-3}{2}\right)^{3} = 3\left(1\right)\left(\frac{1}{2}\right)\left(\frac{-3}{2}\right)$$

$$\left[ \frac{3}{1} + \left( \frac{1}{2} \right)^{3} + \left( \frac{-3}{2} \right)^{3} = \frac{-9}{4} \right]$$

$$8x^3 - 27y^3 - 64z^3$$
.

$$\Rightarrow 8x^{3} - 27y^{3} - 64z^{3} = (2x)^{3} + (-3y)^{3} + (-4z)^{3}$$

$$0 = 2x$$

$$b = -3y$$

$$C = -4z$$

$$(2x)^{3} + (-3y)^{3} + (-4z)^{3} = 3(2x)(-3y)(-4z)$$

$$(2x)^{3} + (-3y)^{3} + (-4z)^{3} = 72xyz$$

Tolentity

(\* 
$$a^3 - b^3 = (a-b)(a^2+ab+b^2)$$

(\*  $a^3+b^3 = (a+b)(a^2-ab+b^2)$ 

Exercise -3.5

$$\frac{Sol:-}{2a^{2}+4a^{2}b+8a^{2}c}$$
=>  $2a^{2}(1+2b+4c)$ 

(ii) 
$$ab - ac - mb + mc$$
  
 $801$   $ab - ac - mb + mc$   
 $\Rightarrow a(b-c) - m(b-c)$   
 $\Rightarrow (b-c)(a-m)$   
(2)  $factorize$  the following:  
(1)  $\chi^2 + 4\chi + 4$   
 $801: - \chi^2 + 4\chi + 4 = \chi^2 + 2(2\chi) + 2^2$   
 $= (\chi + 2)^2$   
(iii)  $3a^2 - 24ab + 48b^2$   
 $\Rightarrow 3(a^2 - 8ab + 16b^2)$   
 $\Rightarrow 3(a^2 - 2(4b)(a) + (4b)^2)$   $a^2 - 2ab + b^2$   
 $\Rightarrow 3(a - 4b)^2$   $a = a$   
 $\Rightarrow 3(a - 4b)^2$ 

(54)

Sol: 
$$x^5 - 16x = x(x^4 - 16)$$
  
=  $x(x^2)^2 - 4^2$   
=  $x(x^2 + 4)$ 

$$= \chi \left(\chi^{2} - 2^{2}\right) \left(\chi^{2} + 4\right)$$

$$x^{5}-16x = x(x-2)(x+2)(x+4)$$

$$(iv)$$
  $m^2 + \frac{1}{m^2} - 23$ 

$$\frac{Sol}{m^2+1} - 23$$

$$= \rangle \left(m + \frac{1}{m}\right)^{2} - 2(m)\left(\frac{1}{m}\right) - 23 \qquad b = \frac{1}{m}$$

$$=$$
  $\left(m + \frac{1}{m}\right)^2 - 2 - 23$ 

$$\Rightarrow \left(m + \frac{1}{m}\right)^2 - 25$$

$$\Rightarrow \left(m + \frac{1}{m}\right)^2 - 5^2$$

$$\Rightarrow$$
  $\left[\left(m+\frac{1}{m}\right)+5\right]\left[\left(m+\frac{1}{m}\right)-5\right]$ 

$$a = \chi^{2}$$

$$b = 4$$

$$a - b = \chi^{2}$$

(a+b)(a-b

a+6=(a+6)-2ab

a2-b=(a+b)(a-b)

$$(V) 6 - 216x^{2}$$

$$S0[:-6 - 216x^{2}] = 6(1 - 36x^{2})$$

$$= 6[1 - (6x)^{2}]$$

$$= 6[(1+6x)(1-6x)]$$

$$= 6[(1+6x)(1-6x)]$$

$$\frac{(\text{Vi})}{a^2} = \frac{1}{a^2} - 18$$

$$\frac{\text{Sol}!}{a^2} = \frac{1}{a^2 + 1} - 18$$

$$\frac{(\text{Vi})}{a^2} = \frac{1}{a^2 + 1} = \frac{1}{a^2} = \frac{1}$$

=> 
$$(a - \frac{1}{a})^2 + 2(a)(\frac{1}{a}) - 18$$
  $a = a$   $b = \frac{1}{a}$ 

$$=> (a+\frac{1}{a})^{2} + 2 - 18$$

$$\Rightarrow (a-\frac{1}{a})^2 - 16$$

$$= (a - \frac{1}{a})^2 - 4^2$$

$$a = a - \frac{1}{a}$$
 $b = 4$ 

(i) 
$$4x^2 + 9y^2 + 35z^2 + 12xy + 30yz + 20xz$$
  
Sol:  $-4x^2 + 9y^2 + 35z^2 + 12xy + 30yz + 20xz$   
=>  $(2x)^2 + (3y)^2 + (5z)^2 + 2(2x)(3y) + 2(3y)(5z) + 2(5z)(2x)$   
=>  $(2x + 3y + 5z)^2$   
(ii)  $25x^2 + 4y^2 + 9z^2 - 20xy + 12yz - 30xz$   
Sol:  $-25x^2 + 4y^2 + 9z^2 - 20xy + 12yz - 30xz$   
=>  $(-5x)^2 + (2y)^2 + (3z)^2 + 2(-5x)(2y) + 2(3z)(-5x)$   
=>  $(-5x)^2 + (2y)^2 + (3z)^2 + 2(-5x)(2y) + 2(3z)(-5x)$   
=>  $(-5x)^2 + 2y + 3z)^2$   
(5)

(i) 
$$8x^3 + 125y^3$$

Set  $8x^3 + 125y^3$ 
 $\Rightarrow (2x)^3 + (5y)^3$ 
 $\Rightarrow (2x)^3 + (5y)^3$ 
 $\Rightarrow (2x + 5y)((2x)^2 + (5y)^2 - (2x)(5y))$ 
 $\Rightarrow (2x + 5y)[4x^2 + 25y^2 - 10xy]$ 

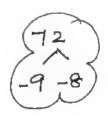
(ii)  $27x^3 - 8y^3 = (3x)^3 - (8y)^3$ 
 $\Rightarrow (3x - 2y)((3x)^2 + (2y)^2 + (3x)(2y))$ 
 $\Rightarrow (3x - 2y)[9x^2 + 4y^2 + 6xy]$ 

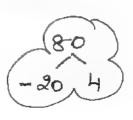
(iii)  $a^6 - 64$ 

Sol:  $a^6 - 64 = (a^2)^3 - 4^3$ 
 $\Rightarrow (a^2 - 4)(a^2)^2 + 4^2 + (a^2)(4)$ 
 $\Rightarrow (a^2 - 2)(a + 2)(a^4 + 16 + 4a^2)$ 
 $\Rightarrow (a^2 - 2)(a + 2)(a^4 + 16 + 4a^2)$ 
 $\Rightarrow (a^2 - 2)(a + 2)(a^4 + 16 + 4a^2)$ 

(i) 
$$x^2 + 10x + 24$$

(ii) 
$$Z^2 + 4z - 12$$





(vi) 
$$a^2 + 10a - 600$$

Sol:  $-(a + 30)(a - 20)$ 

(2) Factor'se the following:  $-$ 

(1)  $2a^2 + 9a + 10$ 

Sol:  $-2a^2 + 9a + 10$ 

(20)

 $-2a^2 + 9a + 10$ 

(30)

(2)

 $-2a^2 + 9a + 10$ 

(30)

(2)

 $-2a^2 + 9a + 10$ 

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60

= (2x-3)(4x-3)

(iv) 
$$6x^2 + 16xy + 8y^2$$
  
 $\frac{Sol}{6x^2 + 16xy + 8y^2}$   
 $2(3x^2 + 8xy + 4y^2)$   
 $2(x+2y)(3x+2y)$ 

$$\begin{array}{c|c}
(12y^2) \\
2y \\
3x \\
3x
\end{array}$$

$$(V)$$
  $12x^2 + 36x^2y + 27y^2x^2$ 

$$\frac{Sol}{-}$$
  $12x^2 + 36x^2y + 27y^2x^2$ 

$$3x^{2}(4 + 12y + 9y^{2})$$

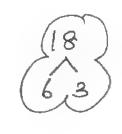
$$\Rightarrow$$
  $3x^{2}(4y^{2}+12y+4)$ 

$$\Rightarrow 3x^{2}(3y+2)(3y+2)$$

$$(Yi)(a+b)^2+9(a+b)+18$$

$$=$$
  $\chi^2 + 9\chi + 18$ 

$$(x+6)(x+3)$$



(i) 
$$(P-q)^2 - 6(P-q) - 16$$
  
Sol:  $(P-q)^2 - 6(P-q) - 16$   
Let  $(P-q)^2 - 6(P-q) - 16$   
Let  $(P-q)^2 - 6(P-q) - 16$   
 $(x-8)(x+2)$   
 $\Rightarrow (P-q-8)(P-q+2)$   
(ii)  $m^2 + 2mn - 24n^2$   
Sol:  $(m+6n)(m-4n)$   
(iii)  $\sqrt{5}a^2 + 2a - 3\sqrt{5}$   
 $\sqrt{5}a^3 + 2a - 3\sqrt{5}$   
 $\sqrt{5}a^3 + 2a - 3\sqrt{5}$   
( $\sqrt{5}a-3$ ) ( $\sqrt{5}a+5$ )  
(iv)  $a^4 - 3a^2 + 2$   
Sol:  $a^4 - 3a^2 + 2$   
 $a^4 -$ 

$$\frac{Sol}{m} = 8m^3 - 2m^2 n - 15m^2$$
  
 $m(8m^2 - 2mn - 15n^2)$   
 $m(2m - 3n)(4m + 5n)$ 

$$(120n^2)$$
 $(-12n)$ 
 $(8m)$ 
 $(2)$ 
 $(4)$ 

$$(vi) \frac{1}{2^2} + \frac{1}{y^2} + \frac{2}{2y}$$

$$\Rightarrow \left(\frac{1}{x}\right)^2 + \left(\frac{1}{y}\right)^2 + 2\left(\frac{1}{x}\right)\left(\frac{1}{y}\right)$$

$$\Rightarrow \left(\frac{1}{x} + \frac{1}{y}\right)^2$$



(i) 
$$(4x^3+6x^2-23x+18)$$
  $\div$   $(x+3)$ 

Sol: 
$$-4x^2 - 6x - 5$$
  
 $4x^3 + 6x^2 - 23x + 18$   
 $-6x^2 - 6x$   
 $-6x^2 - 6x$   
 $-6x^2 - 6x$   
 $-6x^2 - 6x$   
 $-5x - 18x$   
 $-5x - 15$ 

Quotient = 
$$4x^2-6x-5$$

Remainder = 33

$$(ii)(8y^3-16y^2+16y-15)\div(2y-1)$$

$$2y-1$$
  $8y^{3}-16y^{2}+16y-15$   $8y^{3}-4y^{2}$ 

$$-12y^{2}+6y$$
(+)
(-)
 $10y-15$ 

(iii) 
$$(8x^3-1) \div (2x-1)$$

Sol! -  $8x^3 + 0x^2 + 0x - 1$ 
 $4x^2 + 2x + 1$ 
 $8x^3 + 0x^2 + 0x - 1$ 
 $8x^3 - 4x^2$ 

(+)

 $4x^2 + 0x$ 
 $4x^2 + 0x$ 
 $4x^2 - 2x$ 

(-)  $4x^2 - 2x$ 

(-)  $4x^2 - 2x$ 

(-)  $4x^2 - 2x$ 

(-)  $4x^2 - 2x$ 

$$(1V) \left(-18z + 14z^{2} + 24z^{3} + 18\right) \div (3z + 4)$$

$$\frac{Sol}{-}\left(-18z + 14z^{2} + 24z^{3} + 18\right) \div (3z + 4)$$

$$\Rightarrow \left(24z^{3} + 14z^{2} - 18z + 18\right) \div (3z + 4)$$

$$\frac{8z^{2} - 6z + 2}{24z^{3} + 14z^{2} - 18z + 18}$$

$$\frac{24z^{3}}{3z} = 8z^{2}$$

$$\frac{24z^{3}}{3z} = 8z^{2}$$

$$\frac{24z^{3}}{3z} = 6z$$

$$\frac{24z^{3}}{3z} = -6z$$

$$\frac{-18z^{2} - 24z}{(+)}$$

$$\frac{6z + 18}{(-)}$$

$$\frac{6z + 18}{(-)}$$

Remainder = 10

2) The area of a rectangle is

$$\chi^2 + 7x + 12$$
. It its breadth is (x+3)

then find its length.

Sol:-

Area of rectangle =  $\chi^2 + 7x + 12$ 

Area of rectangle = 
$$x^2 + 7x + 12$$
  
breadth =>  $b = x+3$   
length =>  $l = ?$   
 $l \times b = Area$   
 $l(x+3) = x^2 + 7x + 12$   
 $l = x^2 + 7x + 12$ 

$$x + 4$$
 $x + 3$ 
 $x + 4$ 
 $x + 3$ 
 $x + 3$ 
 $x + 3$ 
 $x + 12$ 
 $x + 13$ 
 $x + 13$ 
 $x + 14$ 
 $x + 14$ 

(3) The base of a parallelogram is (5x+4). Frod its height, if the area is 25x2-16.

Sol:- Parallelogram

base = 5x+4Area =  $bxh = 25x^2-1b$ height = ?

 $bxh = 25x^{2}-16$   $h = 25x^{2}-16$  5x+4

 $= (5x)^{2} - 4^{2}$  = 5x + 4

$$=(5x-4)(5x+4)$$
 $(5x+4)$ 

a-b=(a-b)

(4) The Sum of (x+5) Observations is (x3+125). Find the mean of the Observation. Sol: -Number of Observation = x+5 Sum of Observation = x3+125 Mean of Observation = ? 2 Sum of observation Number of Observation  $= \chi^3 + 125$ a3+63=  $= \chi^3 + 5^3$  $=(\chi+5)(\chi^2+5^2-(5)(\chi))$ (x+5)

Mean =  $\chi^2 + 25 - 5\chi$ 

(5) Find the quotient and remainder for the following using synthetic division:

(i) 
$$(x^3+x^2-7x-3)$$
 ÷  $(x-3)$ 

$$\underline{\underline{Sol}}:=\left(\chi^{3}+\chi^{2}-7\chi-3\right)\div(\chi-3)$$

$$x - 3 = 0$$

(11) 
$$(\chi^3 + 2\chi^2 - \chi - 4) \div \chi + 2$$

2+2=0

X = -2

(iii) 
$$(3x^3 - 2x^2 + 7x - 5) \div (x + 3)$$
  
 $\frac{Sol}{x = -3}$   
 $-3$   $\frac{3}{2}$   $\frac{-2}{2}$   $\frac{7}{2}$   $\frac{-5}{2}$   
 $\frac{3}{2}$   $\frac{-11}{2}$   $\frac{40}{2}$   $\frac{-125}{2}$ 

$$Sol: 4x+1=0$$
 $4x=-1$ 
 $x=-\frac{1}{4}$ 

Quotient = 
$$\frac{1}{4} \left[ 8x^3 - 2x^2 - \frac{3}{2}x + \frac{51}{8} \right] = \frac{51}{32}$$

Remainder = 109/32

Sol:-Given quotient = 4x3+px2-qx+3 (8x4-2x2+6x-7)+2x+1

$$2x+1=0$$

$$2x=-1$$

$$2=-\frac{1}{2}$$

-1 x8 = -4

-1 x 6 = -3

Quotient obtained =  $= \frac{1}{2} [8x^{3} + x^{2} + 6]$   $= \frac{1}{2} \times \times [4x^{3} - 2x^{2} + 3]$ 

Obtained Quotient = 
$$4x^3 - 2x^2 + 0x + 3$$
  
Given Quotient =  $4x^3 + px^2 - qx + 3$   

$$P = coeff of  $x^2 \mid q = coeff of x$ 

$$P = -2 \qquad | 9 = 0$$
Remainder = -10$$

The quotient obtained on dividing 3x3+11x2+34x+106 by x-3
is 3x2+ax+b, then find q,b and also the remainder.

Given quotient =  $3x^2 + ax + b$   $(3x^3 + 11x^2 + 3+x + 106) + (x-3)$  x-3=0x=3

(13)

Obtained Quotient = 
$$3x^2 + 20x + 24$$

Given Quotient =  $3x^2 + ax + b$ 
 $a = \text{Coeff of } x$ 
 $b = \text{Constant}$ 
 $a = 20$ 

Femainder =  $388$ 

The following Polynomials using Synthetic

division: -

(i) 
$$\chi^3 - 3\chi^2 - 10\chi + 24$$

Sol: - | | -3 -10 24

0 | -2 -12 | |  $\sqrt{5} \neq 0$ 

- :  $(\chi - 1)$  is not a factor

$$\chi^2 - \chi - 12 = (\chi + 3)(\chi - 4)$$

$$= > (x-2)(x+3)(x-4)$$

(ii) 
$$2x^3 - 3x^2 - 3x + 2$$

$$\frac{Sol}{0}$$
 $\frac{1}{2}$   $\frac{-3}{-3}$   $\frac{-3}{2}$   $\frac{2}{71-1}$  is not a
 $\frac{2}{2}$   $\frac{-1}{-4}$   $\frac{-4}{-2}$  factor

(78)

$$(\chi-1)$$
 is a factor  
 $+\chi^2 + 4\chi - 3 = (2\chi+3)(2\chi-1)$ 

$$=>(x-1)(2x+3)(2x-1)$$

$$(1)$$
  $\chi^3 + \chi^2 - 14\chi - 24$ 

(x-1) is not a

-factor

9

when 
$$\chi = -1$$
;  $P(-1) = (-1)^3 + (-1)^2 - 14(-1) - 24$   
 $= -1 + 14 - 24$   
 $P(-1) = -10$   
 $(\chi + 1)$  is not a factor  
When  $\chi = 2$ ,  $P(2) = (2)^3 + (2)^2 - 14(2) - 24$   
 $= 8 + 4 - 28 - 24$   
 $= 12 - 52$   
 $P(2) = 40$   
 $(\chi - 2)$  is not a factor  
When  $\chi = -2$ ;  $P(-2) = (-2)^3 + (-2)^2 - 14(-2) - 24$ 

When 
$$x = -2$$
;  $P(-2) = (-2)^3 + (-2)^2 - 14(-2) - 24$   
 $= -8 + 4 + 28 - 24$   
 $= -32 + 32$   
 $P(-2) = 0$ 

- (x+2) is a factor

$$(x-1) \text{ is } a \text{ factor}$$

$$= x^2 + x - 6 = (x+3)(x-2)$$

$$= x^2 + x - 6 = (x+3)(x-2)$$

$$(Vi) \quad \chi^{3} = 10\chi^{2} - \chi + 10$$

$$Sol \quad \chi^{3} = 10\chi^{2} - \chi + 10$$

$$\begin{vmatrix} 1 & -10 & -1 & 10 \\ 0 & 1 & -9 & -10 \\ \hline 1 & -9 & -10 & 0 \end{vmatrix}$$

$$\therefore (\chi - 1) \quad \text{is a factor}$$

$$\Rightarrow \chi^{2} = 9\chi - 10 = (\chi - 10)(\chi + 1)$$

$$\Rightarrow (\chi - 1)(\chi - 10)(\chi + 1)$$

(i) 
$$P^5$$
,  $P^{"}$ ,  $P^9$ 

Sol  $P^5$ ,  $P^{"}$ ,  $P^9$ 

GLD =  $P^5$ 

(Vii) 25 abc, 100 abc, 125 ab

Sol: 25abc = 5x5abc

100 a2bc = 2x2x5x5 a2bc

125 ab = 5x5 ab

GLD = 5x5ab

GW = 25ab

(Viii) 3abc, 5xyz, 7Pgr

Sol: - 3abc, 5xyz, 7Pgr

: G CD = 1

(2) Find the G. UD of the following:

i) (2x+5), (5x+2)

Sol: - GCD =1

(11)  $a^{m+1}$ ,  $a^{m+2}$ ,  $a^{m+3}$ 

Sol:-
$$a^{m+1} = a^{m} \times a^{1}$$

$$a^{m+2} = a^{m} \times a^{2}$$

$$a^{m+3} = a^{m} \times a^{3}$$

$$\therefore GD = a^{m} \times a^{1}$$

$$GCD = a^{m+1}$$

$$\frac{Sol}{2a^{2}+a} = a(2a+1)$$

$$4a^{2}-1 = (2a)^{2}-1^{2}$$

$$= (2a-1)(2a+1)$$

$$\frac{GcD}{2a+1} = 2a+1$$

$$(iv)$$
  $3a^2$ ,  $5b^3$ ,  $1c^4$ 

(v) 
$$x^{4}-1$$
;  $x^{2}-1$   
 $\leq 0$ :-  $x^{4}-1 = (x^{2})^{2}-1$   
 $= (x^{2}-1)(x^{2}+1)$   
 $= (x-1)(x+1)(x^{2}+1)$   
 $x^{2}-1 = (x-1)(x+1)$   
 $\therefore GcD = (x-1)(x+1)$   
(vi)  $a^{3}-qax^{2}$ ;  $(a-3x)^{2}$   
 $\leq 0$ :-  $a^{3}-qax^{2} = a(a^{2}-qx^{2})$   
 $= a(a^{2}-(3x)^{2})$   
 $= a(a-3x)(a+3x)$   
 $(a-3x)^{2} = (a-3x)(a-3x)$   
 $GcD = (a-3x)$ 

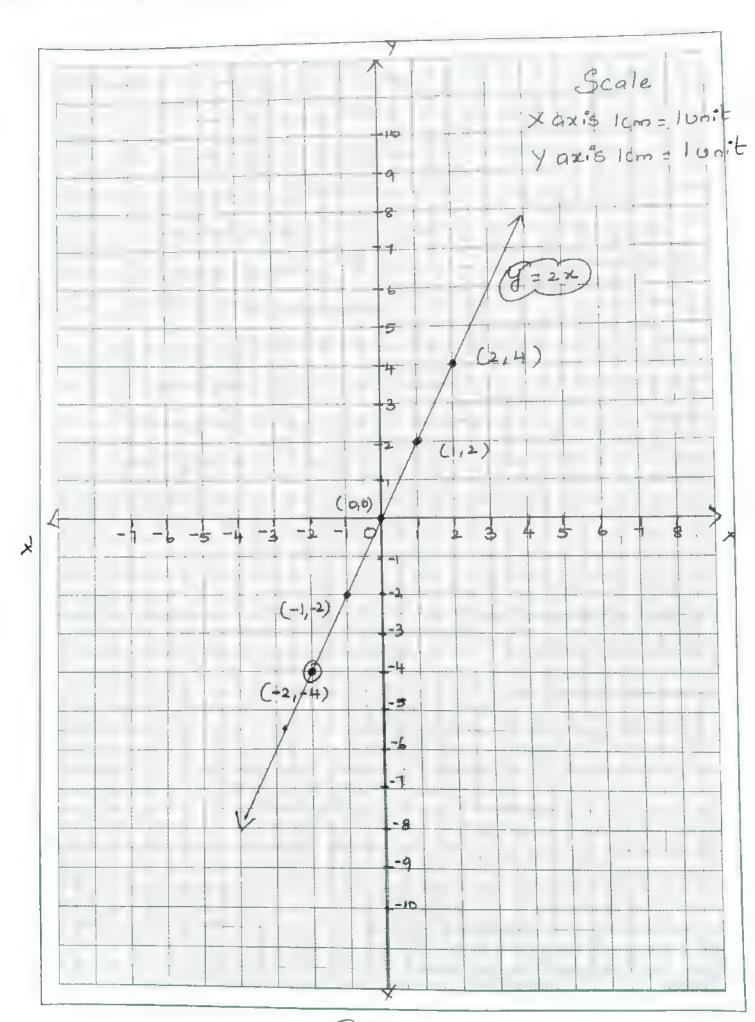
$$x = -1$$
;  $y = 2(-1) = -2$ 

$$\chi = 0; y = 2(0) = 0$$

$$\chi = 1$$
;  $y = 2(1) = 2$ 

$$x = 2$$
;  $y = 2(2) = 4$ 

×	-2	-1	0		2
Y	-4	-2	0	2	4



(iii) 
$$y = (\frac{3}{2})x + 3$$

$$Sol:- y = (\frac{3}{2})x + 3$$

$$x = -4$$
;  $y = (\frac{3}{2})(-4) + 3$ 

$$= -6 + 3$$

$$9 = -3$$

$$\chi = -2$$
;  $y = (\frac{3}{3})(-x) + 3$ 

$$= 3(-1) + 3$$

$$x = 0$$
 ;  $y = \frac{3}{2}(0) + 3$ 

$$= 0 + 3$$

$$9 = 3$$

$$\chi = 2$$
;  $y = \frac{3}{2}(z) + 3$ 

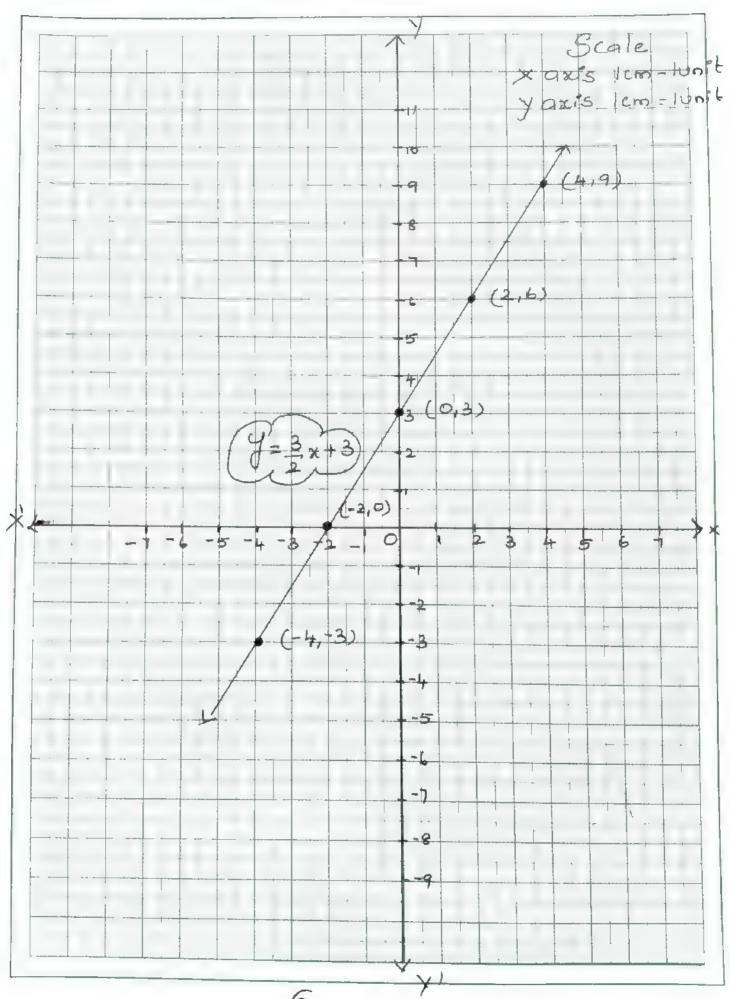
$$x = +4 ; y = \frac{3}{2}(x^{2}) + 3$$

$$= 3(2) + 3$$

$$= 6 + 3$$

$$= 9$$

X	-4	- 2.	0	2,	4
y	-3	O	3	6	9



(ii) 
$$y = 4x-1$$
  
Sol  $y = 4x-1$   
 $x = -1$ ;  $y = 4(-1)-1$   
 $= -4-1$   
 $y = -5$   
 $x = 0$ ;  $y = 4(0)-1$   
 $= 0-1$   
 $y = -1$   
 $y = 4(1)-1$   
 $y = 3$ 

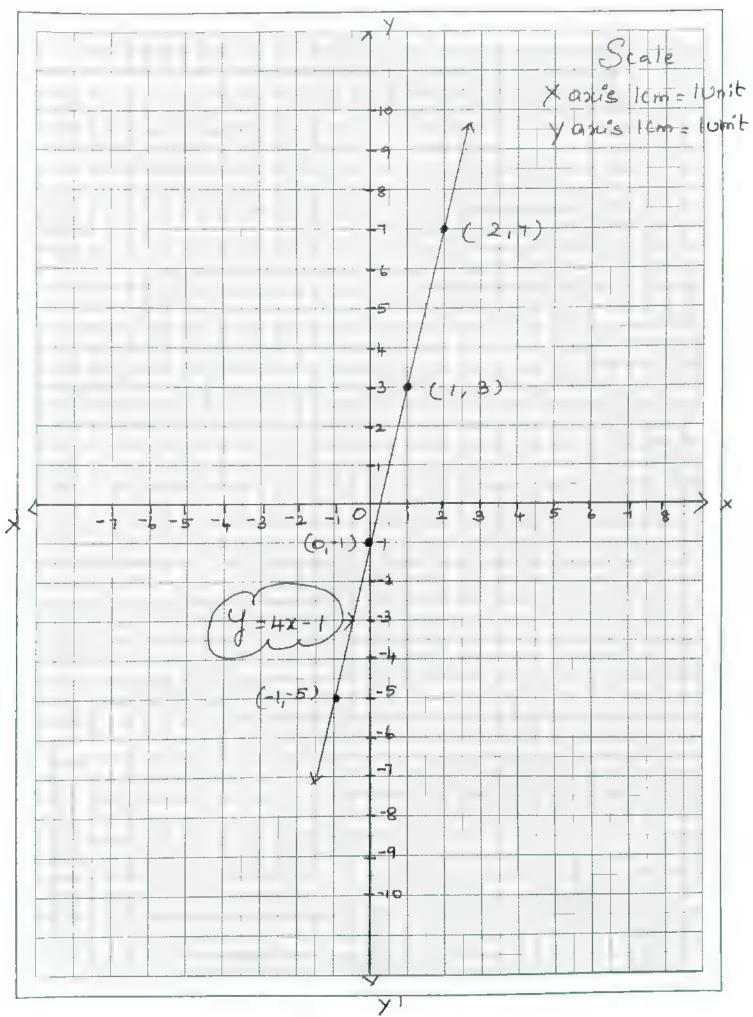
$$\chi = 1$$

$$y = 4(1)^{-1}$$

$$= 4 - 1$$

$$y = 3$$

$$\chi = 2$$
;  $y = 4(2) - 1$   
= 8 - 1  
 $y = 7$ 



(iv) 
$$3x + 2y = 14$$
  
Sol: -  $3x + 2y = 14$   
 $2y = 14 - 3x$   
 $y = \frac{14 - 3x}{2}$ 

$$\chi = -2$$
;  $y = \frac{14 - 3(-2)}{2}$ 

$$\chi = 0$$
;  $y = \frac{14 - 3(0)}{2}$ 

$$\chi = 2$$
;  $y = 14 - 3(2)$ 

$$=\frac{14-6}{2}=\frac{8}{2}$$

$$x = 4$$
;  $y = \frac{14 - 3(4)}{2}$ 

$$= \frac{14 - 12}{2}$$

$$= \frac{2}{2}$$

$$y = 1$$

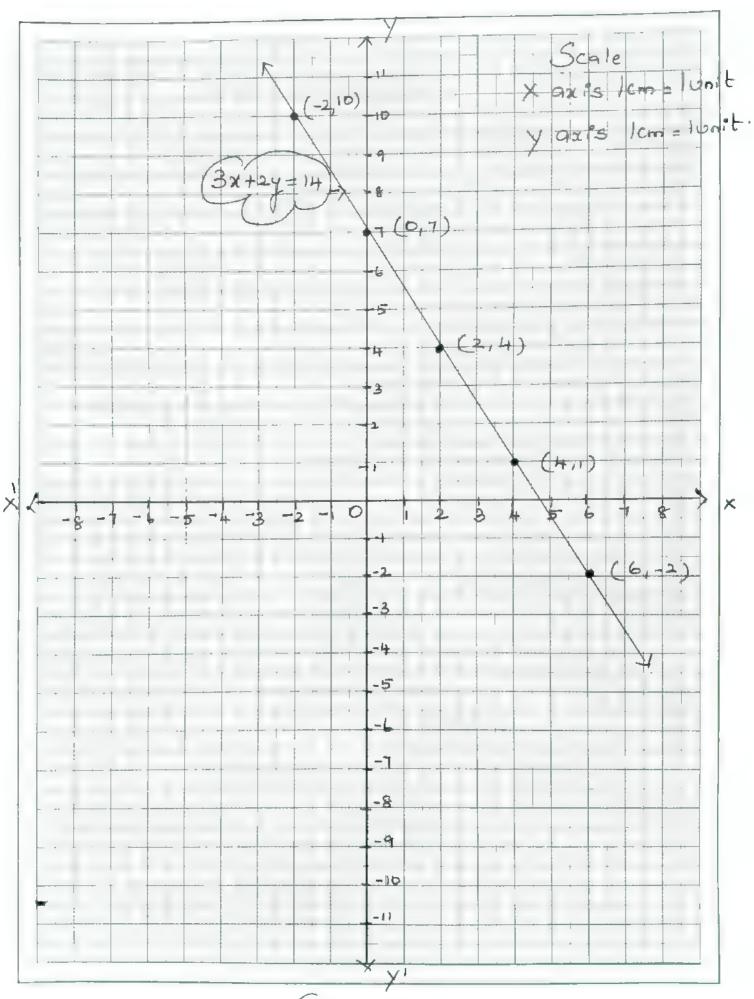
$$\chi = 6$$
,  $y = \frac{14 - 3(6)}{2}$ 

$$= \frac{14 - 18}{2}$$

$$= -\frac{4}{2}$$

$$y = -2$$

×	-2.	0	2	4	6
У	10	7	4	1	-2



96)

(2) Solve graphically

(i) 
$$x+y=7$$
;  $x-y=3$ 

Sol:  $x+y=7 \rightarrow 0 \Rightarrow y=7-x$ 
 $x-y=3 \rightarrow 2 \Rightarrow x-3=y$ 

From (1)

 $y=x-3$ 

				ı.	
χ	-2	-1	0	<b>)</b> '1	2.
7	7	٦	٦	7	7
-χ	2.	1	0	- 1	-2
9	9	8	٦	6	5

Plot: (-2,9) (-1,8) (0,7) (1,6) (2,5)

~	_
From (2)	

χ	-2,	-1	0	1	2_
-3	-3	-3	-3	-3	-3
y	-5	-4	-3	-2.	<b>~</b> I

Plot: (-2,-5) (-1,-4) (0,-3) (1,-2) (2,-1)

: Point of intersection = {5,2}

Scale Xazis Icm = (-1,8) (0,7) (-1,-4) -1 -8 (98)

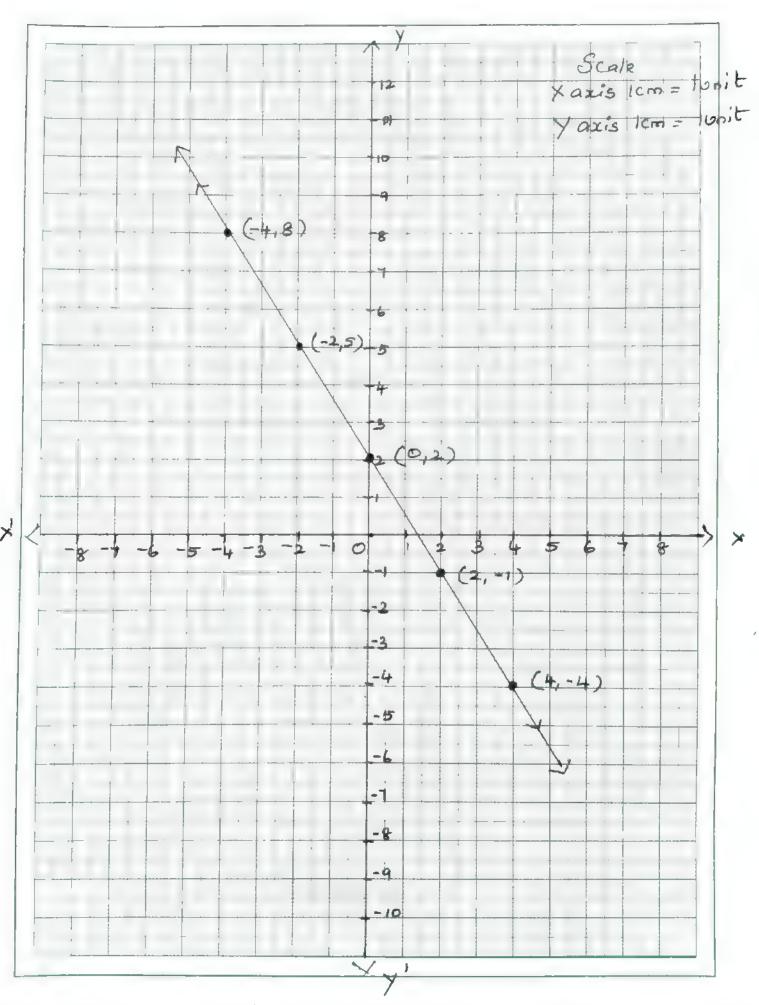
(i) 
$$3\pi + 2y = 4$$
;  $9x + 6y - 12 = 0$   
Sol:  $-3x + 2y = 4 \longrightarrow 0$   
 $9x + 6y = 12 \xrightarrow{2} -6y = 3$   
 $3x + 2y = 4 \longrightarrow 2$   
 $3x + 2y = 4$   
 $2y = 4 - 3x$   
 $y = 4 - 3x$ 

			<del></del> +		
α	-4	-2	0	2.	4
4	4	4	4	4	4
-32	12.	6	0	-6	-12
4-3x	16	10	4	- 2	-8
y= 4-3x 2	16 = 8	10 = 5	4 = 2	-2, 2-1	-8 -4

(99

Plot: (-4,8) (-2,5) (0,2) (2,-1) (4,-4)From (2) 3x + 2y = 4i. eqn (1) = eqn (2)

It has infinite number of Solution



$$\frac{50!}{2^{x+2}} + \frac{y^{x}}{4} = 1$$

$$\frac{2^{x+4}}{4} + \frac{y^{x}}{4} = 1$$

$$2^{x+4} + \frac{y^{x}}{4} = 1$$

$$2^{x+4} + \frac{y^{x}}{4} = 1$$

$$2^{x+4} + \frac{y^{x}}{4} = 1$$

$$\frac{\chi^{+2}}{2} + \frac{y^{+}}{4} = 2$$

$$\frac{2\chi + y}{4} = 2$$

$$4 \longrightarrow 2$$

$$2\chi + y = 8$$

$$2\chi + y = 8$$

From (1)

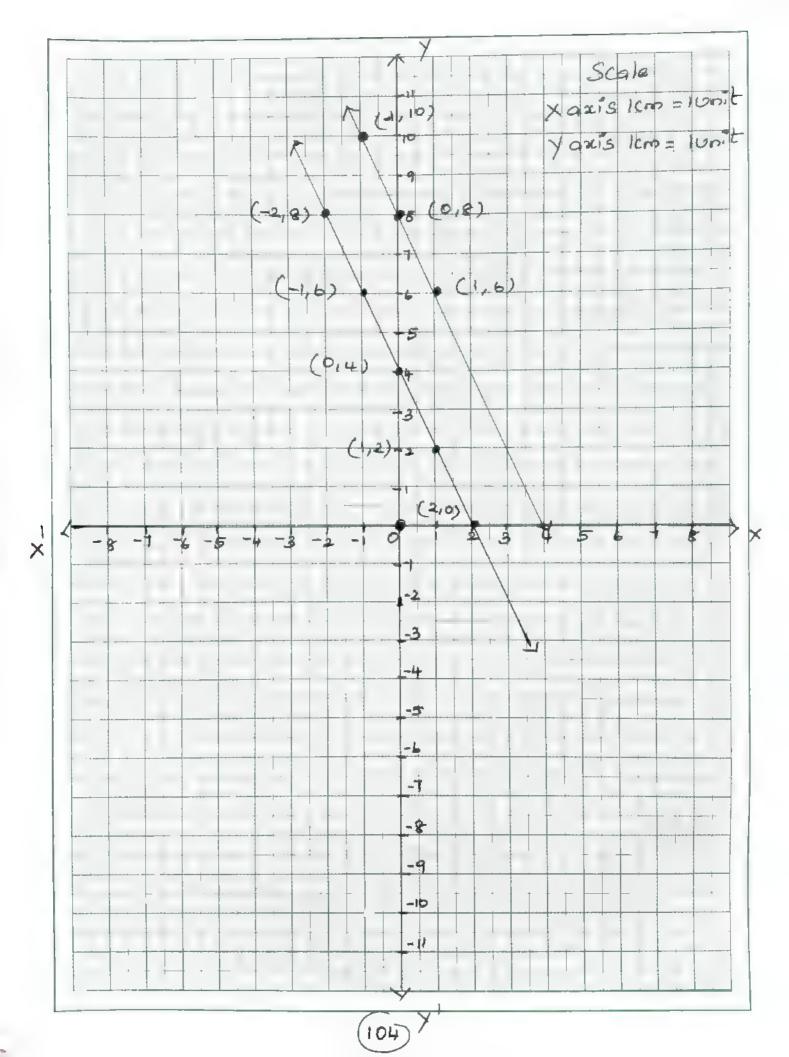
$$2x + y = 4$$
  
 $y = 4 - 2x$ 

χ	-2	-1	0		2
4	4	4	4	4	4
-2x	4	2.	0	- 2	-4
y	8	6	4	2	0

Plot: (-2,8)(-1,6), (0,4) (1,2) (2,0)

From (2)
$$2x+y=8$$
 $y=8-2x$ 

χ	-1	0	
8.	. 8	8	8
-2.	+2.	0	-2
y	+10	8	6



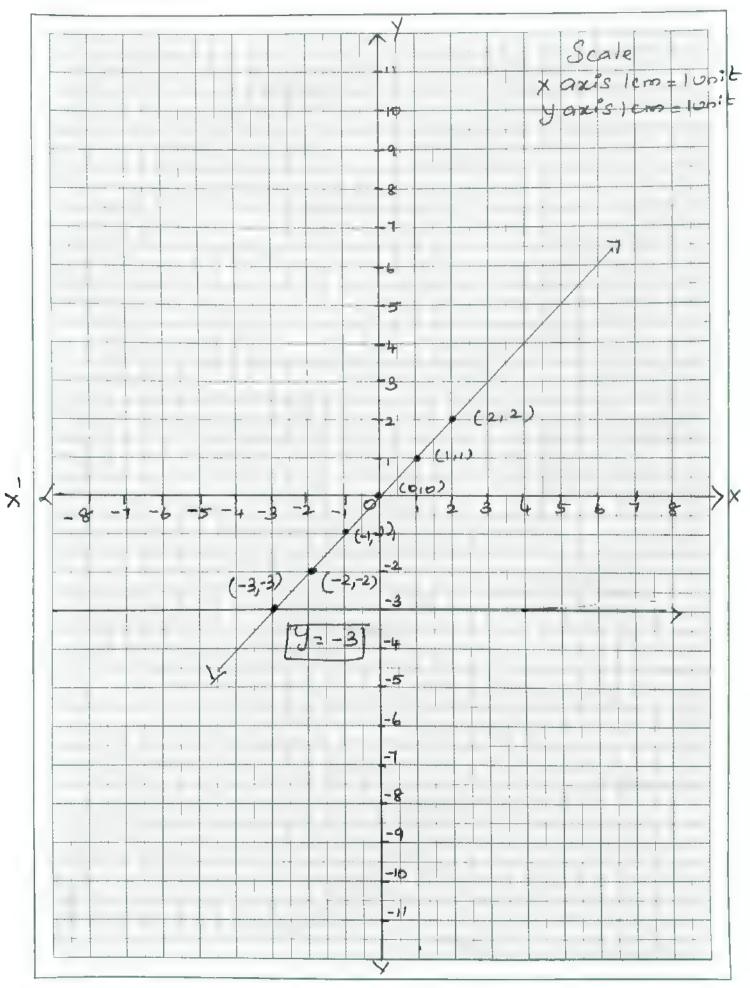
(i°v) 
$$x-y=0$$
;  $y+3=0$   
Sol:-  $x-y=0 \rightarrow 0$   
 $y+3=0 \rightarrow 2$   
 $x-y=0$   
 $x=y=0$   
Plot:-  $(-2,-2), (-1,-1), (0,0), (1,0)$ 

Plot: - (-2,-2), (-1,-1), (0,0), (1,1), (2,2)

$$y + 3 = 0$$

$$y = -3$$

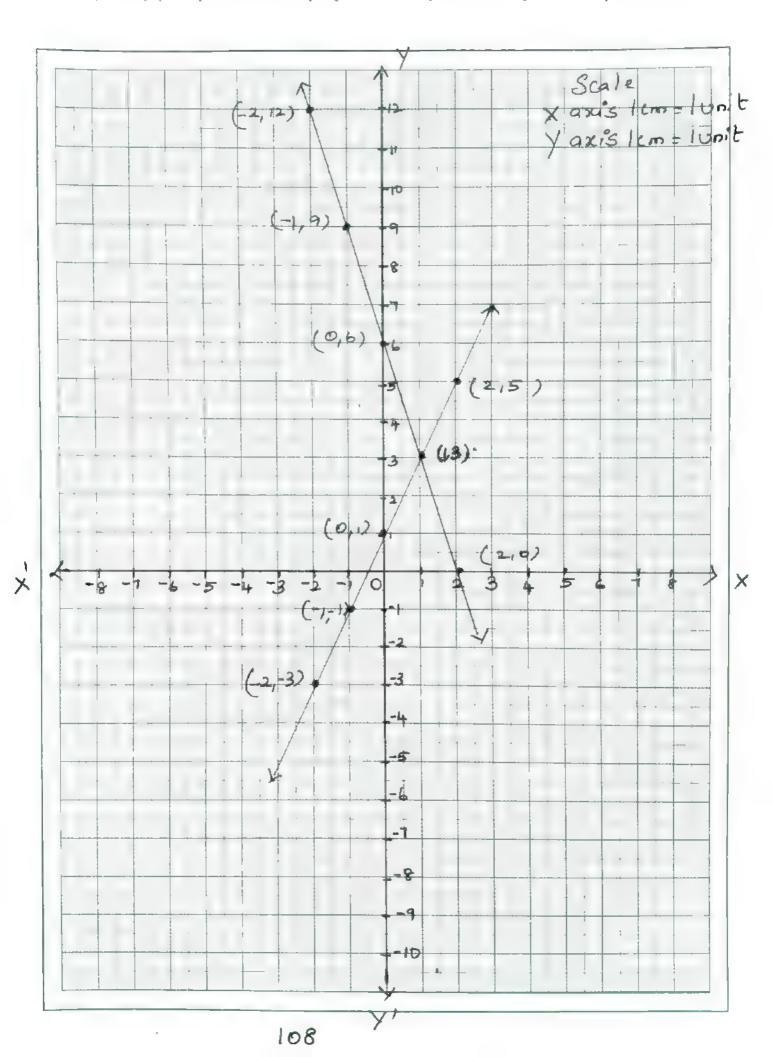
Solution = {-3,-3}



(166) × 1

(v) 
$$y = 2x + 1$$
;  $y + 3x - 6 = 0$   
 $50! = y = 2x + 1 \rightarrow 0$   
 $y + 3x - 6 = 0$   
 $y = -3x + 6 \rightarrow 2$   
 $2x - 4 - 2 \quad 0 \quad 2 \quad 4$   
 $1 \quad 1 \quad 1 \quad 1 \quad 1$   
 $y - 3 \quad -1 \quad 1 \quad 3 \quad 5$   
Plot:  $(-2, -3), (-1, -1), (0, 1), (1, 3), (2, 5)$   
 $x - 2 \quad -1 \quad 0 \quad 1 \quad 2$   
 $x - 2 \quad -1 \quad 0 \quad 1 \quad 2$   
 $x - 2 \quad -1 \quad 0 \quad 1 \quad 2$   
 $x - 3x \quad 6 \quad 3 \quad 0 \quad -3 \quad -6$   
 $x - 2 \quad -1 \quad 0 \quad 6 \quad 6$   
 $x - 2 \quad -1 \quad 0 \quad 6$   
 $x - 2 \quad -1 \quad 0 \quad 1 \quad 2$   
 $x - 3x \quad 6 \quad 3 \quad 0 \quad -3 \quad -6$   
 $x - 3x \quad 6 \quad 6 \quad 6 \quad 6$   
 $x - 3x \quad 6 \quad 6 \quad 6 \quad 6$   
 $x - 3x \quad 6 \quad 6 \quad 6 \quad 6$ 

(07)



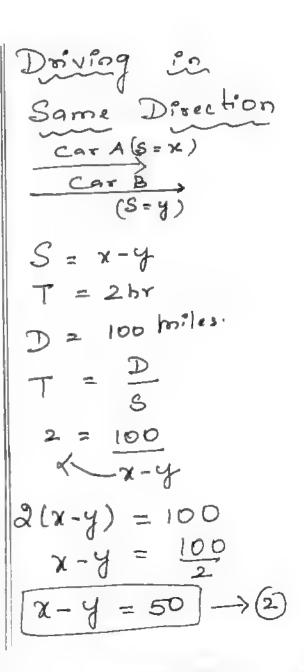
(Vi) 
$$\chi = -3$$
;  $y = 3$   
 $Sol = 3 \rightarrow 1$   
 $Y = 3 \rightarrow 2$   
Solution =  $\{-3, 3\}$ 

Scale X axis Icm = Ivnit axis Icm = I unit (-3,3) × × -5 -1 -8 -10 -[] (110)

(3) Two Cars are 100 miles apart. If they drive to lhr. If they drive towards each other they will meet in Ihr. If they drive in the Same direction they will meet in 2 hrs. Find their Speed by using graphical method.

Sol: -

x+y=100 ->





$$x + y = 100 - x$$

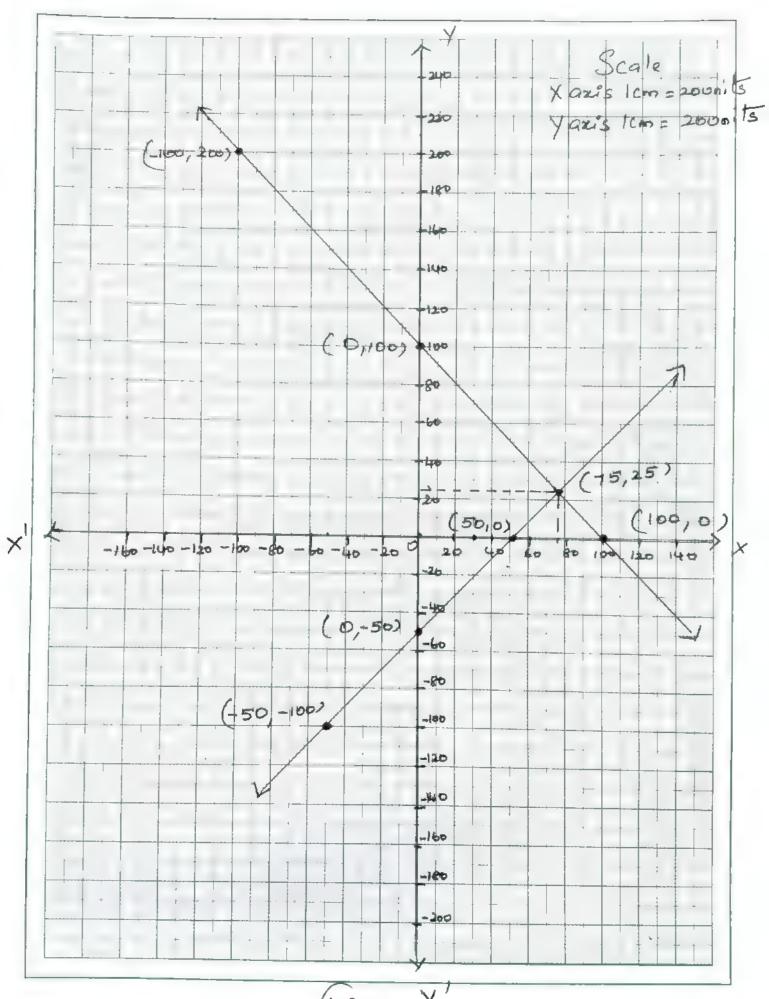
χ	-100	0	100
100	100	100	100
-2	100	0	-100
y	200	100	0

Plot! - (-100, 200), (0,100) (100,0)

7-50 = 4 = x-50

5		0		-
Ĭ ——	χ	-50	0	50
	- 5b	-50	- 50	-50
	У	-100	-50	0

Plot = (-50,-100), (0,-50), (50,0) Solution = {75,25}



(113)

Y

(1) Solve, Using the method of Substitution.

(i) 
$$2x - 3y = 7$$
;  $5x + y = 9$ 

$$2x - 3(9 - 5x) = 7$$

$$2x - 27 + 15x = 7$$

$$\chi = \frac{34}{13}$$

Put 
$$x=2$$
 in (3)  
 $y = 9-5(2)$   
 $y = 9-10$   
 $y = -1$ 

$$\begin{array}{c} -1 \\ \end{array}$$

(ii) 
$$1.5x + 0.1y = 6.2$$
,  $3x - 0.4y = 11.2$   
Sol:  $1.5x + 0.1y = 6.2 \rightarrow ① \times ^{1/2} by 10$   
 $3x + 0.4y = 11.2 \rightarrow ② \times ^{1/2} by 10$ 

$$= \rangle 15 \times + 9 = 62 \rightarrow 6$$

$$15x + y = 62$$
 $y = 62 - 15x \rightarrow 3$ 

(115)

$$30x-4(62-15x) = 112$$

$$30x-248+60x = 112$$

$$90x = 112+248$$

$$90x = 360$$

$$x = 360$$

$$x = 4$$

$$-62-15x$$

$$= 62-15(4)$$

$$= 62-60$$

$$y = 2$$

$$x = 4$$

$$y = 2$$

$$|0\% of x + 20\% of y = 24$$

$$\Rightarrow \frac{10}{100}x + \frac{20}{100}y = 24$$

$$\frac{x}{10} + \frac{24}{10} = 24$$

$$\frac{\chi + 2y}{10} = 24$$

$$x + 2y = 240 \longrightarrow \bigcirc$$

$$3x-y=20 \rightarrow 2$$

$$x + 2y = 240$$

$$\chi = 240 - 2y \rightarrow 3$$

$$3(240-24)-4=20$$

$$720 - 6y - y = 20$$

$$720 - 7y = 20$$

$$720 - 20 = 74$$

$$700 = 7y$$

$$7y = 700$$

$$y = \frac{700}{7}$$

$$y = 100$$

$$x = 240 - 2(100)$$

$$= 240 - 200$$

$$x = 40$$

$$y = 100$$

$$y = 100$$

$$x = 40$$

$$y = 100$$

$$y = 100$$

$$x = 40$$

$$y = 100$$

$$y = 100$$

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$$y = 100$$

$$x = 40$$

$$y = 100$$

$$y = 100$$

$$x = 40$$

$$y = 100$$

$$y =$$

(118)

$$\sqrt{3} \times = \sqrt{8} \cdot 4$$

$$\chi = \sqrt{8} \cdot 4$$

$$\chi = 2\sqrt{2} \cdot 4$$

$$\sqrt{3}$$

$$\sqrt{2} = 2\sqrt{2} \cdot 4$$

$$\sqrt{3} = 2\sqrt{2} \cdot 4$$

$$\sqrt{4} = 2\sqrt{2} \cdot 4$$

$$\sqrt{4} = 2\sqrt{2} \cdot 4$$

$$\sqrt{4} = 2\sqrt{$$

2) Raman's age is three times the Sum of the ages of his two Sons.

After 5 years his age will be twice the Sum of the ages of his two Sons.

Find the age of Raman.

Sol!-Let Raman's age = x Sum of age of b= y his two sons

=> Raman's age = 3 Times Sum of age of his two sons.

$$= \Rightarrow \boxed{x - 3y = 0}$$

$$\Rightarrow \boxed{1}$$
After 5 years

=) Raman's age = Tworce the Sum of ages
of his two Sons.

$$x+5 = 2(y+10)$$

$$x+5 = 2y+20$$

$$x-2y = 20-5$$

$$x-2y=15 \longrightarrow 2$$

$$x-3y=0$$

$$x=3y \longrightarrow 3$$

$$x-2y=15$$

$$y=15$$

$$y=15$$

$$y=15$$

$$y=15$$

$$y=15$$

$$y=15$$

$$y=3(15)$$

$$\chi = 3(15)$$

$$\chi = 45$$

- Age of Raman = 45 yrs.

3) The middle digit of a number between 100 and 1000 is Zero and the Sum of the Other digit is 13. It the digits are reversed, the number so tormed exceeds the Original number by 495. Find the number.

Sol:\_

Let the 3 digit Number = XOY

[Since 'O' is the middle Number]

=> Sum of other 2 digit is 13 ie, x+y = 13 -> (

=> Original Number = 100x + y

Reversed digit = 100y + x

Reversed digit = Original No + 495 100y + x = 100x + y + 495100y + x - 100x - y = 495

$$y - \chi = 5$$

$$y = 5 + \chi \longrightarrow (2)$$

$$\chi + 5 + \chi = 13$$

$$\chi = \frac{8}{2}$$

$$\chi = 4$$

1. Solve by the method of Elimination

$$2x-y/=3$$

$$x = \frac{10}{5}$$

$$2(1)-y=3$$
 $2-y=3$ 

$$\chi = 2$$
 $\gamma = -1$ 

(24)

(ii) 
$$x-y=5$$
;  $3x+2y=25$ 

Sol: 
$$x-y=5 \rightarrow 0$$
  $x^{1}y^{2}$   $y^{2}$   $y^$ 

$$3x + 2y = 25 \rightarrow \textcircled{3}$$

$$= > 2x - 2y = 10$$

$$3x + 2y = 25$$

$$x = \frac{35}{5}$$

$$x - y = 5$$

$$\begin{array}{c} x = 7 \\ y = 2 \end{array}$$

(iii) 
$$\frac{x}{10} + \frac{4}{5} = 4$$
;  $\frac{x}{8} + \frac{4}{6} = 15$ 

$$\frac{Sol}{10}$$
:-  $\frac{x}{10} + \frac{4x^2}{5} = 14$ 

$$\frac{\chi + 2y}{10} = 14$$

$$\frac{\chi^{3}}{8x^{3}} + \frac{y^{3}}{6x^{4}} = 15$$

$$\frac{3x+44}{24} = 15$$

$$3x + 4y = 360$$

Solve (1) 4 (2)  

$$\chi + 2y = 140 \longrightarrow x^{1/4} \text{ by } 2$$

$$3\chi + 4y = 360$$

$$= > 2x + 4y = 280$$

$$(-)3x + 4y = 360$$

$$- + x = + 80$$

(26)

$$80 + 2y = 140$$

$$2y = 140 - 80$$

$$2y = 60$$

$$y = \frac{60}{2}$$

$$y = 30$$

$$y = 30$$

$$y = 30$$

$$4y = 7xy; 3(x+3y) = 1$$

$$2x+y = 7xy = 6x + 3y = 7$$

(PV) 
$$3(2x+y) = 7xy$$
;  $3(x+3y) = 11xy$   
 $\frac{Sol}{3}$ :  $3(2x+y) = 7xy = 36x + 3y = 7xy - 3000$   
 $3(x+3y) = 11xy = 3x + 9y = 11xy - 3000$   
 $Solve (1) 4 (2)$ 

$$6x + 3y = 7xy$$

$$3x + 9y = 11xy \longrightarrow x^{1y} by^{2}$$

$$= \begin{cases} 6x + 3y = 7xy \\ 6x + 18y = 2xy \\ (-) & (-) \end{cases}$$

$$75 = 75 \times 3$$

$$15 = 15 \times 3$$

$$17 = 17 \times 3$$

$$\frac{Sol}{x} = \frac{1}{x} + 5y = 7 \rightarrow 0$$

$$\frac{3}{x} + 4y = 5 \rightarrow 2$$

$$\Rightarrow 4z + 5y = 7 \rightarrow 3x^{1/3} \text{ by } 3$$

$$3z + 4y = 5 \rightarrow 4x^{1/3} \text{ by } 4$$

$$\Rightarrow 12z + 15y = 21$$

$$-y = 1$$

$$y = -1$$

$$y = -1$$

$$\frac{1}{x} + 5(-1) = 7$$

$$\frac{1}{x} - 5 = 7$$

$$\frac{1}{x} = 7 + 5$$

$$\frac{1}{x} = 7 + 5$$

$$\frac{1}{x} = 7 + 5$$

$$\frac{1}{x} = 2x$$

$$\frac{1}{x^{1/3}} = x$$

$$\frac{1}{x^{1/3}} = x$$

$$\frac{1}{x^{1/3}} = x$$

(vi) 
$$18x + 11y = 70$$
;  $11x + 13y = 74$   
 $\frac{Sol}{1}$ ;  $-13x + 11y = 70$   $\rightarrow \textcircled{5}$   
 $13x + 11y = 70$   
 $+11x + 13y = 74$   
 $\frac{34x + 34y = 1144}{24x + 34y = 144}$   
 $\Rightarrow x + y = 6$   
 $\Rightarrow x + y = 6$   
 $\Rightarrow x + y = 6$   
 $\Rightarrow x - y = -2$   
 $\Rightarrow x = 4$   
 $\Rightarrow x = 4$   
 $\Rightarrow x = 4$   
 $\Rightarrow x = 4$   
 $\Rightarrow x = 2$ 

130)

Put 
$$x = 2$$
 in (3)  

$$2 + y = 6$$

$$y = 6 - 2$$

$$y = 4$$

$$x = 2$$

$$\chi = 2$$
 $y = 4$ 

(2) The monthly income of A and B are in the ratio 3:4 and their monthly expenditure are in the 5:7. If each Saves 7 5,000 per month, Hend the monthly for come of each.

Sol

PERSON	Income (x)	EXPENDITURE	SAVINGS
A	3	5	5000
В	4	7	5000

$$3x - 5y = 5000 \rightarrow 6 \times 19 by 4$$
  
 $4x - 7y = 5000 \rightarrow 6 \times 19 by 3$ 

$$= ) |2x - 20y = 20000$$

$$|2x - 2|y = |5000$$

$$(-) (+) (-)$$

$$y = 5000$$

$$\chi = \frac{10000}{30000}$$

3) Free years ago, a man was Seven times as old as his son, while free years hence, the man will be four times as old as his son. Find their present age.

801:

1. + age of man = x

Man = 4 threes the Son x+5 = 4(y+5)x+5 = 4y+20

(134)

(1) Solve by cross multiplecation method:

(i) 
$$8x-3y=12$$
;  $5x=2y+7$ 

$$\frac{S0!}{5x-2y-1} = 0$$

$$\frac{\chi}{21-24} = \frac{y}{-60-(-56)} = \frac{1}{-16-(-15)}$$

$$\frac{x}{-3} = \frac{y}{-60+56} = \frac{1}{-16+15}$$

$$\frac{\chi}{-3} = \frac{4}{-4} = \frac{1}{-1}$$

$$\frac{\chi}{-3} = -1$$

$$\frac{y}{-4} = -1$$

$$\frac{SQ}{5x + 2y - 13 = 0}$$

$$\frac{7}{-91-(-22)} = \frac{4}{-55-(-18)} = \frac{1}{12-35}$$

$$\frac{-\chi}{-91+22} = \frac{9}{-55+78} = \frac{1}{-23}$$

$$\frac{\chi}{-69} = \frac{y}{23} = \frac{1}{-23}$$

$$\frac{3L}{-69} = \frac{1}{23} = \frac{1}{23}$$

$$\chi = -\frac{69}{-23} \qquad \qquad y = \frac{23}{-23}$$

$$\chi = 3$$
 
$$\gamma = -1$$

(iii) 
$$\frac{2}{2} + \frac{3}{9} = 5$$
;  $\frac{3}{2} - \frac{1}{9} + 9 = 0$   
Sol Let  $\frac{1}{2} = 9$ ,  $\frac{1}{9} = 6$   
=>  $\frac{2a + 3b - 5 = 0}{3a - b + 9 = 0}$ 

$$\frac{a}{27-5} = \frac{b}{-15-18} = \frac{1}{-2-9}$$

$$\frac{a}{22} = \frac{b}{-33} = \frac{1}{-11}$$

$$\frac{a}{22} = \frac{1}{11}$$

$$a = \frac{22}{-11}$$

$$a = -2$$

$$\frac{1}{x} = \frac{-2}{x}$$

$$b = -\frac{33}{-11}$$

(37)

2) Akishaya has 2 ruper coins and 5 ruper coins in her purse. It in all She has 80 coins totalling 7220, how many coins of each kind does She have:

Sol:-Let 2 rupee = x 5 rupee = y

Total Coins = 80

$$x + y = 80$$

$$x + y - 80 = 0 \longrightarrow \bigcirc$$

Total amount = 220

$$2x + 5y = 220$$



5 (-) = 220 (-) 2 (-) 5

$$\frac{\chi}{-220 - (-400)} = \frac{4}{-160 - (-220)} = \frac{1}{5 - 2}$$

$$\frac{\chi}{-220 + 400} = \frac{y}{-160 + 220} = \frac{1}{3}$$

$$\frac{\chi}{180} = \frac{9}{60} = \frac{1}{3}$$

$$\frac{\chi}{180} = \frac{1}{3}$$

$$\frac{4}{60} = \frac{1}{3}$$

$$x = 180$$
  $y = 60$ 

$$\chi = 60$$
 
$$y = 20$$

3) It takes 24 hours to fill a Swimming pool Using two Pipes. If the pipe of larger diameter is used for 8 hours and the pipe of the Smaller diameter is used for 18

hours. Only half of the pool is filled. How long would each pipe take to fill the Swimming pool.

Sol:

Let Time taken by larger pipe = x

For Ihr = \frac{1}{\times }

Time taken by Smaller pipe = y

For Ihr = \frac{1}{\times }

$$\Rightarrow \frac{1}{x} + \frac{1}{y} = \frac{1}{24} \Rightarrow \bigcirc$$

Larger pipe takes 8hrs = Fills half Smaller pipe takes 18hrs the pool

$$\Rightarrow \frac{8}{x} + \frac{18}{y} = \frac{1}{2} \Rightarrow 2$$

$$24(a+b) = 1$$
  
 $24a+24b-1=0 \longrightarrow 3$ 

(2) => 
$$8a + 18b = \frac{1}{2}$$
  
 $2(8a + 18b) = 1$   
 $16a + 36b - 1 = 0 \longrightarrow 4$   
Solve (3) 4 (4)

$$\frac{a}{12} = \frac{b}{8} = \frac{1}{480}$$

$$\frac{a}{12} = \frac{1}{480}$$

$$a = \frac{1}{480}$$

$$a = \frac{1}{40}$$

$$40 = 2$$

$$x = 40$$

· Larger pipe takes 40 hrs. Smaller pipe takes 60 hrs.



The Sum of a two digit number and the number formed by Poterchanging the digits is 110. It 10 is Subtracted from the first number the new number is 4 more than 5 times the Sums of the digits of the first number. Find the first number. Dumber.

Sol:-Let Two digit Number = x, y Original Number = 10x+y

After interchanging the digits
New Number = 10y+x

=> [Sum of 2 digit No] + [No a) ter interchanging digit] = 110

ie, lox+y+loy+x = 110

(143

$$\frac{\chi}{-54} = \frac{y}{-36} = \frac{1}{-9}$$

$$\frac{x}{-54} = \frac{+1}{-9}$$
 $\frac{y}{-36} = \frac{1}{-9}$ 

$$\chi = -\frac{54}{-9} \qquad \qquad y = -\frac{36}{-9}$$

$$\left[ \chi = 6 \right]$$

2) The Sum of the numerator and denominator of a fraction is 12. It the denominator is increased by 3, the fraction becomes \fraction. Find the fraction.

Sol: Let the numerator = x Denominator = y (145)

Sum of Numerator & Denominator = 12

1è, 
$$x+y=12$$
  $\longrightarrow$  (D

1è,  $x+y=12$   $\longrightarrow$  (D

2)

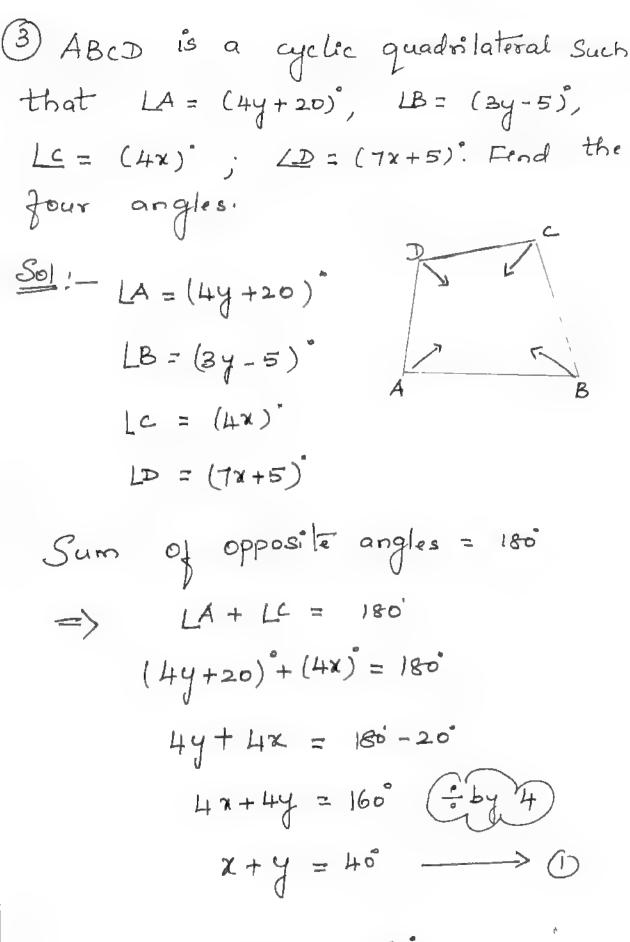
Denominator in creased  $\int_{-1}^{2}$  Fraction is  $\frac{1}{2}$ 

by 3

1è,  $\frac{x}{y+3}$   $= \frac{1}{2}$ 
 $2x = y+3$ 
 $2x-y=3$ 
 $2x-y=3$ 
 $3x = 15$ 
 $x = \frac{15}{3}$ 
 $x = \frac{15}{3}$ 
 $x = 5$ 

Out  $x = 5$  in (D)

 $x = \frac{15}{3}$ 
 $x = 5$ 
 $x = \frac{15}{3}$ 
 $x = \frac{15}{3}$ 



 $= 3y - 5 + 7x + 5 = 180^{\circ}$ 

$$7x + 3y = 180^{\circ} \implies (2)$$

$$7x + 3y = 180^{\circ}$$

$$7x + 3y = 180^{\circ}$$

$$7x + 8y = 180^{\circ}$$

$$7x + 8y = 180^{\circ}$$

$$15 + y = 40$$

$$168$$

$$LA = 4y + 20 = 4(25) + 20 = 100 + 20 = 120$$

$$LB = 3y - 5 = 3(25) - 5 = 75 - 5 = 70^{\circ}$$

$$LC = 4x = 4(15) = 60^{\circ}$$

$$LD = 7x + 5 = 7(15) + 5 = 105 + 5 = 110^{\circ}$$

$$LA = 120^{\circ}$$

$$LC = 60^{\circ}$$

$$LD = 110^{\circ}$$

(4) On Selling a Tivat 5% gain and a fridge at 10%. gain a Shopkeeper gains 7 2000. But it he Sells the T. V at 10% gain and the fridge at 5% loss, he gains Rs 1500 on the transaction. Find the actual price of the T.V and the fridge. Sol! - Let Price of T.V = x

Price of Fridge = 4

5% gain for T.V + 10% gain for Findge = Gains   

$$\frac{5}{100}$$
 X +  $\frac{10}{100}$  y = 2000  
 $\frac{5}{100}$  X +  $\frac{10}{100}$  y = 2000  
 $\frac{5}{100}$  X +  $\frac{10}{100}$  y = 20000  
 $\frac{5}{100}$  X +  $\frac{2}{100}$  =  $\frac{10}{100}$  %  $\frac{10}{100}$  Y =  $\frac{1500}{100}$   $\frac{10}{100}$  Y =  $\frac{15000}{100}$   $\frac{10}{100}$   $\frac{1}{100}$  Y =  $\frac{1}{100}$   $\frac{1$ 

$$2x - y = 40000$$

$$2x - y = 30000$$

$$4x - 2y = 60000$$

$$x = 100000$$

$$x = 20000$$

$$x = 20000$$

$$2y = 40000$$

$$2y = 40000$$

$$2y = 40000$$

$$2y = 40000$$

$$2y = 20000$$

$$y = 20000$$

Price of Fridge = \$ 20000

Price of Fridge = \$ 10000

(5) Two numbers are in the ratio 5:6. If 8 is Subtracted from each of the numbers, the rateo becomes 4:5. Find the numbers. Let the 2 numbers = x and y. => Two numbers are in ratio = 5:6 12, × = 5 6x = 5y6x-5y=0 -> () => 8 Subtracted from 4 = ratio 4:5 each Number 1e, 7-8 = 4 7-8 > 5 5(x-8) = 4(y-8)5x - 40 = 4y - 325x - 4y - 40 + 32 = 05x -4y - 8 = 0 -> 2

$$\frac{\chi}{-4} = \frac{y}{-24 - (-25)}$$

$$\frac{\chi}{40} = \frac{y}{-48} = \frac{1}{-24 + 25}$$

$$\frac{\chi}{40} = \frac{y}{48} = \frac{1}{1}$$

$$\frac{\chi}{40} = \frac{1}{48} = \frac{1}{1}$$

- Two Numbers are 40 4 48

6 4 Indians and 4 Chinese Can do a piece of Work in 3days. while 2 Indians and 5 Chinese Can finish it in 4days. How long would it take for 1 Indian to do it? How long would it take it take for 1 Chinese to do it?

$$3(4x + 4y) = xy$$

$$12x + 12y = xy \longrightarrow 0$$

Work done by 2 Indians = 4 days.

154

$$\Rightarrow \frac{2^{x}}{x} + \frac{5}{y} = \frac{1}{4}$$

$$\frac{2y + 5x}{xy} = \frac{1}{4}$$

$$4(5x+2y)=xy$$

$$12x + 12y = xy \rightarrow x^{1/8}$$
  
 $20x + 8y = xy \rightarrow x^{1/8}$ 

$$=$$
  $96x + 96y = 8xy$ 

(55)

$$y = \frac{144}{4}$$

$$y = 36$$

$$y = 36 \text{ in } 0$$

$$y = 3$$

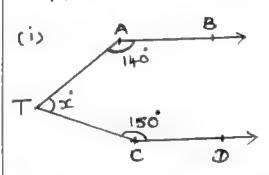
.. Nork done by | Indian = 18 days Nork done by | Chinese = 36 days.

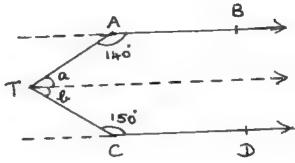
## CHAPTER-4

## GEOMETRY

## EXERCISE 4.1

1) In the figure, AB is parallel to CD, find x.





:. a+140 = 180 [co-Interior angles are Supplementary

$$a = 40$$

Similarly,

&+150=180 [co-Interior angles are (Supplementary)

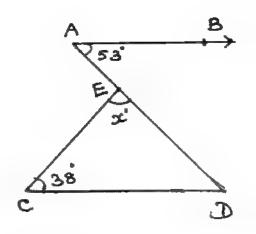
=> x = a+b

$$x = 40 + 30$$

=) 
$$x^{\circ} = a + b$$
  
=  $132 + 156$ 

$$x = 288$$

In 
$$\triangle$$
 EcD,  
 $x + 38 + 53 = 180$   
 $x + 91 = 180$ 



$$x = 180 - 91$$
 $x = 89$ 

2) The angles of a triangle are in the ratio 1:2:3, find the measure of each angle of the triangle.

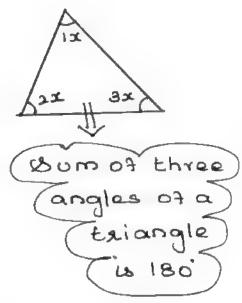
$$(Ratio) => 1:2:3$$
  
 $1x+2x+3x=180$ 

6x=180

$$x = 180^{\circ} 30$$

$$x = 30$$

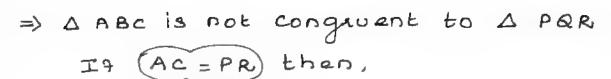
 $1^{\text{st}}$  angle => 1x = 1(30) = 30  $2^{\text{nd}}$  angle => 2x = 2(30) = 60 $3^{\text{rd}}$  angle => 3x = 3(30) = 90



- and say whether each pair is that of congruent triangles. If the triangles are congruent, say how; if they are not congruent say why and also say if a small modification would make them congruent.
- (i) In  $\triangle$  ABC and  $\triangle$  PQR,

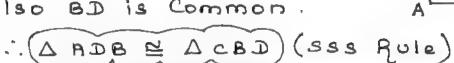
  AB = PQ & (given)

  BC = QR J



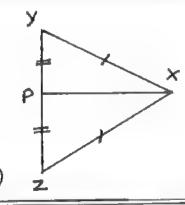
(ii) In A ADB and A CBD,

Also BD is Common.





Also PX is Common



A

(IV) In A OAB and A OCA

[AOB = LCOD (vertically opp. angles)

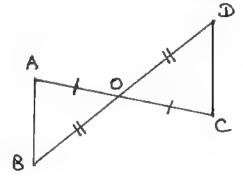




(V) In A OAB and A OCD

[AOB = [COD (vertically opp.

angles)





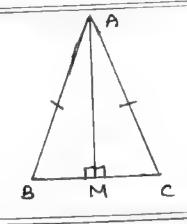
## : (A OAB = AOCD) (SAS Rule)

(Vi) In A ABM and A ACM

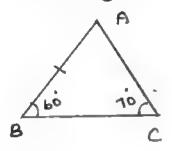
AB = Ac (given) (hypotenuse)

AMB = AMC = 90

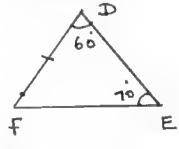
AM is Common



4)  $\triangle$  ABC and  $\triangle$  DEF are two triangles in which  $\triangle$  AB = DF,  $\triangle$  ACB = 70,  $\triangle$  ABC = 60,  $\triangle$  DEF = 70 and  $\triangle$  ABC = 60. Prove that the triangles are Congruent.



In A ABC, [A+60+70=180] [A+130=180] [A=180-130] [A=50]



In A DFE, 60+ LF+70 = 180 LF+130 = 180 LF = 180-130 LF=50

Now, In A ABC and ADFE

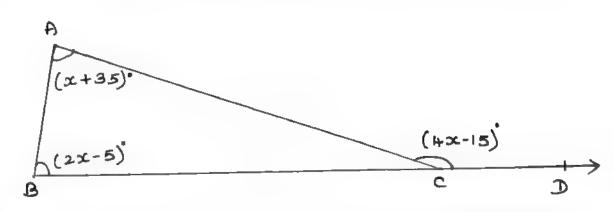
AB = DF (Given)

[ACB = DEF = 70 (Given)

[A = LF = 50

DABC & DDFE (ASA Rule)

5) Find all the three angles of A ABC



Exterior angle = som of two opposite interior angles.

$$4x-15 = x+35+2x-5$$
  
 $4x-15 = 3x+30$   
 $4x-3x = 30+15$   
 $x = 45^{\circ}$ 

=) |A = x + 35 = 45 + 35 = 80 (A = 80)

=) 
$$B = 2x - 5 = 2(A5) - 5 = 90 - 5 = 85$$

=)  $|C = 180 - (4x-15)^{\circ}$ =  $180 - [4(45) - 15^{\circ}]$ =  $180 - [180 - 15^{\circ}]$ =  $180 - 180 + 15^{\circ}$ 

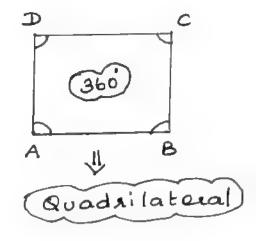
EXERCISE 4.2

i) The angles of a quadrilateral are in the ratio 2:4:5:7. Find all the angles.

Ratio: => 2:4:5:7  

$$2x+4x+5x+7x=360$$
  
 $18x=360$   
 $x=\frac{360}{18}$   
 $x=20$ 

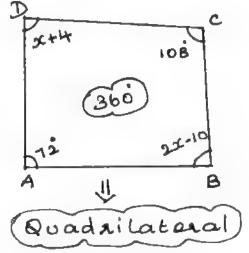
=) 
$$A = 2x = 2(20) = 40$$
  
 $B = 4x = 4(20) = 80$   
 $C = 5x = 5(20) = 100$   
 $D = 7x = 7(20) = 140$   
360



In a quadrilateral ABCD, LA=72 and LC is the supplementary of LA. The other two angles are 2x-10 and x+4. Find the value of x and the measure of all the angles.

D.

|C is the supplementary 09 LA :. |C = 180-72



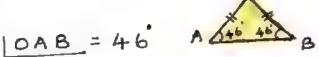
$$A + B + C + D = 360$$
  
 $72 + 2x - 10 + 108 + x + 4 = 360$   
 $3x + 184 - 10 = 360$   
 $3x + 174 = 360$   
 $3x = 360 - 174$   
 $3x = 186$ 

$$x = \frac{186}{3} 62$$

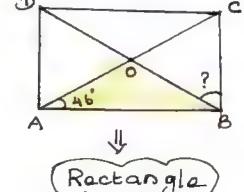
$$x = 62$$

$$=) \quad \underline{18} = 2x - 10 = 2(62) - 10 = 124 - 10 = 114$$

3) ABCD is a rectangle whose diagonals Ac and BD intersect at 0. It LOAB = 46° Find LOBC.



Similarly LOBA = 46



8

$$\begin{array}{c} \Rightarrow & | OBA + | OBC = 90^{\circ} \\ & + | OBC = 90^{\circ} \\ & | OBC = 90^{\circ} - 46^{\circ} \\ & | OBC = 44^{\circ} \\ \end{array}$$

4) The lengths of the diagonals of a Rhombus are 12 cm and 16 cm. Find the Side of the Rhombus.

Diagonals => 12 cm and 16 cm

In Rhombus, diagonals bisect

at 90

In A AOD,

$$AD^2 = AO^2 + OD^2$$

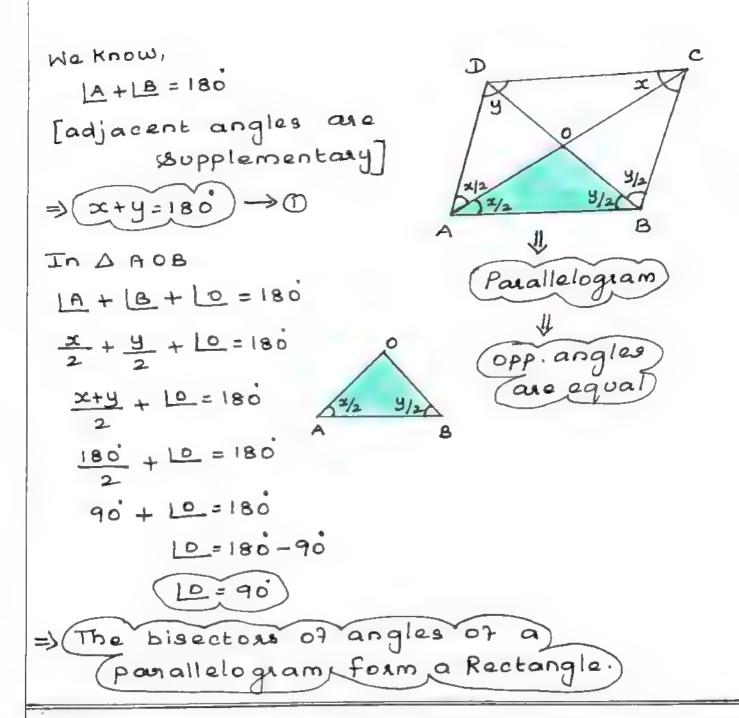
$$AD^2 = 8^2 + 6^2$$

$$AD^2 = 64 + 36$$

$$AD^2 = 100$$

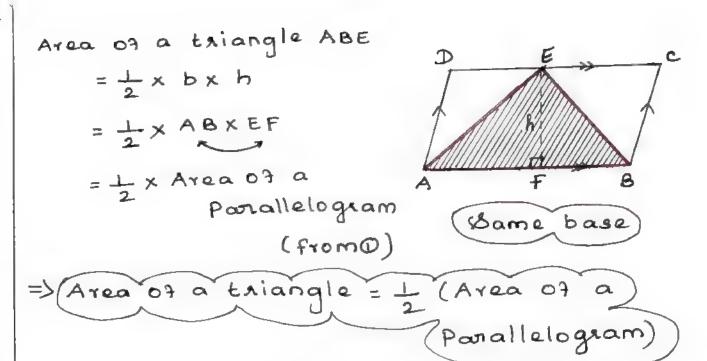


5) show that the bisectors of angles of a panallelogram form a Rectangle.

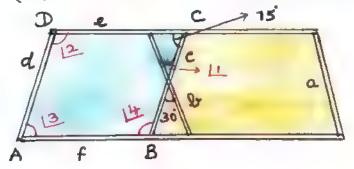


6) It a triangle and a parallelogram lie on the same base and between the same parallels, then prove that the area of the triangle is equal to half of the area of parallelogram.

Area of a Parallelogiam



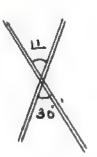
Thon rods a, b, c, d, e, and f are making a design in a bridge as shown in the figure. It all b, clld, ellf, find the marked angles between (i) b and c (ii) d and e (iii) d and f (iv) c and f



(i) band c:

(ii) dande:

ABCD is a parallelogram



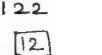
(iii) d and F:

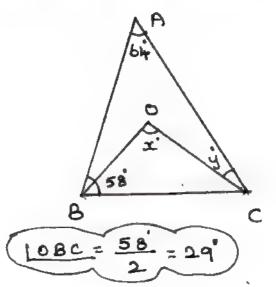
(iv) cand f:

(or)

8) In the given fig 4.39, 1A = 64, 1ABC = 58. If Bo and co one the bisectors of [ABC and LACB respectively of A ABC. find x and y.

In A ABC,

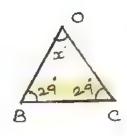




$$y' = \frac{1c}{2} = \frac{58}{2} = 29$$
 [co is the bisector]  
 $\Rightarrow y' = \frac{29}{2}$ 

In A OBC.

$$x+29+29=180$$
  
 $x+58=180$   
 $x=180-58$ 



(x = 122)

9) In the given fig. if AB=2, BC=6, AE=6, BF=8, CE=7 and CF=7, Compute the nation of the area of quadrilateral, ABDE to the area of ACDF (Use congruent property of triangles)

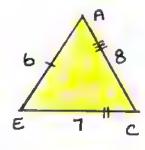
(Given:

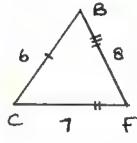
AB= 2, BC= 6,

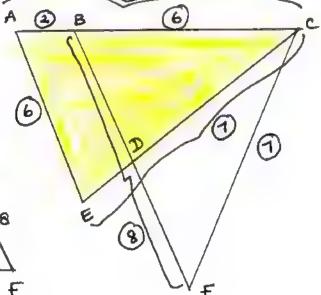
AE=6 , BF=8

CE=7 , CF=7

In A AEC and A BCf,







AE=BC, EC=CF, AC = BF

S DAEC & A BCF

13

=) Area of  $\Delta$  AEC = Area of  $\Delta$  BCF

[Subtract  $\Delta$  BDC on both sides]

Area of  $\Delta$  AEC - Area of  $\Delta$  BDC = Area of  $\Delta$  BCF

- Area of  $\Delta$  BDC

=) Area of a quadrilateral  $\lambda$  = Area of  $\Delta$  CDF.

ABDE

-	RaH	05 0912	equal)
			- V

10) In the figure, ABCD is a rectangle and EFGH is a parallelogram. Using the measurements given in the figure, what is the length d' or the segment that is perpendicular to HE and FG?

D

=) Area of a Rectangle A

ABCD

= (2xb)

= 10x8

5

80 cm<sup>2</sup>

Area of A AHE = \_

Area of DCGF

Area of A BEF =

(Area of DAG

AB = 4+6 = 10 cm (l)

AD = 3+5 = 8 cm (l)

В

5

Area of the panallelogram EF9H

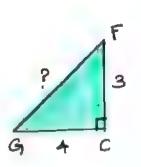
= Area of a Rectangle ABCD 
2(Area of DAHE) - 2(Area of DBEF)

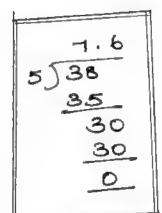
$$=80-2\left[\frac{1}{2}\times\cancel{A}\times3\right]-2\left[\frac{1}{2}\times\cancel{A}\times5\right]$$

$$=80-2(2\times3)-2(3\times5)$$

In 
$$\triangle$$
 GCF
$$/GF^2 = GC^2 + CF^2$$

$$G_1F^2 = 4^2 + 3^2$$

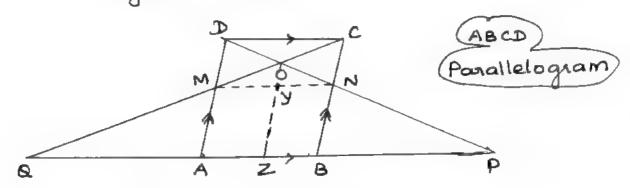




: Area 09 a Parallelogram EFGH = 38 cm2 basex height = 38 cm 5 x d = 38

11) In parallelogiam ABCD of the accompanying diagram, line DP is drawn bisecting Bc at N and meeting AB (extended) at P. From vertex c, line ca is drawn bisecting side

AD at M and meeting AB (extended) at Q. Lines DP and Ca meet at O. Show that the area of the parallelogram ABCD.



In A ADP

MN = 1 (AP) -> 2

In A BCQ,

$$MN = \frac{1}{2}(QB) \rightarrow 0$$

From 1 and 2

Area of A QOP = = xbxh

$$= \frac{1}{2} \times (QA + AB + BP) \times OZ$$

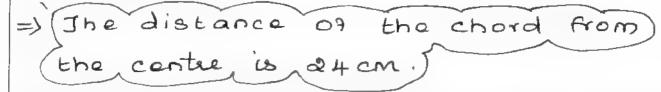
NOW, OZ = OY+YZ

= 0y + BN  
= 0y + 
$$\frac{1}{2}$$
 (Bc)  
=  $\frac{1}{2}$  (Nc) +  $\frac{1}{2}$  (Bc)  
=  $\frac{1}{2}$  ( $\frac{1}{2}$  Bc) +  $\frac{1}{2}$  (Bc)  
=  $\frac{1}{4}$  Bc +  $\frac{1}{2}$  Bc  
= Bc  $\left[\frac{1}{4} + \frac{1}{2}\right]$   
= Bc  $\left[\frac{3}{4}\right]$   
= Bc  $\left[\frac{3}{4}\right]$   
= DZ =  $\frac{3}{4}$  (Bc)  
PUE OZ =  $\frac{3}{4}$  (Bc) in (3)  
+ =) Area of  $\Delta$  Rop =  $\frac{1}{2}$  (3 AB) x OZ  
=  $\frac{1}{2}$  (3 AB) x  $\frac{3}{4}$  (Bc)  
=  $\frac{9}{8}$  (Abx Bc)  
Area of  $\Delta$  Rop =  $\frac{9}{8}$  (Area of Panallelogram)  
Hence Paprad.

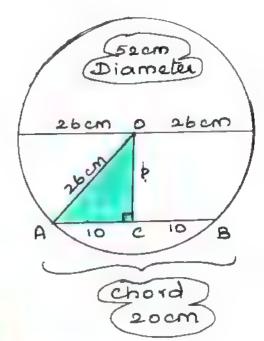
i) The diameter of the circle is 52 cm and the length of one of its chord is 20 cm. Find the distance of the chord from the centre.

Radius = 52 = 26 cm

IN A DAC,



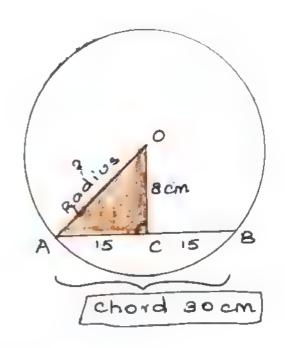
2) The chord of length 30cm is drawn



at the distance of 8cm from the centure of the circle. Find the Radius of the circle.

chord → 30cm Distance → 8cm

In  $\triangle$  OAC,  $OA^2 = OC^2 + AC^2$   $OA^2 = 8^2 + 15^2$   $OA^2 = 64 + 225$   $OA^2 = 289$  $OA^2 = 17^2$ 

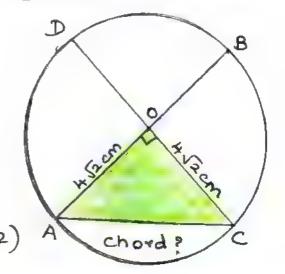


0A=17cm

3) Find the length of the chord AC where AB and CD are the two diameters perpendicular to each other of a circle with radius 452cm and also find LOAC and loca.

Radius = 4 Jzcm

In  $\triangle$  oAc,  $Ac^{2} = OA^{2} + Oc^{2}$   $Ac^{2} = (452)^{2} + (452)^{2}$   $Ac^{2} = (442)^{2} + (442)^{2}$   $Ac^{2} = (442)^{2} + (442)^{2}$ 



$$Ac^{2} = 32 + 32$$

$$Ac^{2} = 64$$

$$Ac^{2} = 8^{2}$$

$$Ac = 8cm$$

$$=) Jhe length of the chord  $Ac = 8cm$ 

$$To \triangle OAC,$$

$$90 + 2x = 180$$

$$2x = 180 - 90$$

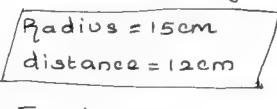
$$2x = 90$$

$$x = 90$$

$$x = 90$$

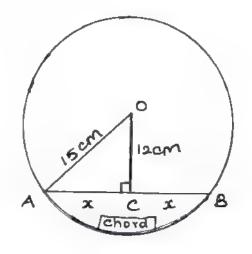
$$x = 45$$$$

4) A chord is 12cm away from the centre of the circle of radius 15cm. Find the length of the chord.



=) ( LOAC = 45, LOCA = 45°

In 
$$\triangle$$
 OAC  
 $OA^2 = OC^2 + AC^2$   
 $15^2 = 12^2 + AC^2$ 



$$225 = 144 + x^{2}$$

$$225 - 144 = x^{2}$$

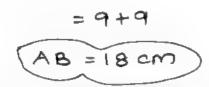
$$81 = x^{2}$$

$$x^{2} = 81$$

$$x^{2} = 9^{2}$$

$$x = 9 \text{ cm}$$

=) chord AB = x+x

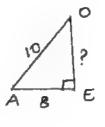


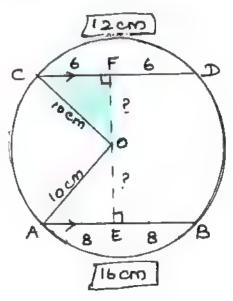
5) In a cincle, AB and cD one two Parallel chords with centre o and Aadius 10 cm Such that AB=16cm and cD=12cm. determine the distance between the two chords.

Radius = 10 cm AB = 16 cm CD = 12 cm

In  $\triangle$  OAE,  $OA^2 = OE^2 + AE^2$   $IO^2 = OE^2 + 8^2$   $IOO = OE^2 + 64$   $IOO - 64 = OE^2$  $36 = 0E^2$ 

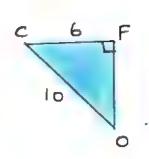
0E2 = 36





In A OFC

$$Oc^2 = Fc^2 + Fo^2$$



=) Distance between two chords

b) Two cincles of nadii 5 cm and 3 cm intersect at two points and the distance between their centres is 4 cm. Find the length of the common chord.

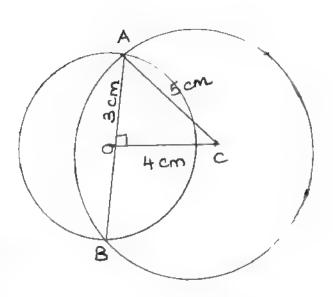
Radius => 5cm, 3cm

Distance between their centres is 4cm.

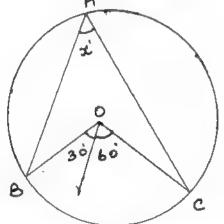
In A DAC,

$$5^2 = 3^2 + 4^2$$

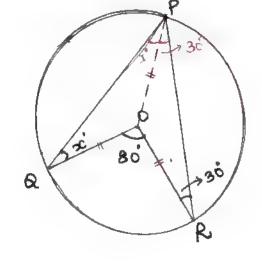
AB=> common chord



T) Find the value of x in the following figures.

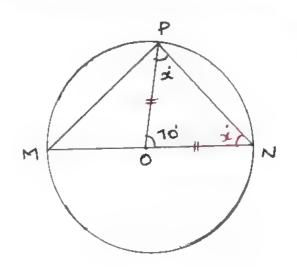


A OPR is an Isoceles talangle.



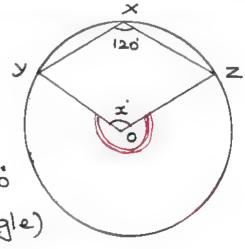
=) (x=10) (9 soceles Exiangle Property)

$$x = 110^{\circ}$$

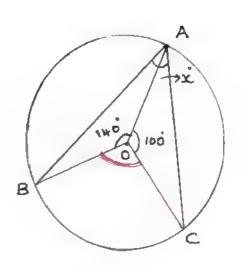


## (iv) exterior of yoz

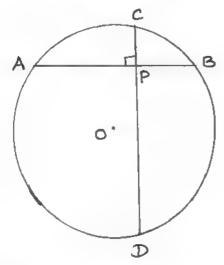
(whole angle)

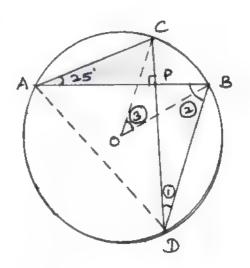


$$\Rightarrow$$
  $x = \frac{120}{2} = 60$ 



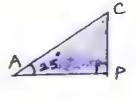
8) In the given figure, LAB = 25, find LBDC, LDBA and LCOB





In A ACP,





$$|C = 65$$

$$|Angle in a & ame & Segment|$$

$$|COB = 2 | CAB|$$

$$= 2(25)$$

$$|COB = 50$$

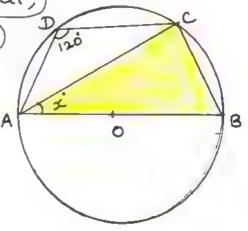
1) Find the value of oc in the given figure.

In a cyclic quadrilateral, (Som or opp angles are) (supplement ary LB + LD = 180

[c=90 [Angle in a semicircle is 90]

In A ACB x + 90 + 60 = 180x+150 = 180

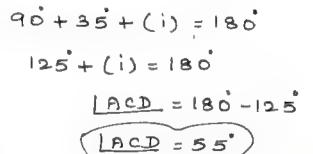
$$x = 180 - 150 = x = 30$$

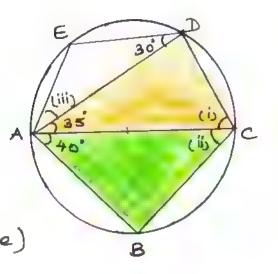


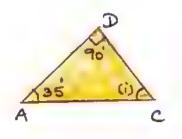
2) In the given figure, Ac is the diameter of the circle with centre 0. It [ADE = 30; [DAC = 35° and LCAB = 40 . Find (i) LACD (ii) LACB

(i) LACD ?

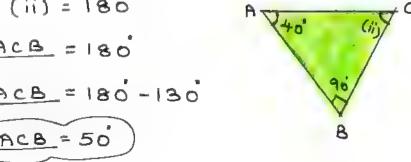
In A ACD,







In A ABC,



(iii) [DAE ?

3) Find all the angles of the given cyclic quadrilateral ABCD in the figure.

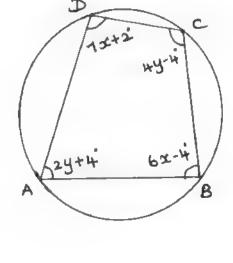
$$2y+1+4y-1=180$$

$$6y=180$$

$$y=\frac{180}{5}30$$

$$6x-4^{2}+7x+2^{2}=180^{2}$$

$$13x-2=180^{2}$$



$$|\Delta = 2y + 4 = 2(30) + 4 = 60 + 4 = 64$$

$$|B = 6x - 4 = 6(14) - 4 = 84 - 4 = 80$$

$$|C = 4y - 4 = 4(30) - 4 = 120 - 4 = 116$$

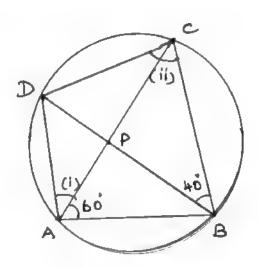
$$|D = 7x + 2 = 7(14) + 2 = 98 + 2 = 100$$

$$|360$$

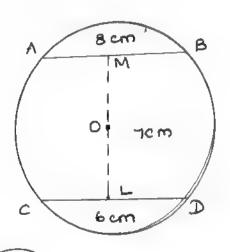
4) In the given figure, ABCD is a cyclic quadrilateral where diagonals intersect at P such that [DBC = 40 and [BAC = 60 find (i) [CAD (ii) [BCD]

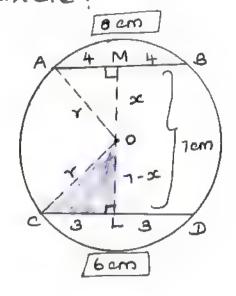
a same segme

$$A = (i) + 60$$
  
=  $40 + 60$ 



5) In the given figure, AB and CD one the parallel chords of a cincle with centre o such that AB=8cm and CD = 6 cm. It OM \_ AB and OLICD distance between LM is 7cm. Find the radius of the circle?





Given

OM LAB OL LCD

In A AMO, OA2 = OM2 + MA2  $y^2 = x^2 + 4^2$  $y^2 = x^2 + 16 \longrightarrow 0$ 

Form (1) and (2) xx+16= x2-14x+58 14x = 58-16

$$x = \frac{4x}{3}$$

$$x = \frac{4x}{3}$$

$$x = 3$$
Put  $x = 3$  in (1)
$$x^2 = x^2 + 16$$

$$x^2 = (3)^2 + 16$$

$$x^2 = 9 + 16$$

$$x^2 = 25$$

$$x^2 = 5^2$$

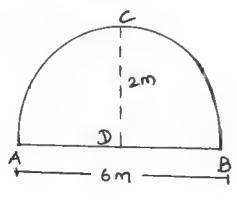
$$x = 5^2$$

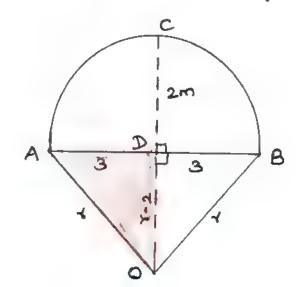
$$x = 5^2$$
Padius of the circle

6) The auch of a buildge has dimensions as shown, where the auch measure 2m at its highest point and its width is 6m. What is the madius of the circle that contains the auch?

is 5 cm

31





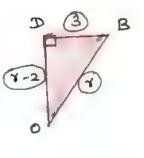
OA, OB, OC => radius => &

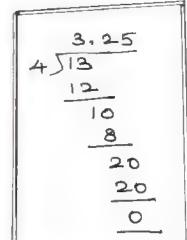
In A OBD

$$OB^2 = BD^2 + OD^2$$

$$x^2 = 3^2 + (x-2)^2$$
 0

$$y^2 = 9 + (\tau)^2 + (2)^2 - 2(\tau)(2)$$

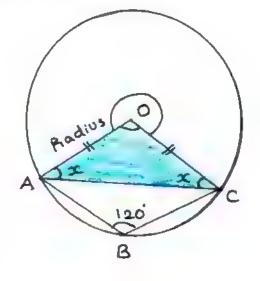




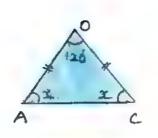
## =) (Radius of the circle = 3.25 m

7) In figure, LABC = 120, where A, B and c are points on the circle with centre o . Tind LOAC?

32



In  $\triangle$  Aoc, x+x+120=180 2x+120=180 2x=180-120 2x=60 $x=\frac{60}{2}$ 



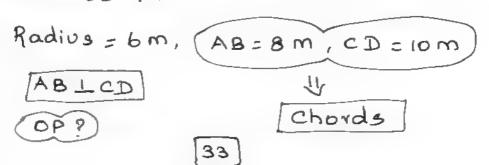
$$x = \frac{60}{2}$$

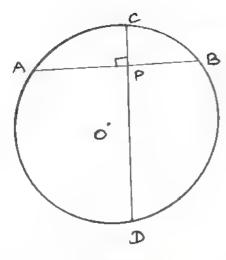
$$x = 30$$

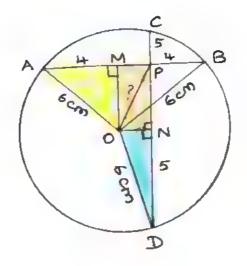
$$\Rightarrow 0$$

$$\Rightarrow 0$$

Plantation programme. For this a teacher allotted a circle of radius 6m ground to nineth standard students for planting sapplings. Four students Plant trees at the points A,B,C and D as shown in figure. Here AB=8m, CD=10m and AB LCD. It another student Places a flower pot at the Point P, the intersection of AB and CD, then find the distance from the centre to P.







In A AMO

$$Ao^2 = AM^2 + MO^2$$
  
 $6^2 = 4^2 + MO^2$ 

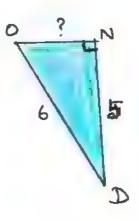
In A OND,

$$OD^2 = ON^2 + ND^2$$

$$6^2 = 0N^2 + 5^2$$

$$36 = 0N^2 + 25$$

$$11 = 0N^2$$



In A ONP OP = ON + PN  $OP^2 = (\sqrt{11})^2 + (\sqrt{20})^2$ Op2 = 11+20

$$OP^{2} = ON^{2} + PN$$

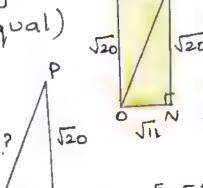
$$OP^{2} = (\sqrt{11})^{2} + (\sqrt{20})^{3}$$

$$OP^{2} = 11 + 20$$

$$OP^{2} = 31$$

$$OP = \sqrt{31}$$

OP = 5.56



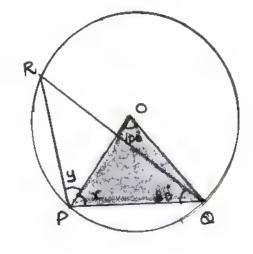
	5,56
5 (	31.0000
	25 +4
105	600
	525
1106	7500
	6636
	864

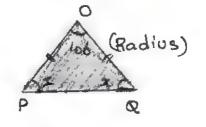
9) In the given figure, [ poq = 100 and LPAR = 30, then find IRPO

[PAR = 30, [POQ = 100

In A OPR 100 + x + x = 180 100+2x=180

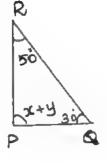
$$2x = 180 - 100$$
 $2x = 80$ 

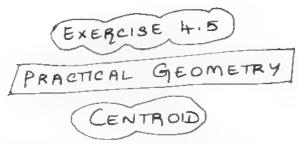




$$x = \frac{80}{2}$$
 $x = 40$ 
 $x = 40$ 

=> [RPO=60



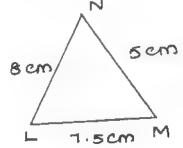


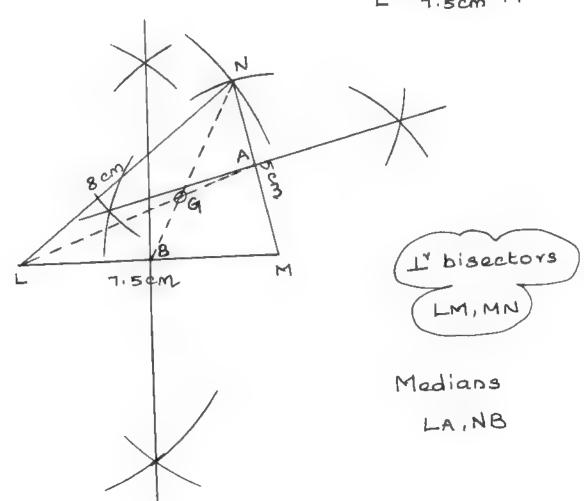
1) Construct A LMN, where LM= 7.5cm,

MN=5cm, LN=8cm. Locate its

centroid.

ROUGH DIAGRAM





#### 1) CONSTRUCTION !

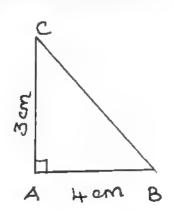
- \* D 51 aw LM = 7.5 cm
- \* With L and M as centre draw two ares of radius 8cm and 5cm to meet at N.
- \* Join LN and MN
- \* Thus A LMN is the Required triangle.
- \* Draw the perpendicular bisector of any two sides [LM and MN] to meet at A and B.
- \* Join the medians LA and NB to meet at 'G'.
- \* 'G' is the centroid of A LMN.
- 2) Draw and locate the centroid of triangle ABC where right angled at A where AB=4cm and Ac=3cm.

ROUGH DINGRAM

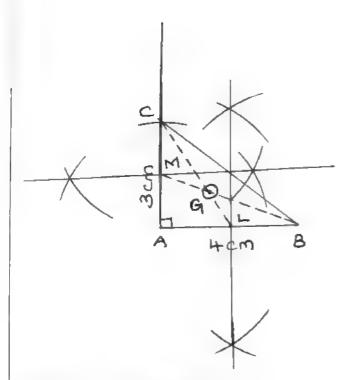
Right angled triangle

L' bisectors => AB, AC

Medians CL, BM

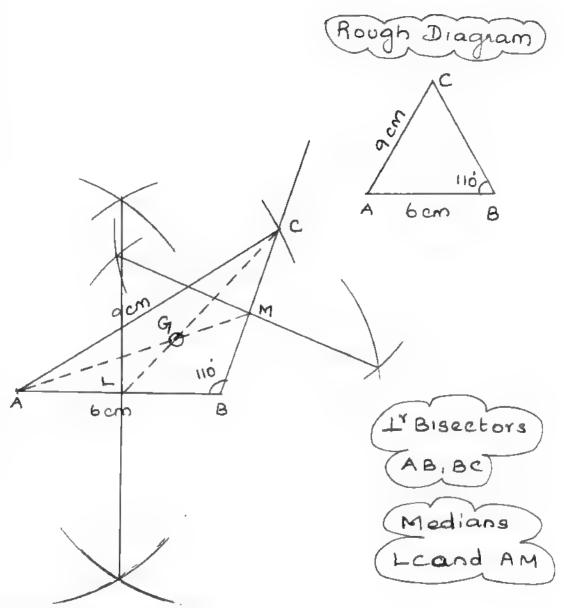


38



### 2) CONSTRUCTION!

- \* Draw AB = 4cm
- \* With A as centre make an angle 90
- \* With A as centre draw an are of radius sem to meet at c.
- \* Join BC
- \* Thus A ABC is the orequired triangle.
- \* Draw the perpendicular bisector of any two Bides [AB and Ac] to meet at Land M.
- \* Join the medians BM and CL to meet at G.
- \* 'G' is the centroid of A ABC.
- 3) Draw DABC, where AB=6cm, [B=110]
  AC=9cm and construct the centroid.



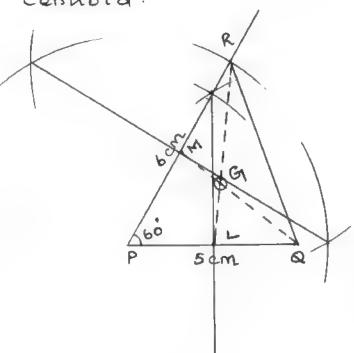
#### 3) CONSTRUCTION:

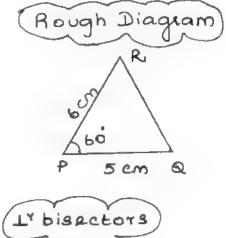
- \* Donaw AB=6cm
- \* With Bas centre make an angle 110
- \* With A as centure draw an one of madius 9cm to meet at c.
- \* Join Ac
- \* Thus A ABC is the required triangle.
- \* Donaw the perpendicular bisector of any two sides [AB and Bc] to meet at L and M.
- \* Join the medians CL and AM to

meet at 'g'.

# \* G is the centroid of A ABC

PR=6cm, Lapr=60 and Locate its
centroid.





Pa, PR

Medians

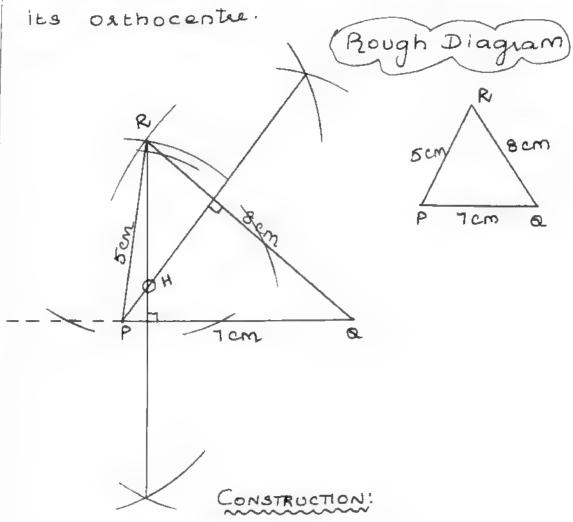
LR, am

4) CONSTRUCTION:

- \* Draw Pa= 5cm
- \* With Pas centre make an angle 60
- \* With P as centre draw an arc of radius 6 cm to meet at R.
- \* Join OR
- \* Thus A PQR is the required topiangle.
- \* Draw the perpendicular bisector of any two sides [pa and pr] to meet at L and M.
- \* Join the medians RL and QM to meet at q.
- \* G is the control of APRR.

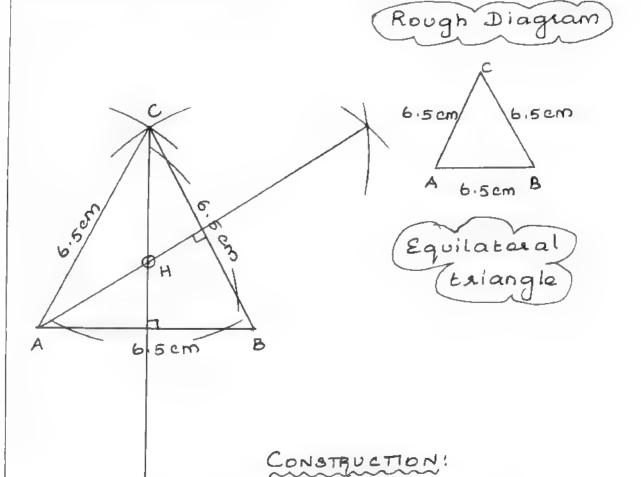
### ORTHOCENTRE

5) Draw D Par with Sides Pa=Tem, ar=8cm and Pr=5cm and construct



- \* Draw Pa=7cm
- \* With P and Q as Centre, 5cm and 8cm Radius, draw two ares to meet at R
- \* Join PR and QR
- \* Thus A Par is formed.
- \* Draw altitudes from any two vertices to their opposite Bides to meet at H'.
- \* H' is the Dathocentre of A Par

6) Draw an equilateral triangle of sides 6.5cm and locate its outhocentre.



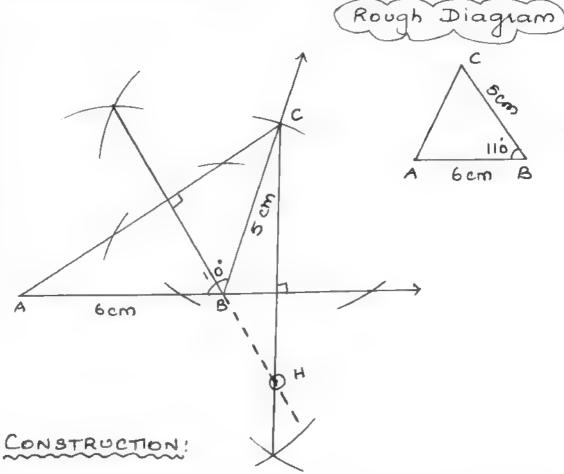
\* Draw AB = 6.5 cm

\* With A and B as centre,

meet at c.

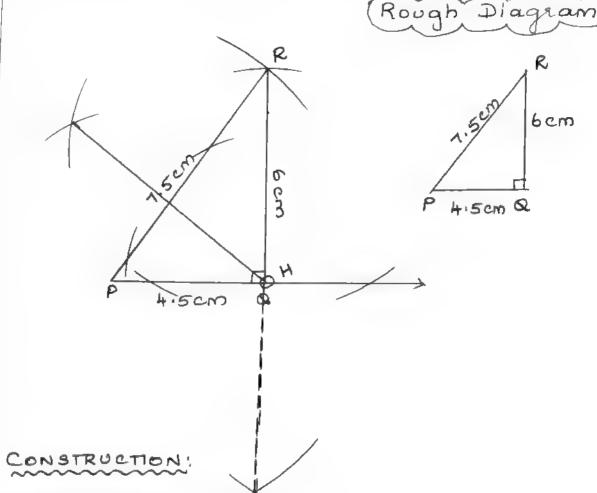
- \* Join Ac and Bc
- \* Thus A ABC is formed.
- \* Draw Altitudes from any two vertices to their opposite Bides to meet at H.
- \* H is the oathocentre of A ABC.

1) Draw A ABC, where AB=6cm, [B=110, and Bc=5cm and construct its orthocentre.



- \* Draw AB = 6 cm.
- \* With B as centre make an angle 110
- \* With B as centre, 5 cm radius, draw an are to meet at c.
- \* Join Ac
- \* Thus A ABC is formed
- \* Daaw altitudes from any two vertices to their opposite sides to meet at H.
- \* H is the osthocentre of AABC.

B) Draw and locate the oxthocenter of a right triangle Par where Pa=4.5cm, ar=6cm, pr=7.5cm.



\* Draw Pa= 4:5 cm

\* With P and @ as centre 7.5 cm and 6 cm radius, draw two ares to meet at R.

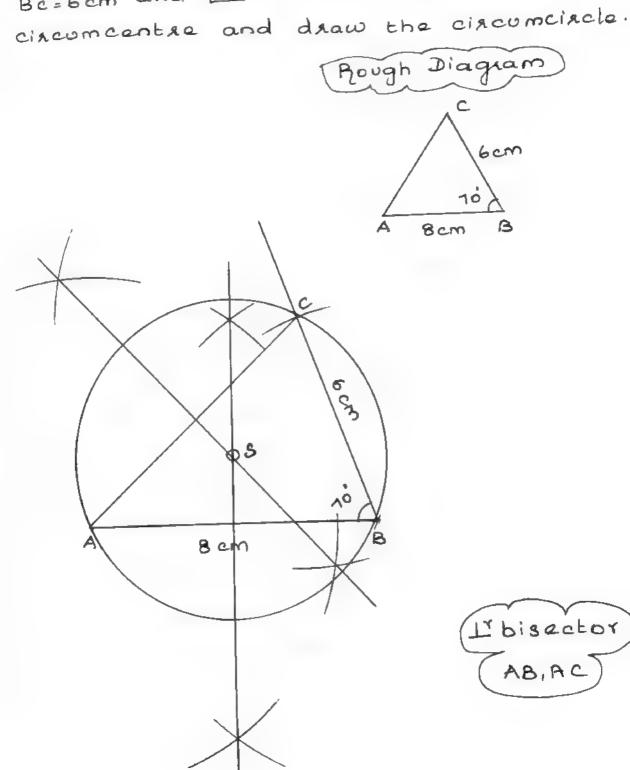
- \* Join PR and OR
- \* Thus A Par is formed.
- \* Draw altitudes From any two vertices to their opposite sides to meet at H.
- \* H is the outhocentre of A PQR.



1) Draw a triangle ABC, where AB= 8cm,

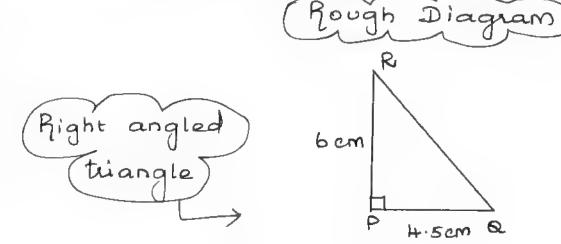
Bc=bcm and LB= 70 and locate its

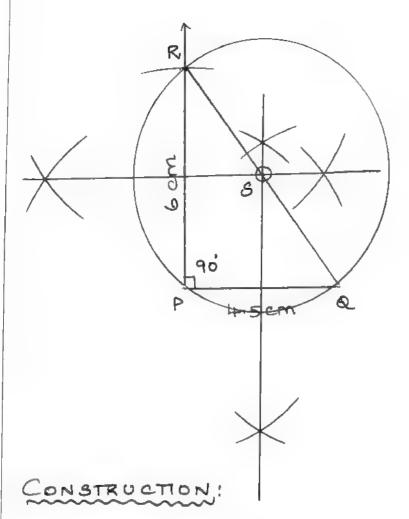
circumcentre and draw the circumcircle.



### 1) CONSTRUCTION:

- \* Draw AB = 8cm
- \* With B'as contre make an angle 70
- \* With 'B' as centre draw an auc 07 radius 6cm to meet at c.
- \* Join AC
- \* Thus A ABC is formed.
- \* Draw the perpendicular bisectors of any two sides (AB and Ac) to meet at 's'.
- \* 's' is the circumcentee of the triangle.
- \* With 's' as centre, SA, SB and SC as radius draw the circumcircle.
- 2) Construct the Right angled triangle Par whose perpendicular sides are 4.5 cm and 6 cm. Also locate its circumcentre and draw circumcircle.





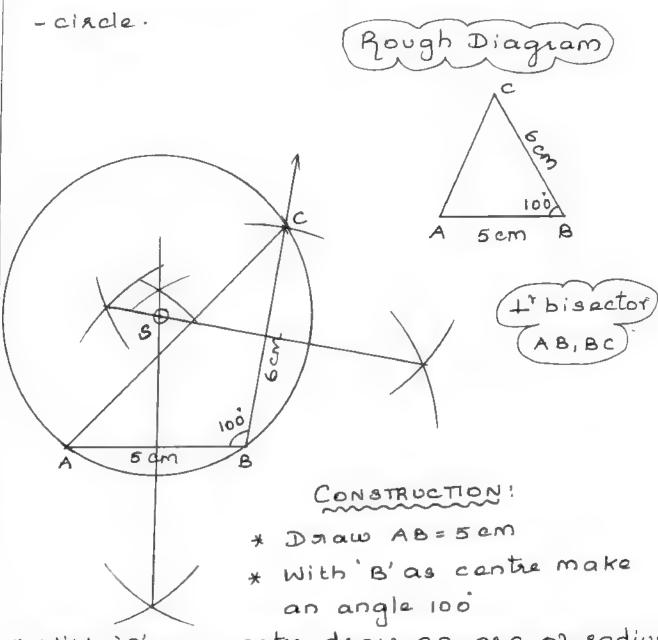
L' bisactor (PQ,PR)

- \* Draw PQ = 4.5cm
- \* With p'as centre make an angle 90
- \* with 'p' as centre draw an arc of radius 6cm to meet at R.
- \* Join ar
- \* Thus A Par is formed.
- \* Draw the perpendicular bisectors of any two sides (PR and PR) to meet at's'.
  - \* 'S' is the circumcentre of the triangle.
  - \* With 's' as centre SP, SQ, SR as Radius [48] draw the circumcircle.

3) Construct A ABC with AB=5cm,

[B=100 and Bc=6cm. Also Locate

its circumcentue and deaw circum

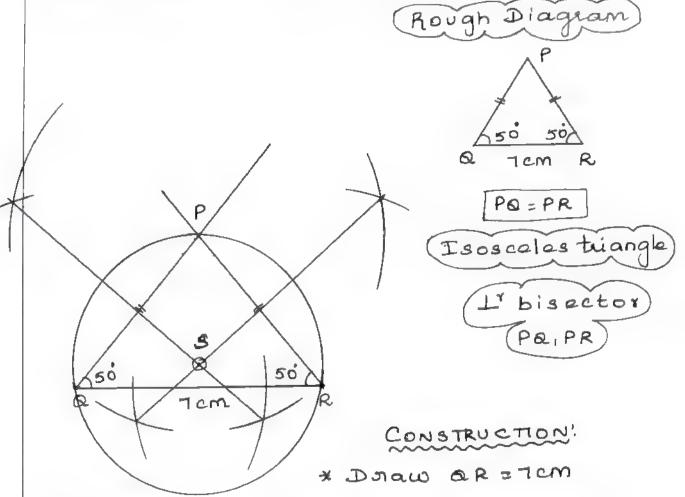


- \* With 'B' as centre deaw an arc of radius 6cm to meet at c.
- \* Join AC
- \* Thus A ABC is formed
- \* Draw the perpendicular bisectors of any two sides (AB, Bc) to make at 3.
- \* '3' is the circumcente of the triangle.

  \* With 's' as centre, SA, SB, SC as radius

49 draw the clacum clacle.

4) Construct an Isosceles triangle PER where PE=PR and La=50, ER=7cm.
Also draw its circumcircle.



\* With a and R as centre make an angle 50° to meet at P.

\* Thus A Par is formed.

\* Draw the perpendicular bisectors of any two sides [pa and PR] to meet at s.

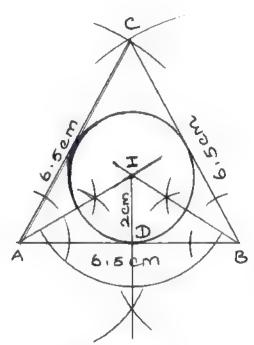
\*'s' is the circumcentre of the triangle.

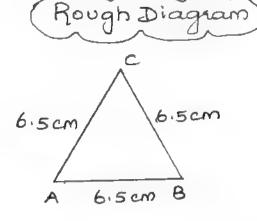
\* with 's' as centre SP, SQ and SR as radius draw the circumcircle.

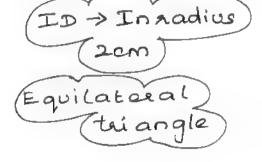
## Incentae

5) Draw an equilateral triangle of sides 6.5 cm and locate its incentre.

Also draw the incircle.



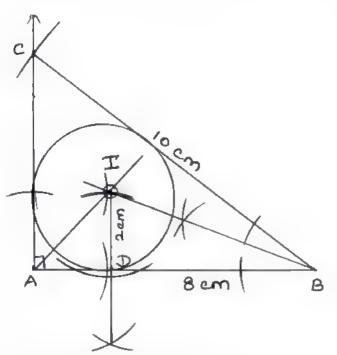


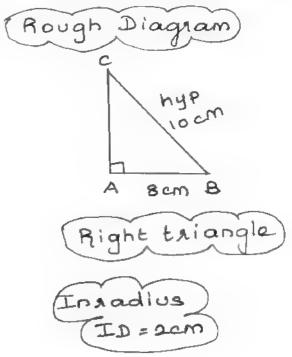


#### CONSTRUCTION:

- \* Draw AB = b.5cm
- \* With A and B as centre, draw two ares
  - \* Join Ac and BC
  - \* Thus A ABC is formed.
  - \* Draw the angle bisectors of A and B to meet at I
  - \* I' is the incentre of the triangle.
- \* Draw perpendicular from I to AB to meet at 'D'
- \* With I as centre and ID as Radius draw the incircle that touches all sides of the triangle. \* Instadius ID=2cm.

6) Draw a sight triangle whose hypotenuse is 10cm and one of the legs is 8 cm. Locate its incentre and also draw incincle.



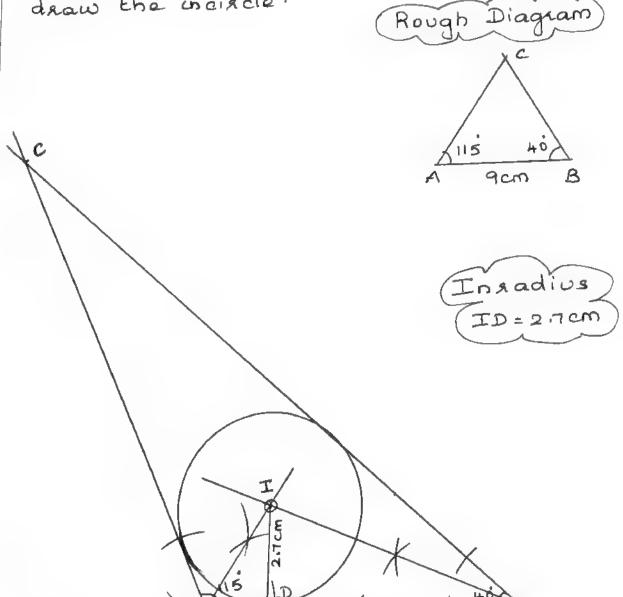


#### CONSTRUCTION;

- \* Draw AB=Bcm
- \* With 'A' as centre make an angle 90
- \* With B' as centre draw an arc of radius 10cm too meet at c.
  - \* Join BC , Thus A ABC is formed.
- \* Draw the angle bisectors of A and B to meet at I.
  - \* I is the incenter of the tainingle.
- \* Draw the perpendicular from I to AB to meet at D.
- \* With I as centre and ID as radius draw the incircle that touches all sides of the tuangle.
  - \* Innadius ID=2cm

7) Draw A ABC, given AB= 9cm, ICAB=115 and LABC = 40. Locate its incentire and also

draw the incircle.



CONSTRUCTION:

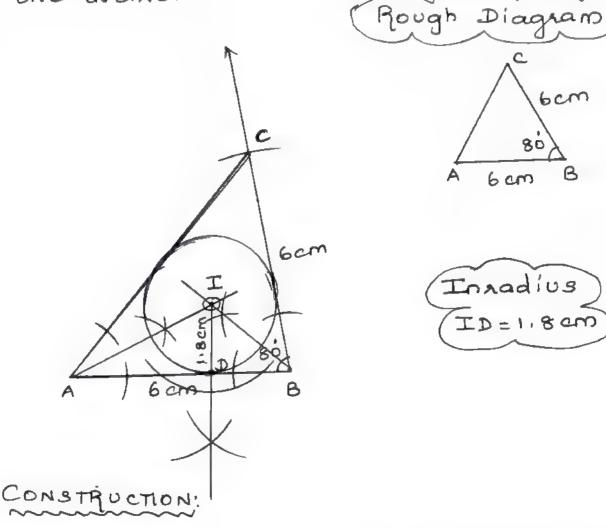
\* D J a w A B = 9cm

\* With A and B as centre make angles 115 and 40 to meet at c.

\* Thus AABC is formed.

\* Draw the angle bisectors of A and B to meet at I. 53

- \* I is the incentre of the triangle.
- \* Draw perpendicular from I to AB to meet at D.
- \* With I as centre and ID as radius draw the incircle that touches all sides of the triangle.
  - \* In Radius, ID = 2.7cm.
- 8) Construct AABC in which AB=BC=6cm, LB=80. Locate its incentre and draw the incircle.



- \* Draw AB = 6 cm
- \* With B as centre make an angle

- \* With 'B' as centre draw an arc of radius 6 cm to meet at c.
- \* Join Ac
- \* Thus A ABC is formed.
- \* Donaw the angle bisectors of A and B to meet at I.
  - \* I is the incentre of the triangle.
- \* Donaw perpendicular from I to AB to meet at D.
- \* With I as centre and ID ors radius draw the incircle that touches all sides of the triangle.
  - \* Insadius ID = 1.8 cm.

# CHAPTER-5 CO- ORDINATE GEOMETRY EX 5:1

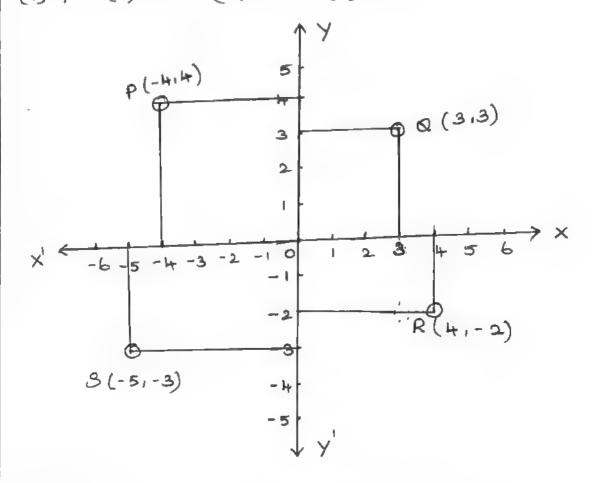
1) Plot the following points in the co-ordinate system and identity the quadrants.

P(-7,6) a (7,-2) R(-6,-7) 3 (3,5) and T (3,9) PT(3,9) TT P (-1,6) 8 3(3,5) 5 4 3 2 6 -5 -4 -3 -2 -1 -2 Q (7,-2) -3 14 一件 -5 -6 R (-6,-7) -8 111

POINTS	QUADRANTS	
P (-7,6)	I	
Q (7,-2)	TY	
R (-6,-7)	TIT.	
3 (3,5)	工	
T (3,9)	エ	

2) White down the abscissa and ordinate of the following from figure.

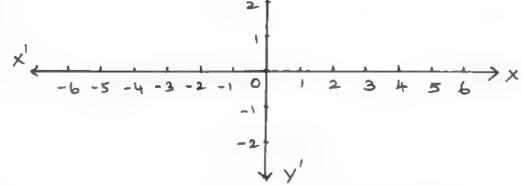
(i) P (ii) Q (iii) R (iv) S

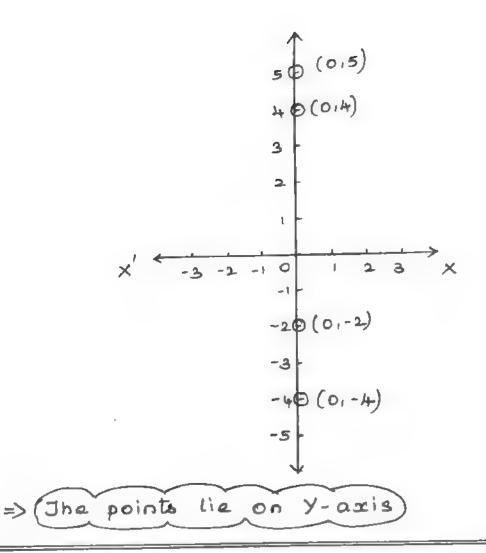


		1
POINTS	abscissa	Ordinate
(i) P(-4,4)	- 4·	4
(ii) Q (3,3)	3	3
(iii) R (4,-2)	4	-2
(iv) 3 (-5, -3)	-5	-3

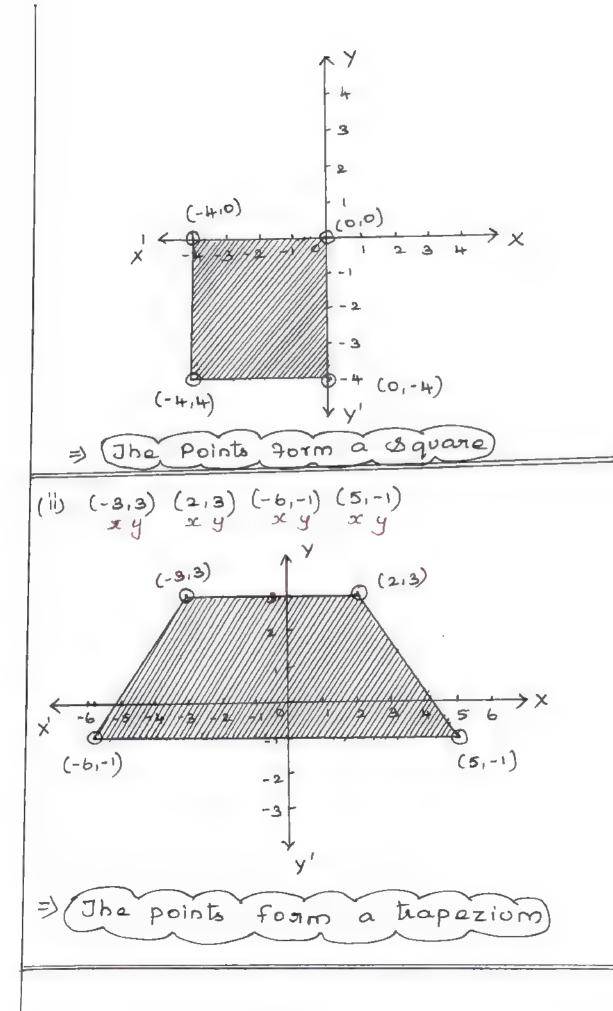
3) Plot the following points in the co-ondinate plane and join them. What is your conclusion about the mesulting figure?

(i) 
$$(-5,3)$$
  $(-1,3)$   $(0,3)$   $(5,3)$   $(-5,3)$   $(-5,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$   $(-1,3)$ 





4) Plot the following points in the co-ondinate plane. Join them in order. What type or geometrical shape is formed?



1. Find the distance between the following Pair of Points.

Distance = 
$$\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}$$

$$= \int (4-1)^2 + (3-2)^2$$

$$=\int (3)^2 + (1)^2$$

$$= \int (-7-3)^2 + (2-4)^2$$

$$= \sqrt{(-10)^2 + (-2)^2}$$

$$= \int (c-a)^2 + (b-b)^2$$

= 
$$\int (c-a)^2 + (o)^2$$
  
=  $\int (c-a)^2$   
=  $c-a$  units

(iv) 
$$(3,-9)(-2,3)$$
  
 $x_1 y_1 x_2 y_2$   
Distance =  $\int (x_2-x_1)^2 + (y_2-y_1)^2$   
=  $\int (-2-3)^2 + (3+9)^2$   
=  $\int (-5)^2 + (12)^2$   
=  $\int 25 + 11 + 14$   
=  $\int 169$   
=  $\int (13)^2$   
= 13 units.

a) Determine whether the given set of points in each case are Collineau or not?

$$A(7,-2) B(5,1)$$
  
 $x_1 y_1 x_2 y_2$ 

AB = 
$$\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}$$
  
=  $\sqrt{(5-7)^2+(1+2)^2}$ 

Bc = 
$$\int (x_2-x_1)^2 + (y_2-y_1)^2$$
  
=  $\int (3-5)^2 + (4-1)^2$ 

$$= \int (-2)^{2} + (3)^{2}$$

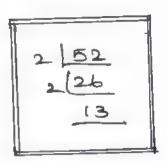
$$= \int 4+9$$
AB =  $\sqrt{13}$  Units

$$= \sqrt{(-2)^2 + (3)^2}$$

$$= \sqrt{4+9}$$
BC =  $\sqrt{13}$  unib

AC = 
$$\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$
  
=  $\sqrt{(3-7)^2 + (4+2)^2}$   
=  $\sqrt{(-4)^2 + (6)^2}$   
=  $\sqrt{16+36}$   
=  $\sqrt{52}$   
=  $\sqrt{2 \times 2 \times 13}$ 

AC= 2 Jis unità



$$\sqrt{13} + \sqrt{13} = 2\sqrt{13}$$
 $2\sqrt{13} = 2\sqrt{13}$ 

A 
$$(a_1-2)$$
 B  $(a_13)$   
 $x_1y_1$   $x_2y_2$   
AB =  $\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$   
=  $\sqrt{(a-a)^2 + (3+2)^2}$   
=  $\sqrt{(5)^2}$   
AB =  $\sqrt{(5)^2}$ 

$$A(a_{1}-2) C(a_{1}0)$$

$$x_{1}y_{1} x_{2}y_{2}$$

$$AC = \sqrt{(x_{2}-x_{1})^{2} + (y_{2}-y_{1})^{2}}$$

$$= \sqrt{(a-a)^{2} + (o+2)^{2}}$$

$$= \sqrt{(o)^{2} + (2)^{2}}$$

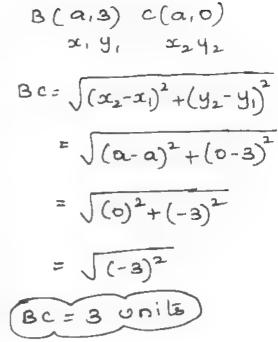
$$= \sqrt{(2)^2}$$

$$Ac = 2 \text{ units}$$

$$= 3 + 2$$

5 = 5

.. The points are Collinear.



$$=\sqrt{(2-5)^2+(0-4)^2}$$

$$= \sqrt{(-3)^2 + (-4)^2}$$

$$A(5,4) \subset (-2,3)$$
  
 $x_1 y_1 \qquad x_2 y_2$ 

BC = 
$$\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}$$

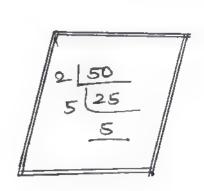
$$= \sqrt{(-2-2)^2 + (3-0)^2}$$

$$= \sqrt{(-4)^2 + (3)^2}$$

$$AC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(-2 - 5)^2 + (3 - 4)^2}$$

$$=\sqrt{(-7)^2+(-1)^2}$$



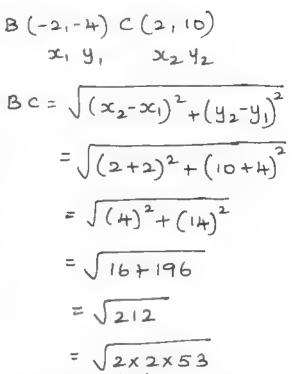
$$Ac = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(2 - 6)^2 + (10 + 4)^2}$$

$$= \sqrt{(-4)^2 + (14)^2}$$

= \[ 212

4) Show that the points taken in Order form an equilateral triangle is each



(i) 
$$A(2,2) B(-2,-2) C(-2\sqrt{3},2\sqrt{3})$$
 $A(2,2) B(-2,-2)$ 
 $x_1y_1$ 
 $x_2y_2$ 
 $AB = \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$ 
 $= \sqrt{(-2-2)^2 + (-2-2)^2}$ 
 $= \sqrt{(-4)^2 + (-4)^2}$ 
 $= \sqrt{16+16}$ 
 $AB = \sqrt{32 \text{ on } 18}$ 
 $B(-2,-2) C(-2\sqrt{3},2\sqrt{3})$ 
 $x_1 y_1$ 
 $x_2 y_2$ 
 $BC = \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$ 
 $= \sqrt{(-2\sqrt{3})^2 + (2)^2 + 2(-2\sqrt{3})(2) + (2\sqrt{3})^2 + (2)^2 + 2(2\sqrt{3})(2)}$ 
 $= \sqrt{(+x^3)^2 + (-2\sqrt{3})^2 + (-2\sqrt{3})(2) + (-2\sqrt{3})^2 + (-2\sqrt{3})(2)}$ 
 $= \sqrt{(-2\sqrt{3})^2 + (2)^2 + 2(-2\sqrt{3})(2) + (-2\sqrt{3})^2 + (-2\sqrt{3})(2)}$ 
 $A(2,2) C(-2\sqrt{3},2\sqrt{3})$ 
 $A(3,3) A(3,3) A($ 

$$= \int (-2\sqrt{3})^{2} + (2)^{2} - 2(-2\sqrt{3})(2) + (2\sqrt{3})^{2} + (2)^{2} - 2(2\sqrt{3})(2)$$

$$= \int (4\times3) + 4 + 8\sqrt{3} + (4\times3) + 4 - 8\sqrt{3}$$

$$= \sqrt{12+4+12+4}$$

$$Ac = \sqrt{32} \text{ units}$$

$$= \sqrt{(0-\sqrt{3})^2 + (1-2)^2}$$

$$=\sqrt{(-\sqrt{3})^2+(-1)^2}$$

$$A(\sqrt{3},2) \subset (0,3)$$
  
 $x_1 y_1 x_2 y_2$ 

$$AC = \int (x_2 - x_1)^2 + (y_2 - y_1)^2$$

$$= \int (0 - \sqrt{3})^2 + (3 - 2)^2$$

B(0,1) c(0,3)  

$$x_1 y_1 \quad x_2 y_2$$
  
Bc =  $\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}$ 

$$= \sqrt{(0-0)^2 + (3-1)^2}$$
$$= \sqrt{(0)^2 + (2)^2}$$

$$= \sqrt{(-\sqrt{3})^{2} + (1)^{2}}$$

$$= \sqrt{3+1}$$

$$= \sqrt{4}$$

$$= \sqrt{(2)^{2}}$$

$$Ac = 2 \text{ units}$$

$$\Rightarrow \sqrt{AB = Bc = Ac}$$

$$\therefore \text{ It is an equilateral triangle}$$

$$\Rightarrow \text{ Show that tha following points to exide form the vertices of a parallelogram.}$$

$$(i) A(-3,1) B(-6,-7) c(3,-9) D(6,-1)$$

$$A(3,1) B(-6,-7) c(3,-9) D(6,-1)$$

$$x_{1}y_{1} x_{2}y_{2}$$

$$AB = \sqrt{(x_{2}-x_{1})^{2} + (y_{2}-y_{1})^{2}}$$

$$= \sqrt{(-6+3)^{2} + (-7-1)^{2}}$$

$$= \sqrt{(-3)^{2} + (-8)^{2}}$$

$$= \sqrt{9+64}$$

$$AB = \sqrt{73} \text{ units}$$

$$C(3,-9) D(6,-1)$$

$$x_{1}y_{1} x_{2}y_{2}$$

$$A = \sqrt{(x_{2}-x_{1})^{2} + (y_{2}-y_{1})^{2}}$$

$$A = \sqrt{(x_{1}-x_{1})^{2} + (y_{2}-y_{1})^{2}}$$

5) Show that the following points taken in exdex form the vertices of a parallelogram.

i) 
$$A(-3,1)$$
  $B(-6,-1)$   $C(3,-9)$   $D(6,-1)$ 

A(-3,1)  $B(-6,-7)$   $C(3,-9)$   $C($ 

$$= \sqrt{(6-3)^2 + (-1+9)^2}$$

$$= \sqrt{(3)^2 + (8)^2}$$

$$= \sqrt{9+64}$$

$$CD = \sqrt{13} \text{ units}$$

$$AB = CD$$

$$= \sqrt{(6+3)^2 + (-1-1)^2}$$

$$= \sqrt{(9)^2 + (-2)^2}$$

$$= \sqrt{81+4}$$
AD =  $\sqrt{85}$  Units

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(5 + 7)^2 + (10 + 3)^2}$$

$$= \sqrt{(12)^2 + (13)^2}$$

$$= \sqrt{144 + 169}$$

BC = 
$$\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$
  
=  $\sqrt{(15-5)^2 + (8-10)^2}$   
=  $\sqrt{(10)^2 + (-2)^2}$   
=  $\sqrt{100+4}$   
BC =  $\sqrt{104}$  Units

$$C(15.8) D(3,-5)$$

$$x_1 y_1 x_2 y_2$$

$$CD = \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$

$$= \sqrt{(3-15)^2 + (-5-8)^2}$$

$$= \sqrt{(-12)^2 + (-13)^2}$$

$$= \sqrt{144 + 169}$$

$$CD = \sqrt{313} \text{ Units}$$

$$A(-7,-3) D(3,-5)$$

$$x_1 y_1 x_2 y_2$$

$$AD = \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$

$$= \sqrt{(3+7)^2 + (-5+3)^2}$$

$$= \sqrt{(10)^2 + (-2)^2}$$

$$= \sqrt{100 + 4}$$

AD= JIOH Units

6) Verity that the following points taken in order form the vertices of a Rhombus.

AB = 
$$\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$
  
=  $\sqrt{(7-3)^2 + (6+2)^2}$   
=  $\sqrt{(4)^2 + (8)^2}$ 

$$= \sqrt{(-1-7)^2 + (2-6)^2}$$

$$= \sqrt{(-8)^2 + (-4)^2}$$

$$= \sqrt{(-5+1)^2 + (-6-2)^2}$$

$$=\int (-4)^2 + (-8)^2$$

$$A(3,-2) D(-5,-6)$$
  
  $x_1 y_1 x_2 y_2$ 

$$AD = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(-5-3)^2 + (-b+2)^2}$$

$$= \int (-8)^2 + (-4)^2$$

=) AB=BC=CD=AD

It is a Phombus

$$D(1,2)$$

$$C(2,2) D(1,2)$$

$$x_1 y_1 x_2 y_2$$

$$CD = \int (x_2 - x_1)^2 + (y_2 - y_1)^2$$

$$= \int (-1)^2 + (0)^2$$

$$= \int (-1)^2 + (0)^2$$

$$CD = |U \cap I| = 0$$

$$A(1,1) D(1,2)$$

$$x_1 y_1 x_2 y_2$$

$$AD = \int (x_2 - x_1)^2 + (y_2 - y_1)^2$$

$$= \int (1-1)^2 + (2-1)^2$$

$$= \int (0)^2 + (1)^2$$

$$= \int (1)^2 + (1)^2$$

$$= \int (1)^2 + (1)^2$$

7) It A (-1,1) B(1,3) and C(3,a) are points and if [AB=BC], then find'a'.

A (-1,1) B (1,3)  

$$x_1 y_1 \quad x_2 y_2$$
  
AB=  $\int (x_2 - x_1)^2 + (y_2 - y_1)^2$ 

$$B(113) C(3,a)$$

$$x_1 y_1 x_2 y_2$$

$$Bc = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(1+1)^{2} + (3-1)^{2}}$$

$$= \sqrt{(2)^{2} + (2)^{2}}$$

$$= \sqrt{4+4}$$

$$AB = \sqrt{8} \text{ Units}$$

$$= \sqrt{(3-1)^2 + (a-3)^2}$$

$$= \sqrt{(2)^2 + (a)^2 + (3)^2 - 2(a)(3)}$$

$$= \sqrt{4 + a^2 + 9 - 6a}$$
Bc =  $\sqrt{a^2 - 6a + 13}$  units

Given:

AB = BC

$$\sqrt{8} = \sqrt{a^2 - 6a + 13}$$
 $8 = a^2 - 6a + 13$ 
 $a^2 - 6a + 13 - 8 = 0$ 
 $a^2 - 6a + 5 = 0$ 
 $(a - 1)(a - 5) = 0$ 
 $a - 1 = 0$ 
 $a - 5 = 0$ 
 $a = 1$ 
 $a = 5$ 

8) The abscissa of a point A is equal to its condinate and its distance from the point B (1,3) is 10 units, what one the co-ordinates of A?

Distance = 10 units

$$\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2} = 10$$

$$\sqrt{(1-a)^2 + (3-a)^2} = 10$$

$$\sqrt{(1)^2 + (a)^2 - 2(1)(a) + (3)^2 + (a)^2 - 2(3)(a)} = 10$$

$$\sqrt{1+a^{2}-2a+9+a^{2}-6a} = 10$$

$$\sqrt{2a^{2}-8a+10} = 10$$

$$\sqrt{8}$$

$$\sqrt{2a^{2}-8a+10} = (10)^{2}$$

$$\sqrt{2a^{2}-8a+10} = (10)^{2}$$

$$2a^{2}-8a+10 = 100$$

$$(\div 2) \quad a^{2}-4a+5=50$$

$$a^{2}-4a+5=50=0$$

$$\sqrt{a^{2}-4a-45=0}$$

$$(a+5) (a-9) = 0$$

$$a+5=0 \quad a-9=0$$

$$a+5=0 \quad a-9=0$$

$$a=9$$

$$= A(-5,-5) \quad oA \quad A(9,9)$$

9) The point (x,y) is equidistant from the points (3,+) and (-5,6). Find a selation between x and y.  $(x,y) \Rightarrow \text{equidistant} \Rightarrow (3,+) \text{ and } (-5,6)$  (x,y) (3,+)  $x_1y_1 x_2y_2$ Distance =  $\int (x_2-x_1)^2 + (y_2-y_1)^2$ 

 $= \sqrt{(3-x)^2 + (4-y)^2}$ 

$$(x,y) (-5,b)$$

$$x_1y_1 \quad x_2y_2$$
Distance =  $\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$ 
=  $\sqrt{(-5-x)^2 + (b-y)^2}$ 

Since it is equidistant,
$$\sqrt{(3-x)^2 + (4-y)^2} = \sqrt{(-5-x)^2 + (b-y)^2}$$

$$(3)^2 + (x)^2 - 2(3)(x) + (4)^2 + (y)^2 - 2(4)(y) = (-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (y)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (6)^2 + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x) + (9)^2 - 2(6)(y)$$

$$(-5)^2 + (x)^2 - 2(-5)(x)$$

$$(-5)^2 + (x)^2 - 2$$

10) Let A(213) and B(21-4) be two points. If P lies on the x-axis, such that  $AP = \frac{3}{7}AB$ , find the co-ordinates of P.

=) (Plies on x-axis) =) 
$$P(x,0)$$

$$A(2,3) P(x,0)$$
  
  $x_1 y_1 x_2 y_2$ 

$$AP = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(x-2)^2 + (0-3)^2}$$

$$= \int (x)^{2} + (2)^{2} - 2(x)(2) + (-3)^{2}$$

$$=\int x^2 + 4 - 4x + 9$$

$$AP = \int x^2 - 4x + 13$$

$$AB = \int (\alpha_2 - \alpha_1)^2 + (42 - 41)^2$$

$$= \sqrt{(2-2)^2 + (-4-3)^2}$$

$$= \sqrt{(0)^2 + (-7)^2}$$

$$=\sqrt{(-7)^2}$$

$$\sqrt{x^2 - 4x + 13} = \frac{3}{7}(7)$$

$$\sqrt{x^2 + x + 13} = 3$$

$$(\sqrt{x^2-4x+13})^2=(3)^2$$

$$x^2 - 4x + 13 = 9$$

$$x^2 - 4x + 13 - 9 = 0$$

$$(x-2)(x-2) = 0$$

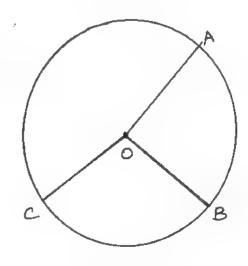
$$x-2=0$$
  $x-2=0$   $x=2$ 

$$\Rightarrow P(x,0) \Rightarrow P(2,0)$$

$$OA = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(1-11)^2 + (2-2)^2}$$

$$= \int (-10)^2 + (0)^2$$



$$0(11,2) \quad B(3,-4) \\ x_1 y_1 \quad x_2 y_2$$

$$0B = \int (x_2-x_1)^2 + (y_2-y_1)^2$$

$$= \int (3-11)^2 + (-4-2)^2$$

$$= \int (-8)^2 + (-6)^2$$

$$= \int 64 + 36$$

$$= \int 100$$

$$= \int (10)^2$$

$$0B = 10 \text{ units}$$

$$0(11,2) \quad B(3,-4) \\ x_1y_1 \quad x_2y_2 \\ 0B = \int (x_2-x_1)^2 + (y_2-y_1)^2 \\ = \int (3-11)^2 + (-4-2)^2 \\ = \int (-8)^2 + (-6)^2 \\ = \int (-6)^2 + (-8)^2 \\ = \int (10)^2 \\ 0B = 10 \text{ units}$$

$$0(11,2) \quad C(5,-6) \\ x_1y_1 \quad x_2y_2 \\ 0C = \int (x_2-x_1)^2 + (y_2-y_1)^2 \\ = \int (5-11)^2 + (-6-2)^2 \\ = \int (-6)^2 + (-6-2)^2 \\ = \int (-6)^2 + (-8)^2 \\ = \int (-6)^2 + (-8)^2 \\ = \int (10)^2 \\ 0B = 10 \text{ units}$$

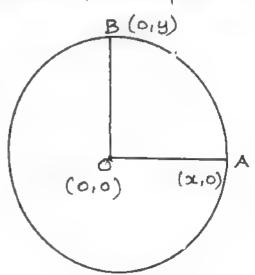
$$0 = \int (10)^2 + (-6)$$

12) The radius of the circle with centre at oxigin is 30 units. Write the co-ordinates of the points where the circle Intersects the axes. Find the distance between any two such points.

Centre => 0 (0,0) = 0 sigin

$$\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2} = 30$$

$$\sqrt{(x-0)^2 + (0-0)^2} = 30$$



=) Distance between two points AB=30/2 units

- joining the points
- (i) (-2,3) and (-6,-5) x, y, x2 42

Midpoint = 
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$= \left(\frac{-2-6}{2}, \frac{3-5}{2}\right)$$

$$= \left(\frac{-8}{2}, \frac{-2}{2}\right)$$

Midpoint = 
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$=\left(\frac{8-8}{2},\frac{-2+0}{2}\right)$$

$$=\left(\begin{array}{ccc} \frac{0}{2} & -\frac{2}{2} \end{array}\right)$$

$$x_1y_1$$
  $x_2$   $y_2$ 

Midpoint = 
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$= \left(\frac{a+a+2b}{2}, \frac{b+2a-b}{2}\right)$$

$$= \left(\frac{2a+2b}{2}, \frac{2a}{2}\right)$$

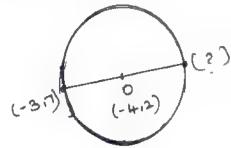
$$= \left(\frac{\chi(a+b)}{\chi}, \frac{\chi a}{\chi}\right)$$
Midpoint =  $(a+b,a)$ 

(iv) 
$$\left(\frac{1}{2}, \frac{3}{7}\right)$$
 and  $\left(\frac{3}{2}, \frac{-11}{7}\right)$   
 $x_1$   $y_1$   $x_2$   $y_2$   
Midpoint =  $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$   
=  $\left(\frac{1}{2} + \frac{3}{2}, \frac{-3}{7}, \frac{-11}{2}\right)$   
=  $\left(\frac{1 + 3}{2}, \frac{-3 - 11}{2}\right)$   
=  $\left(\frac{1 + 3}{2}, \frac{-3 - 11}{2}\right)$   
Midpoint =  $\left(\frac{1 - 1}{2}\right)$ 

2) The centre of a circle is (-4,2). It one end of the diameter of the cincle is (-3,7), then find the other end.

Centre => 0 (-4,12) = midpt One end => (-3,17) Other end => (?)

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Midpoint = 
$$(-4.12)$$
  $(-3.7)$  (?)  
 $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) = (-4.12)$   
 $\left(-\frac{3+x_2}{2}, \frac{7+y_2}{2}\right) = (-4.12)$   
 $-\frac{3+x_2}{2}, \frac{7+y_2}{2} = (-4.12)$   
 $-\frac{3+x_2}{2} = -4$   $\frac{7+y_2}{2} = 2$   
 $-3+x_2 = -8$   $\frac{7+y_2-4}{2}$   
 $x_2=-8+3$   $y_2=4-7$   
 $x_2=-8+3$   $y_2=4-7$   
 $x_2=-3$ 

3) It the midpoint (x,y) of the line joining (3,4) and (P,T) lies on 2x+2y+1=0, then what will be the value of p?

Midpoint = (x,y)

$$\left(\frac{x_1+x_2}{2},\frac{y_1+y_2}{2}\right)=\left(x,y\right)$$

$$\left(\frac{3+P}{2}, \frac{4+7}{2}\right) = (x, y)$$

$$\frac{3+P}{2} = x$$

$$\frac{4+7}{2} = y$$

$$3+p=2x\rightarrow0$$
  $11=2y\rightarrow2$ 

Adding D = 2 3+p+11 = 2x+2y  $\boxed{27}$ 

P+14 = 2x+2y

=) 
$$2x+2y=P+14$$

Given:  $2x+2y+1=0$ 
 $2x+2y=P+14$ 
 $2x+2y=-1$ 
 $(-x)$ 
 $(-x)$ 

4) If the midpoint of the sides of the topiangle are (2,4) (-2,3) and (5,2). Find the co-ordinates of the vertices of the topiangle.

$$\frac{x_1 + x_2}{2} = 2$$

$$\frac{y_1 + y_2}{2} = 4$$

$$\frac{x_1 + x_2 = 4}{2} \rightarrow 0$$

$$\frac{x_2 + x_3}{2} = -2$$

$$\frac{y_2 + y_3}{2} = 3$$

$$\frac{x_2 + x_3 = -4}{2} \rightarrow 3$$

$$\frac{y_1 + y_3}{2} = 6 \rightarrow 4$$

$$\frac{x_1 + x_3}{2} = 5$$

$$\frac{x_1 + x_3}{2} = 5$$

$$\frac{y_1 + y_3}{2} = 2$$

$$\frac{y_1 + y_3}{2} = 4 \rightarrow 6$$

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Adding 1,35 2x,+2x2+2x3=10  $2\left(x_1+x_2+x_3\right)=10$  $x_1 + x_2 + x_3 = \frac{10}{2}$  $x_1 + x_2 + x_3 = 5$  $4 + x_3 = 5$ x3 = 5-4  $(\alpha_3 = 1)$  $x_1 + x_2 + x_3 = 5$ x1+(-4)=5 x,=5+4 2,=9  $x_1 + x_2 + x_3 = 5$ x2+10=5 x2=5-10 (x2=-5)

Adding 1 , 1 , 6 24, +242+243=18 2(41+42+43)=18  $y_1 + y_2 + y_3 = \frac{18}{3}$ y 1+42+43=9 8+43=9 43=9-8 43=1) 91+42+43=9 4,+6=9 4,=9-6 (y,=3) 41+42+43=9 42+4=9 42=9-4 y2=5

5) O(0,0) is the centre of the circle whose one chord is AB, where the Points A and B are (8,6) and (10,0) respectively. OD is the perpendicular

Find the contractes of the midpoint of op.

A(8.6) B(10.0)  

$$x_1y_1$$
  $x_2y_2$   
Midpoint =  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$   
=  $\left(\frac{8+10}{2}, \frac{6+0}{2}\right)$   
=  $\left(\frac{189}{2}, \frac{3}{2}\right)$   
D =  $(9.3)$   
O(0.0) D(9.3)  
 $x_1y_1$   $x_2y_2$   
Midpt =  $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$ 

$$= \left(\frac{9}{2}, \frac{3}{2}\right)$$

$$= \left(\frac{9}{2}, \frac{3}{2}\right)$$

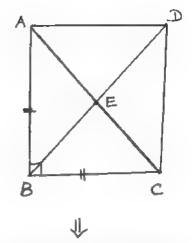
$$= \left(\frac{9}{2}, \frac{3}{2}\right)$$

 $=\left(\frac{0+9}{2},\frac{0+3}{2}\right)$ 

6) The points A(-5.4) B(-1.-2) C(5.2) are the vertices of an 9sosceles right-angled triangle where the right angle is at B, Find the co-ordinates of D so that ABCD is a square.

$$A(-5, +) C(5, 2)$$
  
  $x_1 y_1 x_2 y_2$ 

Midpoint = 
$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$
  
=  $\left(\frac{-5+5}{2}, \frac{++2}{2}\right)$   
=  $\left(\frac{0}{2}, \frac{1}{2}\right)$ 



ABCD Square

$$B(-1,-2) D(?)$$

$$x_1 y_1 x_2 y_2$$

Midpoint = 
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$M \cdot P \cdot O + BD = \left(\frac{-1 + x_2}{2}, -\frac{2 + y_2}{2}\right)$$

Midpt of Ac = Midpt of BD

$$(0,3) = \left(\frac{-1+x_2}{2}, \frac{-2+y_2}{2}\right)$$

$$0 = \frac{-1 + 3C_2}{2}$$

$$0 = -1 + \infty_2$$

$$x_2 = 1$$

$$3 = -\frac{2+y_2}{2}$$

The points A (-3,6) B (0,7) c (1,9) are the midpoints of the sides DE, EF and FD. of the triangle DEF. Show that the quadrilateral ABCD is a Parallelogram.

Midpoint of Ac = Midpoint of BD
$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

$$\left(\frac{-3+1}{2}, \frac{6+9}{2}\right) = \left(\frac{0+x_2}{2}, \frac{7+y_2}{2}\right)$$

$$\left(\frac{-x}{2},\frac{15}{2}\right) = \left(\frac{x_2}{2},\frac{7+y_2}{2}\right)$$

$$\begin{pmatrix} -1, \frac{15}{2} \end{pmatrix} = \begin{pmatrix} \frac{x_2}{2}, \frac{7+4}{2} \end{pmatrix}$$

$$-1 = \frac{\alpha_2}{2}$$

$$-2=x_{2}$$

$$\frac{15}{2} = \frac{7 + 42}{2}$$

$$15 = 7 + 42$$

$$15 = 7 + 42$$

$$15 = 7 + 42$$

8) A (-3,2) B (3,2) and c (-8,-2) one the vertices of the night triangle, night angled at A. Show that the mid-point of the hypotenuse is equidistant

forom the vertices.

$$B(3,2) c(-3,-2)$$
  
 $x_1 y_1 x_2 y_2$ 

$$Midpt = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$=\left(\frac{3-3}{2},\frac{2-2}{2}\right)$$

$$=\left(\frac{0}{2},\frac{0}{2}\right)$$

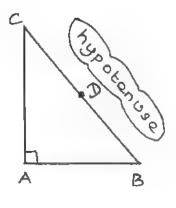
$$AD = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(0+3)^2 + (0-2)^2}$$

$$=\sqrt{(3)^2+(-2)^2}$$

$$CD = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(0+3)^2 + (0+2)^2} = \sqrt{(3)^2 + (2)^2} = \sqrt{9+4} = \sqrt{13}$$
(CD =  $\sqrt{13}$  Units)



$$BD = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(0-3)^2 + (0-2)^2}$$

$$=\sqrt{(-3)^2+(-2)^2}$$

which divides the line segment joining the points A (4,-3) and B (9,7) in the natio 312

2) In what natio does the point P(2,-5) divide the line segment joining A(-3,5) and B(4,-9) P(2,-5) A(-3,5) B(4,-9) Lim?  $P(x,y) = P\left(\frac{1}{2} + mx_1, \frac{1}{2} + my_1, \frac{1}{2} + m\right)$   $P(2,-5) = P\left(\frac{1}{2} + m(-3), \frac{1}{2} + m(5), \frac{1}{2} + m\right)$ 

$$P(2,-5) = P\left(\frac{4l-3m}{l+m}, \frac{-9l+5m}{l+m}\right)$$

$$2 = \frac{4l-3m}{l+m}$$

$$2(l+m) = 4l-3m$$

$$2(l+m) = 4l-3m$$

$$2l+2m = 4l-3m$$

$$2l-4l = -3m-2m$$

$$42l = +5m$$

$$\frac{l}{m} = \frac{5}{2}$$

$$=) P(atio =) 5:2$$

3) Find the Co-obdinates of a Point P on the line segment joining A(1,2)and B(6,1) in such a way that  $AP = \frac{2}{5}AB$  A(1,2) B(6,1) 2:3 2 m A P B A(1,2) B(6,1) 2:3 2 m A P B  $P(x,y) = P(\frac{1}{2}x_2 + mx_1}{1 + m}, \frac{1}{2}y_2 + my_1$  1 + m  $= P(\frac{2(6) + 3(1)}{2 + 3}, \frac{2(1) + 3(2)}{2 + 3})$   $= P(\frac{12 + 3}{5}, \frac{14 + 6}{5})$   $= P(\frac{15}{3}, \frac{26}{5})$ = P(3,4)

4) Find the co-ordinates of the points of trisection of line segment joining the points 
$$A(-5,6)$$
 and  $B(+,-3)$ 

$$= P\left(\frac{1(4)+2(-5)}{1+2}, \frac{1(-3)+2(6)}{1+2}\right)$$

$$= P\left(\frac{4-10}{3}, \frac{-3+12}{3}\right)$$

$$= P\left(\frac{-k^2}{3}, \frac{9}{3}\right)$$

$$Q(x,y) = Q\left(\frac{lx_2+mx_1}{l+m}, \frac{ly_2+my_1}{l+m}\right)$$

$$= Q\left(\frac{2(4)+1(-5)}{2+1}, \frac{2(-3)+1(6)}{2+1}\right)$$

$$= Q\left(\frac{8-5}{3}, -\frac{6+6}{3}\right)$$

$$= Q\left(\frac{3}{3}, \frac{0}{3}\right)$$

5) The line segment joining A (6,3) and B (-1,-4) is doubled in length by adding half of AB to each end. Find the co-ordinates of the new end point.

P A M B Q

(?)

A (6,3) B (-1,-4) M.P

$$x_1 y_1$$
  $x_2 y_2$ 

Midpoint =  $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$ 

=  $\left(\frac{6-1}{2}, \frac{3-4}{2}\right)$ 
 $M = \left(\frac{5}{2}, -\frac{1}{2}\right)$ 

P(?) M  $\left(\frac{5}{2}, -\frac{1}{2}\right)$ 
 $x_1 y_1$   $x_2 y_2$ 

Midpoint  $A = (6,3)$ 
 $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right) = (6,3)$ 
 $\left(\frac{x_1 + 5}{2}, \frac{y_1 - 1}{2}\right) = (6,3)$ 
 $\left(\frac{2x_1 + 5}{2}, \frac{2y_1 - 1}{2}\right) = (6,3)$ 
 $\left(\frac{2x_1 + 5}{4}, \frac{2y_1 - 1}{4}\right) = (6,3)$ 

$$2x_{2} = -9$$

$$2y_{2} = -15$$

$$x_{2} = -\frac{9}{2}$$

$$y_{2} = -\frac{15}{2}$$

$$Q\left(-\frac{9}{2}, -\frac{15}{2}\right)$$

b) Using Section formula, show that the points A(7,-5) B(9,-3) and C(15,1) are Collinear.

$$A(1,-5) B(9,-3)$$

$$x_1 y_1 \qquad x_2 y_2$$

$$AB = \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$

$$= \sqrt{(9-7)^2 + (-3+5)^2}$$

$$= \sqrt{(2)^2 + (2)^2}$$

$$= \sqrt{8}$$
$$= \sqrt{2 \times 2 \times 2}$$

$$A(7,-5) C(13,1)$$
  
 $x_1 y_1 x_2 y_2$ 

$$AC = \int (x_2 - x_1)^2 + (y_2 - y_1)^2$$

$$= \int (13 - 7)^2 + (1 + 5)^2$$

$$= \int (6)^2 + (6)^2$$

$$= \int 36 + 36$$

$$B(9,-3) c(13,1)$$

$$x_1 y_1 x_2 y_2$$

$$Bc = \int (x_2-x_1)^2 + (y_2-y_1)^2$$

$$= \int (13-9)^2 + (1+3)^2$$

$$= \int (4)^2 + (4)^2$$

$$= \int 16+16$$

$$= \int 32$$

$$= \int 2x2x2x2x2$$

$$Bc = 4 \int 2 vnib$$

$$= \sqrt{12}$$

$$= \sqrt{2} \times 2 \times 2 \times 3 \times 3$$

$$= \sqrt{2} \times 2 \times 2 \times 3 \times 3$$

$$= \sqrt{36}$$

$$= \sqrt{18}$$

$$= \sqrt{3}$$

$$=$$

along its length by 25% by paroducing it to c' on the wide B. It x and B have the co-ordinates (-2,-3) (211) respectively, then find the co-ordinates 09'c'?

$$BC = 25 \cdot | AB$$

$$BC = 26 | AB$$

$$| (-2,-3) | (2,1) | (?)$$

$$BC = \frac{1}{4} AB$$

$$BC = \frac{1}{4} AB$$

$$P(x,y) = P\left(\frac{2x_{1} + mx_{1}}{2 + m}, \frac{2y_{2} + my_{1}}{2 + m}\right)$$

$$P(2,1) = P\left(\frac{4(x_{2}) + 1(-2)}{4 + 1}, \frac{4(y_{2}) + 1(-3)}{4 + 1}\right)$$

$$P(2,1) = P\left(\frac{4x_{2} - 2}{5}, \frac{4y_{2} - 3}{5}\right)$$

$$2 = \frac{4x_{2} - 2}{5}$$

$$1 = \frac{4y_{2} - 3}{5}$$

$$10 = 4x_{2} - 2$$

$$10 + 2 = 4x_{2}$$

$$12 = 4x_{2}$$

$$4x_{2} = 12$$

$$4x_{2} = 12$$

$$x_{2} = \frac{12x_{3}}{4}$$

$$x_{2} = 3$$

$$x_{2} = \frac{12x_{3}}{4}$$

$$x_{2} = 3$$

$$x_{2} = \frac{12x_{3}}{4}$$

$$x_{3} = 3$$

$$x_{4} = 3$$

$$x_{2} = 3$$

$$x_{4} = 3$$

$$x_{5} = 4$$

$$x_{7} = 3$$

=) C(3,2)

1) Find the centroid of the taiangle whose vertices are

Contenoid = 
$$\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$
  
=  $\left(\frac{2 - 3 + 7}{3}, \frac{-4 - 7 + 2}{3}\right)$ 

$$= \left(\frac{9-3}{3}, \frac{-11+2}{3}\right)$$
$$= \left(\frac{\cancel{8}}{\cancel{3}}, -\frac{\cancel{3}}{\cancel{3}}\right)$$

(Centroid, G = (2,-3)

(i) 
$$(-5,-5)$$
  $(1,-4)$   $(-4,-2)$   $x_1 y_1 x_2 y_2 x_3 y_3$ 

Contanid = 
$$(x_1 + x_2 + x_3, y_1 + y_2 + y_3)$$

Centroid = 
$$\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$

$$=\left(\frac{-5+1-4}{3},\frac{-5-4-2}{3}\right)$$

$$=\left(\frac{-9+1}{3},\frac{-11}{3}\right)$$

Centroid, 
$$G = \begin{pmatrix} -8 & -11 \\ 3 & 3 \end{pmatrix}$$

2) It the centeroid of a teriangle is at (41-2) and two of its vertices are

$$\left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3}\right) = (4,-2)$$

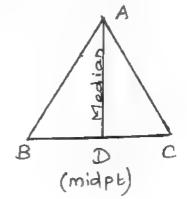
$$\left(\frac{3+5+x_3}{3}, \frac{-2+2+y_3}{3}\right) = (+,-2)$$

$$\left(\frac{8+x_3}{3}, 0+\frac{4}{3}\right) = (4,-2)$$

$$\frac{8+x_3}{3}=4$$

3) Find the length of median through A of a triangle whose vertices are

Midpoint = 
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$



$$= \left(\frac{1+5}{2}, \frac{-1+1}{2}\right)$$

$$= \left(\frac{1+5}{2}, \frac{-1+1}{3}\right)$$

$$D = (3,0)$$

$$A(-1,3) D (3,0)$$

$$x_1 y_1 x_2 y_2$$

$$AD = \int (x_2-x_1)^2 + (y_2-y_1)^2$$

$$= \int (3+1)^2 + (0-3)^2$$

$$= \int (4)^2 + (-3)^2$$

$$= \int 16+9$$

$$= \int 25 = \int (5)^{24}$$

$$= 5 \text{ Unibs}$$

$$=) The length of median AD = 5 \text{ Unibs}$$

H) The ventices of a topiangle are (112)  $(h_1-3)$  and (-4,K). If the centroid of the topiangle is at the point (5,-1) then find the value of  $\sqrt{(h+K)^2+(h+3K)^2}$  (1,2)  $(h_1-3)$  (-4,K)  $x_1y_1$   $x_2y_2$   $x_3y_3$ Centroid = (5,-1)  $\left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3}\right) = (5,-1)$ 

$$\frac{1+h-4}{3}, \frac{2-3+k}{3} = (5,-1)$$

$$\frac{h-3}{3}, \frac{-1+k}{3} = (5,-1)$$

$$\frac{h-3}{3} = 5$$

$$h-3 = 15$$

$$h=15+3$$

$$\frac{1}{1} = 18$$

$$\frac{1}$$

5) Onthocentre and Centroid of a tolongle are A(-3,5) and B(3,3) respectively. It'c' is the cincumcentre and Ac is the diameter of the cincle, then find the nadius of the cincle.

A(-3,5) C(?)

$$P(x,y) = P\left(\frac{1}{2}x_{2} + mx_{1}, \frac{1}{2}y_{2} + my_{1}}{1 + m}\right)$$

$$P(3,3) = P\left(\frac{2}{2}(x_{2}) + 1(-3), \frac{2}{2} + 1\right)$$

$$\frac{2}{2}(y_{2}) + 1(5), A(-3,5)$$

$$\frac{2}{2}(y_{2}) + 1(5), A(-3,5)$$

$$\frac{2}{2}(y_{2}) + 1(5), A(-3,5)$$

$$\frac{2}{3}(y_{2}) + 1(5), A(-3,5)$$

$$\frac{2}{3}(y_{2}) + 1(5), A(-3,5), A(-3,5)$$

$$\frac{2}{3}(y_{2}) + 1(5), A(-3,5), A(-3,5)$$

: Radius of the circle = 3 stounits

6) ABC is a topiangle whose ventices one A(3,4) B(-2,-1) C(5,3). It G is the centroid and BD cG is a parallelogram then find the coordinates of the vartex D.

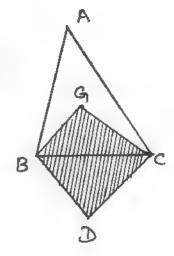
A(3,4) B(-2,-1) c(5,3)  

$$x_1 y_1$$
  $x_2 y_2$   $x_3 y_3$   
Centroid,  $G = \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$   

$$= \left(\frac{3 - 2 + 5}{3}, \frac{4 - 1 + 3}{3}\right)$$

$$= \left(\frac{8 - 2}{3}, \frac{7 - 1}{3}\right)$$

$$= \left(\frac{4}{3}, \frac{4}{3}\right)$$



Bocq is a parallelogram

G = (2,2)

(Diagonals bisect each other)

$$B(-2,-1) C(5,3)$$
  $D(?) G(2,2)$   $x_1 y_1 x_2 y_2$ 

Midpoint of Bc = Midpoint of DG

$$\begin{pmatrix} \frac{\chi_{1} + \chi_{2}}{2}, \frac{y_{1} + y_{2}}{2} \end{pmatrix} = \begin{pmatrix} \frac{\chi_{1} + \chi_{2}}{2}, \frac{y_{1} + y_{2}}{2} \end{pmatrix}$$

$$\begin{pmatrix} -\frac{2+5}{2}, -\frac{1+3}{2} \end{pmatrix} = \begin{pmatrix} \frac{\chi_{1} + 2}{2}, \frac{y_{1} + 2}{2} \end{pmatrix}$$

$$\begin{pmatrix} \frac{3}{2}, \frac{\chi}{2} \end{pmatrix} = \begin{pmatrix} \frac{\chi_{1} + 2}{2}, \frac{y_{1} + 2}{2} \end{pmatrix}$$

$$\left(\frac{3}{2}\right) = \left(\frac{x_1+2}{2} \mid \frac{y_1+2}{2}\right)$$

$$\frac{3}{3^2} = \frac{x_1 + 2}{3^2}$$

$$3 = x_1 + 2$$

$$3 - 2 = 3c_1$$

$$1 = x_1$$

$$x_1 = 1$$

⇒(D(1,0))

The contacted control of the Eriangle obtained by joining the mid-points of the sides of the Eriangle obtained by joining the mid-points of the sides of a total sides of a total sides of a total sides of a total side of the same as the centrold of the original triangle?

$$\left(\frac{3}{2}, 5\right) \left(7, -\frac{9}{2}\right) \left(\frac{13}{2}, -\frac{13}{2}\right)$$
 $x_1 y_1 \quad x_2 y_2 \quad x_3 \quad y_3$ 

Centroid = 
$$\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$

$$= \left(\frac{3}{2} + \frac{7}{3} + \frac{13}{2}, \frac{5 - 9 - \frac{13}{2}}{3}\right)$$

$$= \left(\frac{3+14+13}{2}, \frac{10-9-13}{2}\right)$$

[48]

$$= \frac{30}{6}, \frac{10-22}{6}$$

$$= \frac{30^{5}}{6}, -\frac{12}{6}$$

$$= (5,-2)$$

$$= (5,-2)$$



1) From the given figure, find all the trigonometric ratios or angle B

2) From the given figure, find the values of (i) sinB (ii) secB (iii) cot B (iv) cose (v) tanc (vi) cosec (c

In A ABD,

By Pythagoras

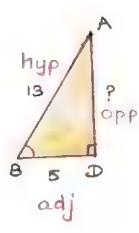
$$AB^2 = AD^2 + BD^2$$

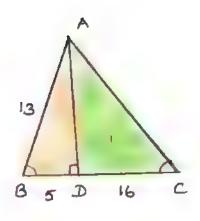
(i) 
$$\sin B = \frac{OPP}{D4P} = \frac{12}{13}$$

In A ADC,

By Pythagoras
Theorem,

$$Ac^2 = AD^2 + Dc^2$$





opp ? nyp

D 16 C

adj

(v) 
$$tanc = \frac{opp}{adj} = \frac{12}{16}$$

3) I7 2 coso = \( \sigma \), then find all the taigonometric ratios of (angle 0)

13

adj

By Pythagoras Theorem,

$$Bc^2 = AB^2 + Ac^2$$

$$2^2 = (\sqrt{3})^2 + Ac^2$$

TRIGONOMETRIC RATIOS:

Sine = 
$$\frac{\text{OPP}}{\text{hyp}} = \frac{1}{2}$$
 $\frac{1}{2}$ 
 $\frac{1}{2}$ 

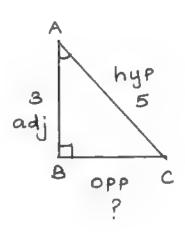
4) It cos A = 3, then find the value of

By Pythagoras Theorem,

$$Ac^{2} = AB^{2} + Bc^{2}$$

$$5^{2} = 3^{2} + Bc^{2}$$

$$9+8c^{2}=25$$
  
 $8c^{2}=25-9$   
 $8c^{2}=16$ 



$$Bc^{2} = 4^{2}$$

$$Bc = 4 \neq (OPP)$$

$$8in A = \frac{OPP}{hyp} = \frac{4}{5}$$

$$=\frac{\frac{4}{5}-\frac{3}{5}}{2\left(\frac{4}{3}\right)}$$

$$=\frac{1}{5} \times \frac{3}{8} = \frac{3}{40}$$

$$\Rightarrow \frac{\sin A - \cos A}{2 \tan A} = \frac{3}{40}$$

5. If 
$$\cos A = \frac{2x}{1+x^2}$$
, then find the value of Sin A and tan A in terms of x.

$$\frac{\cos A = \frac{2x}{1+x^2}}{1+x^2}$$

By Pythagoras Theorem,

$$(Ac)^2 = AB^2 + Bc^2$$

$$(1+x^2)^2 = (2x)^2 + Bc^2$$

$$(1)^{2}+(x^{2})^{2}+2(1)(x^{2})=4x^{2}+Bc^{2}$$

$$1+x^{4}+2x^{2}-4x^{2}=Bc^{2}$$

$$(1-x^2)^{2} = Bc^{2}$$

$$\Rightarrow$$
 SinA = OPP =  $\frac{1-x^2}{1+x^2}$ 

$$\Rightarrow$$
 tan A =  $\frac{OPP}{adj} = \frac{1-x^2}{2x}$ 

6) It sins = 
$$\frac{a}{\sqrt{a^2+b^2}}$$
, then show that

22

adj

1+20

OPP

beine = a coso

$$8in\theta = \frac{a}{\sqrt{a^2 + b^2}} \frac{OPP}{hyp}$$

6

By Pythagoras Theorem,
$$Ac^{2} = AB^{2} + Bc^{2}$$

$$(\sqrt{a^{2}+b^{2}})^{2} = a^{2} + Bc^{2}$$

$$a^{2} + b^{2} = a^{2} + Bc^{2}$$

$$b^{2} = Bc^{2}$$

$$b^{2} = Bc^{2}$$

$$b^{2} = Bc$$

$$Bc = b \iff (adj)$$

$$cos\theta = \frac{adj}{hyp} = \frac{b}{\sqrt{a^{2}+b^{2}}}$$
Show that,

le sine = a coso

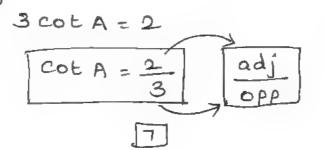
$$le\left(\frac{a}{\sqrt{a^2+b^2}}\right) = a\left(\frac{b}{\sqrt{a^2+b^2}}\right)$$

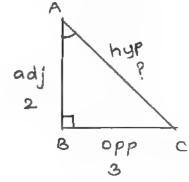
$$\frac{ab}{\sqrt{a^2+b^2}} = \frac{ab}{\sqrt{a^2+b^2}}$$
Hence Veri Fied.

7) If 3 cot A = 2, then find the value of 4 sin A - 3 cos A

2 sin A + 3 cos A

Given





$$= \frac{8(1) - 2(2)}{4(1) + 2(2)}$$

$$\Rightarrow 8 \cos\theta - 2\sin\theta = \frac{1}{2}$$

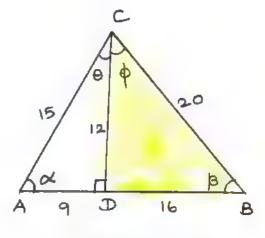
$$+ \cos\theta + 2\sin\theta = \frac{1}{2}$$

9) From the given figure, prove that  $\theta + \phi = 90^{\circ}$ . Also prove that there are two right angled triangles. Find sind, cosp and tand.

By pythagonas Theorem,

$$AB^2 = Ac^2 + Bc^2$$

$$25^2 = 15^2 + 20^2$$

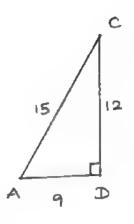


(ii) To parova!

There are two night angled triangle.

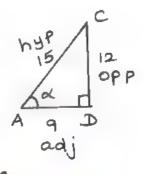
$$Ac^2 = CD^2 + AD^2$$

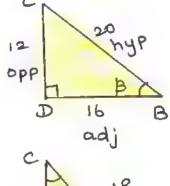
$$15^2 = 12^2 + 9^2$$

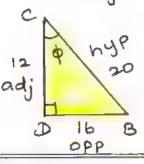


=) Ihere are two right angled triangle.

$$tan \phi = \frac{OPP}{adi} = \frac{16}{12}$$







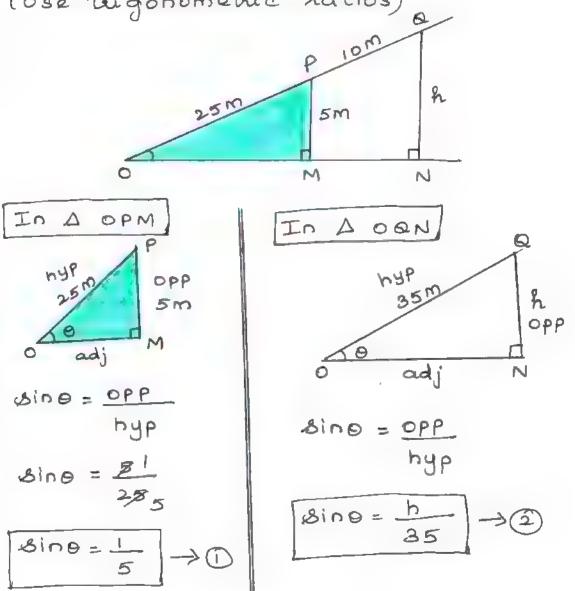
10) A boy standing at a point of finds his kite flying at a point P with distance of = 25 m. It is at a height of 5 m from the ground. When the

thread is extended by 10m from P, it

Reaches a point Q. What will be the

height QN 07 the Kite from the ground?

(Use trigonometric satios)



1) Varity the following equalities:

$$\left(\frac{\sqrt{3}}{2}\right)^2 + \left(\frac{1}{2}\right)^2 = 1$$

Hence Veritied.

$$0 = 1 - 2\left(\frac{1}{\sqrt{2}}\right)^2 = 2\left(\frac{1}{\sqrt{2}}\right)^2 - 1$$

$$0 = 1 - 2 \left( \frac{1}{2} \right) = 2 \left( \frac{1}{34} \right) - 1$$

Hence Veritied.

$$1 + \left(\frac{1}{\sqrt{3}}\right)^2 = \left(\frac{2}{\sqrt{3}}\right)^2$$

$$\frac{3+1}{3} = \frac{4}{3}$$

$$\frac{4}{3} = \frac{4}{3}$$

Hence Veritied.

(iv) 9in 30 cos 60 + cos 30° ∈ 60° = 3in 90°   

$$\left(\frac{1}{2} \times \frac{1}{2}\right) + \left(\frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{2}\right) = 1$$
 $\frac{1}{4} + \frac{3}{4} = 1$ 
 $\frac{1+3}{4} = 1$ 
Hence Venitied.

(i) 
$$\frac{\tan 45}{\cos 20} + \frac{\sec 60}{\cot 45} - \frac{5\sin 90}{2\cos 0}$$
  
 $= \frac{1}{2} + \frac{2}{1} - \frac{5(1)}{2(1)}$   
 $= \frac{1}{2} + \frac{2\times 2}{1\times 2} - \frac{5}{2}$ 

$$=\frac{1+4-5}{2}=\frac{5-5}{2}=\frac{0}{2}=0$$

(ii) 
$$(\sin 90 + \cos 60 + \cos 45) \times (\sin 30 + \cos 60)$$
  

$$= (1 + \frac{1}{2} + \frac{1}{\sqrt{2}}) \times (\frac{1}{2} + \frac{1}{\sqrt{2}})$$

$$= (\frac{2+1}{2} + \frac{1}{\sqrt{2}}) \times (\frac{1+2}{2} - \frac{1}{\sqrt{2}})$$

$$= (\frac{2+1}{2} + \frac{1}{\sqrt{2}}) \times (\frac{1+2}{2} - \frac{1}{\sqrt{2}})$$

$$= \left(\frac{3}{2} + \frac{1}{\sqrt{2}}\right) \times \left(\frac{3}{2} - \frac{1}{\sqrt{2}}\right)$$

$$\left(a + h\right) \times \left(\frac{3}{2} - \frac{1}{\sqrt{2}}\right)$$

$$= \left(\frac{3}{2}\right)^{2} - \left(\frac{1}{\sqrt{2}}\right)^{2} \qquad \left[(a+b)(a-b) = a^{2} - b^{2}\right]$$

$$= \frac{9}{4} - \frac{1 \times 2}{2 \times 2}$$

$$= \frac{9-2}{4} = \boxed{\frac{1}{4}}$$

(iii) 
$$3in^{2}30 - 2\cos^{3}60 + 3\tan^{4}45$$
  

$$= \left(\frac{1}{2}\right)^{2} - 2\left(\frac{1}{2}\right)^{3} + 3\left(1\right)^{4}$$

$$= \frac{1}{4} - 2\left(\frac{1}{4}\right) + 3\left(1\right)$$

$$= \frac{1}{4} - \frac{1}{4} + 3$$

$$= \boxed{3}$$

3) Verity 
$$\cos 3A = 4\cos^3 A - 3\cos A$$
 when  $A = 30$ 

$$\cos 90^{\circ} = 4 \left( \frac{\sqrt{3}}{2} \right)^{3} - 3 \left( \frac{\sqrt{3}}{2} \right)$$

$$0 = 4\left(\frac{3\sqrt{3}}{8}\right) - \frac{3\sqrt{3}}{2}$$

$$0 = \frac{3\sqrt{3}}{2} - \frac{3\sqrt{3}}{2}$$

$$\sqrt{3} \times \sqrt{3} \times \sqrt{3}$$

$$= 3 \times \sqrt{3}$$

$$= 3 \sqrt{3}$$

0=0

Hence Varitied.

H) Find the value of  $8 \sin 2x \cos 4x \sin 6x$ , when x=15

8 sin 2x cos 4x sin 6x

= 8 8in 30° Cos 60° sin 90°

$$= 8 \times \frac{1}{2} \times \frac{1}{2} \times 1$$

I find the value of the following:

(i) 
$$\left(\frac{\cos 47^{\circ}}{\sin 43^{\circ}}\right)^{2} + \left(\frac{\sin 72^{\circ}}{\cos 18^{\circ}}\right)^{2} - 2\cos^{2} 45^{\circ}$$

$$= \left[\frac{\cos(90-43)}{\sin 43^{\circ}}\right]^{2} + \left[\frac{\sin(90-18)}{\cos 18^{\circ}}\right]^{2} - 2\left(\frac{1}{\sqrt{2}}\right)^{2}$$

$$= \left[\frac{81943}{81943}\right]^{2} + \left[\frac{\cos 18}{\cos 18}\right]^{2} - \gamma\left(\frac{1}{2}\right)$$

$$=(1)^2+(1)^2-1$$

(ii) 
$$\frac{\cos 70}{\sin 20} + \frac{\cos 59}{\sin 31} + \frac{\cos 9}{\sin (90-9)} - 8\cos^2 60$$

$$= \frac{\cos(90-20)}{\sin 20} + \frac{\cos(90-31)}{\sin 31} + \frac{\cos \theta}{\cos \theta} - 8\left(\frac{1}{2}\right)^{2}$$

$$= \frac{8in/20}{8in/80} + \frac{8in/3i}{8in/8i} + \frac{cos6}{cos6} - \frac{2}{8}(\frac{1}{4})$$

$$(iv)$$
  $cole + cos(90-0) tane sec(90-0) 
 $tan(90-0) + sin(90-0) col(90-0) cosec(90-0)$$ 

$$= 1 + \begin{bmatrix} 8in\theta \times \frac{1}{8in\theta} \\ \cos \theta \times \frac{1}{\cos \theta} \end{bmatrix}$$

$$= 1 + \left(\frac{1}{1}\right)$$

- 1) find the value of the following:
- (i) Sin 49 = 0.7547
- (11) Cos 74° 39'

- 0,2648
- =) (cos 74 39 = 0, 2648)

$$(m, D) \qquad 2' = \frac{17}{(+)}$$

$$(m \cdot D) \quad 3' = 8 \quad (+)$$

$$(m.D)$$
  $5' = 8 (-)$ 

$$tan 70 12 = 2.7776$$
  
 $(m.D) 5' = \frac{131}{2.7907}$ 

$$\sin 8554 = 0.9974$$
 $(m.D) 3 = 1 (+)$ 

$$(m.D)$$
 3' = \_\_\_\_\_\_\_6 (-)

$$(m.D)$$
  $1' = 3(+)$ 

$$(m.D)$$
  $3^{1} = 9(-)$ 

COS 15 24 = 0,9641

$$5' = 2 (4)$$
 $8in 54' 59' = 0.9962$ 

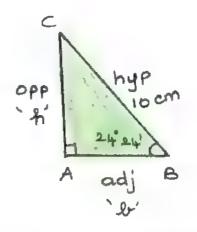
4) Find the area of a right triangle whose hypotenuse is 10cm and one of the acute angle is 24°24'

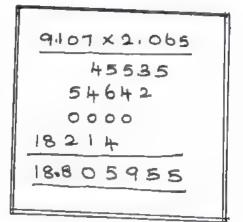
=) Area of a tollangle = 
$$\frac{1}{2} \times b \times h$$

$$= \frac{1}{2} \times 9.107 \times \frac{1}{4.131}$$

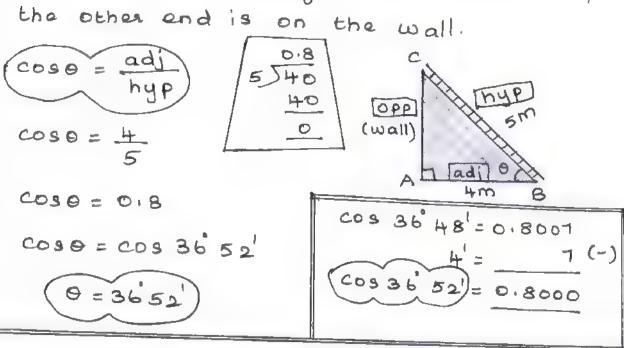
$$= 9.107 \times 2.065$$

$$= 18.805955$$
 $= (18.81 \text{ cm}^2)$ 

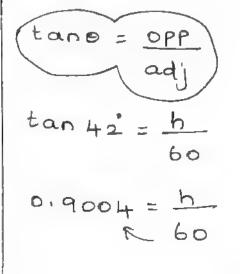


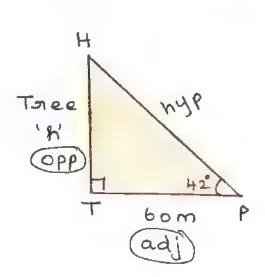


5) Find the angle made by a Ladder of length 5m with the ground. It one of its end is 4m away from the wall and the other end is on the wall



6) In the given figure, HT whows the height of a tree standing vertically. From a point P, the angle of elevation of the top of the tree (that is LP) measures 42 and the distance to the tree is 60 metres. Find the height of the tree.





 $0.9004 \times 60 = h$  54.0240 = hh = 54.0240 m

=) The height of the tree is 54.02 m



1. Heron's Formula

Area of triangle = \( S(S-9) (S-6) (S-6) (S-6) \( S-6) \)

S= a+b+c [sis Semi-perimeter]

Area of equilateral triangle = 18 a2 squoits

Area of triangle (bth) = 1 bxh sq. units

Exercise - 7.1

1. Using Heron's Formula, find the area of a triangle whose sides are
(1) 10cm, 24cm, 26cm.

 $\frac{Sol}{0} = 0 = 10 \text{ cm}$  0 = 24 cm 0 = 26 cm

$$S = \frac{a+b+c}{2}$$

$$= \frac{10+24+2b}{2}$$

$$= \frac{60}{2}$$

$$S = 30cm$$

$$A = \sqrt{S(s-a)(s-b)(s-c)}$$

$$= \sqrt{30(30-10)(30-24)(30-26)}$$

$$= \sqrt{30(20)(6)(4)}$$

$$= \sqrt{6 \times 5 \times 4 \times 5 \times 6 \times 4}$$

$$= 6 \times 5 \times 4$$

(ii) 1.8m, 8m, 8.2m
$$Sol: \alpha = 1.8m$$

$$b = 8m$$

$$C = 8.2m$$

$$S = \frac{1.8}{2} + \frac{8.0}{8.2}$$

$$= \frac{1.8 + 8 + 8.2}{2} = \frac{18.0}{18.0}$$

$$= \frac{18.0}{2} = \frac{9.0}{7.2}$$

$$A = \sqrt{S(S-a)(S-b)(S-c)} = \sqrt{9.0}$$

$$= \sqrt{9(9-1.8)(9-8)(9-8.2)}$$

$$= \sqrt{7.2 \times 7.2}$$

$$A = 7.2 \text{ m}^2$$
The Sides of the triangular ground

2) The Sides of the triangular ground are 22m, 120m, and 122m. Find the area and cost of levelling the ground at the rate of \$\frac{7}{20} per m^2.

$$Sol! - Q = 22m$$
 $b = 120m$ 
 $C = 122m$ 

$$S = \frac{a+b+c}{2}$$

$$= \frac{22+|20+|22}{2}$$

$$= \frac{264}{|32}$$

$$S = \frac{132m}{2}$$

$$A = \sqrt{S(8-a)(s-b)(s-c)}$$

$$= \sqrt{|32(|32-22)(|32-|20)(|32-|22)}$$

$$= \sqrt{|32\times|10\times|2\times|0}$$

$$= \sqrt{|32\times|10\times|2\times|0}$$

$$= \sqrt{|2\times|1\times|10\times|2\times|0}$$

$$= \sqrt{|2\times|1\times|0}$$

$$= \sqrt{$$

-. Cost of levelling 1320m2 = 1320 x20 二 至26,400

3) The perimeter of a triangular plot is 600m. If the Sides are in the ratio 5:12:13, then find the area of the Plot.

Sol: -

$$5x + 12x + 13x = 600$$

$$x = \frac{36}{96}$$

$$C = 13x = 13(20) = 260 \text{ m}$$

$$S = a+b+c$$

$$S = 300 \, \text{m}$$

$$A = \sqrt{S(S-a)(S-b)(S-c)}$$

$$= \sqrt{300(300-100)(300-240)(300-260)}$$

$$= \sqrt{300 \times 200 \times 60 \times 40}$$

$$= \sqrt{3\times100 \times 2\times100 \times 2\times3\times10 \times 2\times2\times10}$$

$$= 3\times2\times2\times100\times10$$

$$A = 12000 \, \text{m}^2$$
Find the area of an equilatival triangle whose perimeter is 180cm.

4) Find the area of an equilateral trangle whose perimeter is 180cm.

Sol :-Equilateral triangle

> Perimeter = 180 cm 3a = 180

3 sides equal

a = 60 cm

6

Area = 
$$\frac{\sqrt{3}}{4} a^2$$
  
=  $\frac{\sqrt{3}}{4} \times (60)^2$   
=  $\frac{\sqrt{3}}{4} \times 60 \times 60$   
A =  $\frac{900 \sqrt{3} \text{ cm}^2}{(07)}$   
=  $\frac{900 \times 1.732}{4}$   
A =  $\frac{1558.800 \text{ cm}^2}{4}$ 

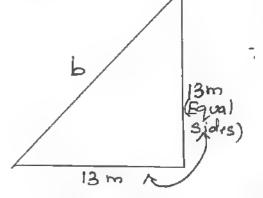
300

V8=1.732

form of an isosceles triangle with perimeter 36m and each of the equal Sides are 13m. Find the cost of painting it at \$\frac{1}{2}\$ 17.50 per Square metre.

Sol: - Isosceles Triangle.

Perimeter = 36m 13+13+b = 36 26+b = 36 b = 36-26 b = 10m



$$S = a+b+c$$

$$= \frac{13+13+10}{2}$$

$$= \frac{36}{22},$$
 $S = 18 \text{ m}$ 

$$A = \sqrt{S(S-a)(S-b)(S-c)}$$

$$= \sqrt{18(18-13)(18-13)(18-10)}$$

$$= \sqrt{18\times5\times.5\times8}$$

$$= \sqrt{12\times12\times5\times5}$$

$$= \sqrt{12\times12\times5\times5}$$

$$= 12\times5$$

$$A = 60 \text{ m}^2$$
Cost of painting per sq m =  $\overline{E}$ 17.50
$$\therefore \text{ cost of painting } 60 \text{ m}^2 = 60 \times 17.50$$

$$= \overline{E}$$
1050.0

6 Find the area of the Unshaded

6 find the area of the Unshaded region.

Sol:-

In 
$$\triangle^{l} ABD$$

Using Pythagoras theorem

 $AB^{2} = AD^{2} + BD^{2}$ 
 $= 12^{2} + 16^{2}$ 
 $= 144 + 256$ 
 $AB^{2} = 400$ 
 $AB^{2} = 100$ 

h = 16cm

$$AB^2 = 400$$

$$AB = \sqrt{400}$$

Area of 
$$\Delta''$$
 ABD =  $\frac{1}{2} \times b \times b$ 

$$= \frac{1}{2} \times 12 \times 16$$

$$A = 96 \text{ cm}^2$$

$$= 34+42+20$$

$$S = 48 cm$$

$$A = \sqrt{S(S-a)(S-b)(S-c)}$$

$$= \sqrt{48(48-34)(48-42)(48-20)}$$

$$= \sqrt{48 \times 14 \times 6 \times 28}$$

$$= \sqrt{6 \times 8 \times 7 \times 2 \times 6 \times 7 \times 4}$$

$$= \sqrt{6 \times 6 \times 7 \times 7 \times 8 \times 8}$$

$$= 6 \times 7 \times 8$$

$$A = 336 cm^{2}$$

$$\therefore Area of Unshaded region = Area of Area o$$

D Find the area of a guadrilateral ABCD whose Sides are AB= 13cm, BC = 12 cm, CD = 9cm, AD = 14cm and diagonal BD = 15 cm. Sol: 14cm D'e ABD a = 13 cm, b = 14 cm, C=150 S= a+b+c = 13+14+15 = 42 S = 21 cm A = |S(s-a)(s-b)(s-c)|= /21 (21-13) (21-14) (21-15) = 21×8×7×6 = \7x3 x 4x2 x 7x 3x2 = 7×3×2×2 A = 84cm2

9 cm c 12cm 13cm D'e BDC a= 12cm, b=9cm, c= 15cm S= a+b+c = 12+9+15 = 36 18 S= 18cm A= (S(s-a)(s-b)(s-c) =[18(18-12)(18-9)(18-15) = 18×6×9×3 = 118 × 18 × 3×3 = 18×3 A = 54 cm2

Area of quadrilateral = Area of De ABD

Area of De BDC

(8) A park is in the Shape of a quadrilateral. The Sides of the park are 15m, 20m, 26m and 17m and the angle between the first two Sides is a right angle. Find the area of the

Park.

Using Pythagoras theo

$$Ac^{2} = AB^{2} + Bc^{2}$$
$$= 15^{2} + 20^{2}$$
$$= 225 + 400$$

$$Ac^{2} = 625$$
 $Ac = \sqrt{625}$ 
 $Ac = 25 m$ 

Area of 
$$\Delta^{1}e^{ABC} = \frac{1}{2}b \times b$$

$$= \frac{1}{2} \times 15 \times 2^{10}$$

$$A = 150m^{2}$$

$$A = 17m \quad b = 26m \quad C = 25m$$

$$A = \sqrt{S(S-a)(S-b)(S-c)}$$

$$S = 17 + 26 + 25$$

$$= \frac{17 + 26 + 25}{2}$$

$$= \frac{17 \times 2 \times 17 \times 2 \times 4 \times 3 \times 3}{2 \times 4 \times 3 \times 3}$$

$$= \frac{17 \times 2 \times 3 \times 2}{4 \times 204 \times 3 \times 2}$$

$$= \frac{17 \times 2 \times 3 \times 2}{4 \times 204 \times 3 \times 3}$$

: Area of quadrilateral = Area of 1'e ABC Area of D'e ACD = 150+204 Area of quadrilateral = 354 m2 (9) A land is in the Shape of shombus. The perimeter of the land is 160m and one of the diagonal is 48m. Find q-the land. the area Rhombus Perimeter = 160m Ha = 160 a = 4000 Area of shombus = 2 Area of D In D' ABC a = 40m, b = 40m c = 48m

(14)

$$S = \frac{a+b+c}{2}$$

$$= \frac{40+40+48}{2}$$

$$= \frac{1286+6}{2}$$

$$S = \frac{64m}{2}$$

$$A = \int S(S-a)(S-b)(S-c)$$

$$= \int \frac{64(64-40)(64-40)(64-48)}{64\times24\times24\times16}$$

$$= \int \frac{8\times8}{2} \times \frac{24\times24}{4}$$

$$= \frac{8\times24\times4}{4}$$

$$A = \frac{768m^2}{4}$$

-. Area of shombus = 2 x 768 = 1536 m<sup>2</sup>

(10) The adjacent Sides of a parallelogram measures 34m, 20m and the measure of one of the diagonal is 42m. Find the area of Parallelogram.

Sol! -Parallelogram Area of Parallelogram = 20 m 2 (Area of D'ABC) De ABC a = 34m, b=20m, c=42m S= a+ b+c = 34+20+42 = 96 48 S = 48m Area of D'e ABC = S(S-a) (S-b) (S-C) A = 48(48-34)(48-20)(48-42) = 148x14x28x6 = V 6x4x2 x 7x2 x7x4 x6

42 ×8 336

: Area of Parallelogram = 2(336)
= 672 m²

## Surface Area of Cuboid and Cube

Shape	Lateral Surface area LSA	Total Surface area TSA
Cuboid	2h(l+b)	2(1b+bh+h1)
Cube	4a2	6 a2



(1) Find the Total Surface Area and the Lateral Surface Area of a cuboid whose dimensions are length = 20cm, breadth = 15cm and height = 8cm

Sol:- l = 20cm b = 15cm h = 8cm

$$TSA = 2(1b+bh+hl)$$

$$= 2[(20x15)+(15x8)+(8x20)]$$

$$= 2[300+120+160]$$

$$= 2[580]$$

$$TSA = 1160 cm2$$

$$LSA = 2h(1+b)$$

$$= 2x8(20+15)$$

$$= 16 \times 35$$

$$= 16 \times 35$$

$$= 560 cm2$$

2) The dimensions of a cuboidal box are 6m × 400 cm × 1.5 m. Find the cost of painting its entire Outer Surface at the rate of \$\mu = 22 per ms^2.

$$l = 6m$$
 $b = 400 cm = \frac{400}{100} = 4m$ 
 $h = 1.5m$ 

The dimension of a hall is 10m x 9m x 8m.

Find the cost of while washing the walls

and ceiling at the rate of \$\frac{1}{2}\$ 8.50 per m.

Sol l = 10m

b = 9m

ceiling = Area of

Rectangle

h = 8m

Area to be White Washed = LSA + Area of Rectangle

$$= 3h(1+b) + (1\times b)$$

$$= 2\times 8(10+9) + (10\times 9)$$

$$= 16(19) + 90$$

$$= 304 + 90$$

$$= 304 + 90$$

$$= 304 + 90$$

$$= 394 m^{2}$$

$$= 334900$$

$$= 304 + 90$$

$$= 304 + 90$$

$$= 394 m^{2}$$

$$= 334900$$

$$= 394 m^{2}$$

$$= 394 m^{2} = 394 m^{$$

(20)

(5) If the total Surface area of the Ceebe is 2400 cm2. then find its lateral Surface area.

Sol:

Cube

TSA = 2400 Cm2

 $6a^2 = 2400$ 

a = 2400 400

a = 400

. LSA = 4a2

= 4(400)

LSA = 1600 cm2

(6) A Cubical Container Of Side 6.5 m is to be painted on the entere Outer Surface. Find the area to be painted and the total cost of painting it at the rate of 7 24 per m2 So):-

Cube

a = 6.5m

$$TSA = 6a^{2}$$

$$= 6(6.5)^{2}$$

$$= 6 \times 42.25$$

$$TSA = 253.50 \text{ m}^{2}$$

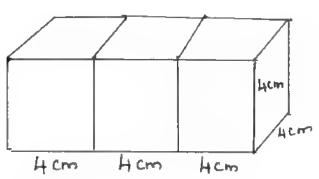
Cost of painting Per sqm = \$24

: Cost of painting 253.50 m2 = 253.50 x24

= \$\frac{2}{2}\$ 6084.0

Three identical cubes of Side 4cm are joined end to end. Find the total Surface area and lateral Surface area and lateral Surface area of the new resulting cuboid.

Sol: -



$$TSA = 2(lb+bh+hl)$$

$$= 2[(l2x+)+(4x+)+(4x+2)]$$

$$= 2[48+1b+48]$$

$$= 2x | 12$$

$$TSA = 224 cm2$$

$$LSA = 2h(1+b)$$
  
=  $2x4(12+4)$   
=  $8x16$   
 $LSA = 128cm^{2}$ 

lolume

Shape	Volume
Cuboid	lbh
Cube	аз



- Thind the Volume of a cuboid whose dimensions are.
- (i) length = 12 cm, breadth = 8cm, height = 6cm (ii) length = 60 m, breadth = 25 m, height = 1.5 m Sol! - Ceeboid

(1) 
$$l = 12 cm$$
  
 $b = 8 cm$   
 $h = 6 cm$   
 $V = 12 k$ 

2) The dimensions of a match box are 6cm × 3.5 cm × 2.5 cm. Find the Volume of packet containing 12
Such match boxes.

Cuboid

l = 6cm b = 3.5cm h = 2.5cm



Volume of 1 match box = 16h = 6×3.5×2.5 = 5250cm3 \_ . Volume of 12 match box = 12x 5250  $= 630 \, \text{cm}^3$ (3) The length, breadth and height of a chocolate box are in the ratio 5:4:3. If its Volume is 7500 cm3, then find its dimensions. Cuboid l = 5x 0=4x h = 3x V = 7500 cm3 16h = 7500 (5x)(4x)(3x)=7500 60x3 = 7500

$$\chi^3 = 125$$
 $\chi^3 = 5^3$ 
 $\chi = 5$ 

(4) The length, breadth and depth of a pond are 20.5 m, 16m, 8m respectively. Find the capacity of the pond in litres.

Sol! -

l = 20.5m b = 16 m h = 8 m

Capacity = Volume = 1 bh

20.5 × 16 12.30 20.5 328.0 × 8 2624.0

Volume= 2624 m3

2624m3 = 2624×1000 litres

(5) The dimensions of a brick are 24cmx12cmx8cm. How many Such bricks will be required to build a wall of 20m length, 48cm breadth, and 6m height? (Mall) 1 = 20m => 20×100 = 2000 cm 1 = 24 cm b = 48cm D = 12 cm h = 6 m => 6x100 = 600 cm h = 8cm Y = lbh V = lbb V = 2000 × 48 × 600 V = 24×12×8

: No of bricks = Vol of Wall

Vol of Brick

2000 × 48 × 600

= 24 × 1× × 8

12 × × 8

= 1000 X25

No 9 bricks = 25000

6) The Volume of a Container 15 1440m? The length and breadth of the container are 15m and 8m respectively. Find ils height (Cuboid) Sol: 1= 15m V = 1440m3 lbb= 1440 15×8×h= 1440 p = 12×8, h = 12 m (1) Find the Volume of a cube each of whose side is (i) 5 cm (ii) 3.5 m

(111) 21 cm

$$V = a^3$$

$$V = a^3$$

$$= (3.5)^3$$

$$V = a^3$$

$$=(21)^3$$

8) A cubical milk tank can hold

125000 litres of milk. Find the length of ils side in metres.

<u>Sol:</u>-

Eube

Capacity = Volume = 125000 litres

V= 125000 litres

125000 litres = 125006

125000 litre= 125m3

. V=125 m3

a3= 125

 $a^3 = 5^3$ 

1. a= 5m

- ' Side = 5m

A metallic cube with Side 15 cm is melted and formed into a cuboid.

If the length and height of the cuboid is 25 cm and 9cm respectively then find the breadth of the cuboid.

Sol: - Cube

a = 15 cm

 $V = \alpha^3$ 

V=(15)3

Cuboid

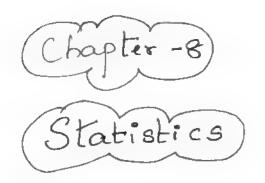
1 = 25 cm

h = 9 cm

b= ?

V= 1xbxh V= 25 x 9 x b

(30)



## Arithmetic Mean

\* Raw Data

Number of Observation

\* Assumed Mean Method

$$\overline{X} = A + \leq fd$$
 $\leq f$ 

A is Assumed mean.

\* Step deviation
$$\overline{X} = A + \left(\frac{2+d}{5}\right) \times C$$

Exercise - 811

DIn a Week, temperature of a Certain place is measured during winter are as follows 26c, 24c, 28c, 3ic, 3oc, 26c, 24c. Find the mean temperature of the Week.

Sol: 26c, 24c, 28c, 3ic, 3oc, 26c, 24c

 $X = \frac{2x}{n} = \frac{26 + 24 + 28 + 31 + 30 + 26 + 24}{7}$ 

$$= \frac{189^{27}}{X} = 27c$$

2) The mean weight of 4 members of a family is 60 kg. Three of them have the weight 56kg, 68kg, and 72kg respectively. Find the weight of the fourth member. Sol: -Meight of 3 members = 56kg, 68kg 472ka. 4 72kg. Let the weight of ] = A Mean Weight of } = 60 kg Ex = 60

 $\frac{56+68+72+A}{4}=60$ 

(3)

$$\frac{196 + A}{4} = \frac{60}{4}$$

$$\frac{196 + A}{4} = \frac{240}{4}$$

$$A = \frac{240 - 196}{4}$$

$$A = \frac{44 + 4}{4}$$

$$A = \frac{4$$

3) In a class test in mathematics,
10 Students Scored 75 marks, 12
Students Scored 60 marks, 8 students
Scored 40 marks and 3 Students
Scored 30 marks. Find the mean
of their Score.

Sol: -

Number of Students => n = 10+12+8+3

Mark Scored by 10 Students = 10x75 = 750

Mark Scored by 12 Students = 12 × 60 = 720 Mark Scored by 8 students = 8 x 40 = 320 Mark Scored by 3 Students = 3 × 30 = 90 \_\_. Total marks Scored }=750+720+320+96
by 33 Students : \ \ \ \ \ \ = 1880 Mean = Ex 56.96 33)1880 X = 1880 -165 230 X = 56.96X = 57 (4) In a research Laboratory Scientists

H) In a research Laboratory Scientist treated 6 mice with lung Cancer using natural medicine. Ten days

later, they measured the Volume of the tumor in each mouse and given the results in the table.

Mouse Marking	1	2.	3	4	5	6
Tumor Volume (mm3)	145	148	142	141	139	140

Find the mean.

Marks	10	15	20	25	30
No of Students	6	8	P	10	6

Sol: -

Mean = 20.2

Marks	NS of dents	fx	
, 10	6	60	
15	8	120	
20	Р	20P	
25	10	250	
30	6	160	
TOTAL	30+P	610+20p	

$$\frac{2fx}{2f} = 20.2$$

$$610 + 20p = 20.2 (30 + p)$$

$$610 + 20p = 606.0 + 20.2 p$$

$$610 - 606 = 20.2 p - 20 p$$

$$4 = 0.2 p$$

$$\Rightarrow 0.2 p = 4$$

$$P = \frac{4}{0.2} \times \frac{10}{10}$$

$$= \frac{40}{2}$$

$$\therefore P = 20$$

6) In the class, weight of Students is measured for class records.
Calculate mean weight of the class Students Using direct Method.

Weight (kg)	15-25	25-35	35-45	45-55	55-65	65-75
40. State	4	11	19	14	0	2

S	<u> </u>  -	d)	1	ıl f	•
	C.I	2	f	fx	
	15-25	2.0	4	80	
	25-35	30	13	330	
	35-45	40	19	760	-
	45 - 55	50	14	700	•
	55 - 65	60	0	0	
	65 - 75	70	2	140	
	Total		50	20 0	

$$\begin{array}{rcl}
\overline{X} &=& \underline{5}fx \\
& \underline{5}f \\
& = & \underline{2010} \\
\hline
5 & \underline{5} & \underline{5} \\
\hline
X &=& \underline{40.2}
\end{array}$$

To Calculate the mean of the following distribution Using Assumed Mean Method.

Sol:-				, 1
C.I	x	f	A = 25 d=x-A	fd
0-10	5	5	5-25= -20	-100
10-20	15	7	15-25 = - 10	-70
20-30	A 25.	15	25 - 25 = 0	0
30-40	35	28	35-25 = 10	280
40-50	45	8	45-25= 20	160
Total.		63		270

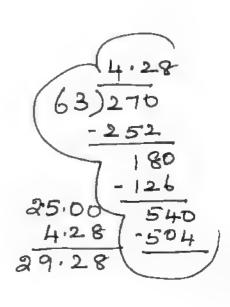
Assumed Mean

$$X = A + \frac{5}{2}fd$$

$$= 25 + \frac{270}{63}$$

$$= 25 + 4.28$$

× = 29.28



8) Find the Anthometic Mean of the following data using Step Deviation Method:

Age	15-19	20-24	25-29	30 - 34	35-39	40-44
No of Persons	4	20	38	24	10	9

Sol : -

C.I	x	ţ	$A = 3^{2}$ $C = 5$ $d = \chi - A$	fd
14.5 - 19.5	17	4	$\frac{17-32}{5} = -3$	-12
19.5 - 24.5	22	20	$\frac{22 - 32}{5} = \frac{-10}{5} = -2$	-40
24.5 - 29.5	27	38	27-32 = -5 = -1	-38
29:5-34:5	32	24	32-32 _ 0	0
34.5-39.5	37	10	37-32 = 5 = 1	10
39.5-44.5	42	9	$\frac{42-32}{5} = \frac{10}{5} = 2$	18
Total.		105		-62

$$\bar{x} = 29.05$$

Median

\* When Nis odd

Median = 
$$\left(\frac{N+1}{2}\right)^{th}$$
 observation

+ when Nis even

Median = 
$$\left(\frac{N}{2}\right)$$
 observation +  $\left(\frac{N}{2}+1\right)$  observation

\* Grouped Frequency Distribution

Median =  $1 + (\frac{N}{2} - rn) \times c$ 

l = lower limit of the median class

N = Total frequency (Ef)

class, preceeding the median class.

C = Width of the median class

f = Highest frequency of median Class.



P Find the median of the given Value: -47, 58, 62, 71, 83, 21, 43, 47, 41 Sol: -

Arranging in ascending order.

21, 41, 43, 47, 47, 53, 62, 71, 83

N=9 => odd.

· Median = (N+1) th term

= (9+1)th term

= (10)th term

= 5th term

- Median = 47

2) Find the Median of the given data 36, 44, 86, 31, 37, 44, 86, 35, 60, 51

Sol: - Arranging is Ascending Order.

31, 35, 36, 37, 44, 44, 51, 60, 86, 86

N=10 => even

(14)

The median of Observation 11, 12, 14, 18, x+2, x+4, 30, 32, 35, 41 arranged in ascending Order is 24. Find the Values of x.

Sol  
11, 12, 14, 18, 
$$x+2$$
,  $x+4$ , 30, 32, 35, 41  
 $N=10 \Rightarrow even$ .  
Median = 24  
 $(\frac{N}{2})$  the term = 24  
 $(\frac{10}{2})$  the term = 24 ×2  
 $(\frac{10}{2})$  the term = 48  
 $(\frac{10}{2})$  the term = 48

$$\frac{\chi}{2} = \frac{42}{2}$$

A researcher Studying the behaviour of mice has recorded the time (in Seconds) taken by each mouse to locate its tood by considering 13 different mice as 31,33,63,33,28,29, 33,27,27,34,35,28,32. Find the median time that mice spent in Searching its food.

Arrange in Ascending Order.

27, 27, 28, 28, 29, 31, 32, 33, 33, 34, 35, 63

N= 13

 $Median = \left(\frac{N+1}{2}\right)^{th}$  [error

 $= \left(\frac{13+1}{2}\right)^{\frac{1}{13}} \text{ term}$ 

= (14) therm

- : Median = 32

5) The following are the marks
Scored by the Students in the
Summative Assessment exam.

Class	0-10	10-20	20-30	30-40	40-50	50-60
NO of Students	2,	7	15	10	Ц	5

Calculate the Median

Sol

C·I		ct
D - 10	2 *	, 2
10-20	7 1	19
20-30	15 1	24
30-40	10 1	3H
40-50	11 2	H5
50-60	5- +	50
	50=N	

Median class = 
$$\left(\frac{N}{2}\right)^{th}$$
 Value =  $\left(\frac{50}{2}\right)^{th}$  Value

Median class = 30-40

$$l = 30$$

$$\frac{N}{2} = 25$$

$$m = 24$$

$$c = 10 \Rightarrow ie, (0-10 \Rightarrow 10-0 = 10)$$

$$f = 10$$
Median =  $l + \frac{(\frac{N}{2} - m)}{t} \times c$ 

$$= 30 + (\frac{25 - 24}{10}) \times 10$$

$$= 30 + 1$$
Median = 31

The renear of five positive integers
$$lie twice their median Theorem$$

6) The mean of five positive integers is twice their median. If four of the integers are 3, 4, 6, 9 and median is 6. then find the fifth integer.

Given: - Mean of 5 integer = twice Median
$$\frac{3+4+6+9+x}{5} = 2 \times 6$$

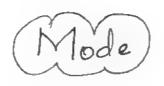
$$\frac{22+x}{5} = 12$$

$$22 + x = 12 \times 5$$

$$22 + x = 60$$

$$x = 60 - 22$$

$$x = 38$$



\* Raw Data

Most frequently occurring data

\* Grouped frequency.

 $Mode = l + \left[\frac{f-f_1}{2f-f_1-f_2}\right] \times c$ 

=> Class interval with maximum
frequency is modal class.

=> l = lower limit

=> f = frequency of modal class

=> f, = frequency of preceding the

=> f2 = frequency of Succeeding the modal class.

=> C = Width of Class Poterval

## Exercise - 8:3

The monthly Salary of 10 employees
in a factory are given below:

\$5000, \$7000, \$5000, \$7000, \$8000 \$7000, \$7000, \$8000, \$7000, \$5000 Find the mean, median, and mode.

Sol:

(i) Mean = Ex

5000 +7000 + 5000 + 7000 + 8000 + 7000 + 8000 + 7000 + 500 D

10

= 66000d

Mean = 6600

Arrange in Ascending Order. 5000, 5000, 5000, 7000, 7000, 7000, 7000, 7000, 8000, 8000 n=10 => even. Median = (=)th term + (= +1)th term (15) therm + (15) +1) therm 5th term + 6 term = 14000 7000 Median = 7000

23

```
(iii) Mode
  Mode = 7000 [Repeated 5 times]
2) Find the mode of the given data
  31, 3.2, 3.3, 2.1, 1.3, 3.3, 3.1
     Mode = 3.1 and 3.3
              [B: modal]
3) For the data 11, 15, 17, x+1, 19, x-2,3
 if the mean is 14, find the Value
 of x. Also find the mode of the data.
   11,15, 17, x+1, 19, x-2,3
   11+15+17+ ×+1 +19 + ×-2+3 = 14
         64+2x = 98
              2x = 98 - 64
```

(24)

2x = 34

$$\chi = \frac{34}{2}$$

$$\chi + 1 = 17 + 1 = 18$$

$$\chi - 2 = 17 - 2 = 15$$

(4) The demand of track Suit of different sizes as Obtained by a

Survey is given below: -

Size 3	39	40	41	42	HS	44	45
No of 3 Persons	6 1:	5 37	13	26	8	6	2

Sol Mode = 40 (37 persons demands)

5) Find the mode of the following data:

Marks	0-10	10-20	20-30	30-40	40-50
Number of Students	22	38	46	34	20

Sol

Marks	f		
0-10	22		
10 - 20	38		
20-30	46		
30-40	34		
HO-50	20		

Modal Class = 
$$20-30$$
 $l = 20$ 
 $f = 46$ 
 $f_1 = 38$ 
 $f_2 = 34$ 
 $C = 10$ 

$$Mode = 1 + \left[\frac{f-f_1}{2f-f_1-f_2}\right] \times c$$

$$= 20 + \left[\frac{46-38}{2(46)-38-34}\right] \times 10$$

$$= 20 + \left[ \frac{8}{92 - 38 - 34} \right] \times 10$$

$$= 20 + \left[ \frac{8}{92 - 72} \right] \times 10$$

$$= 20 + \left(\frac{8^4}{20}\right) \times 10^{-1}$$

Weight (kg)	25-34	35 - 44	45 - 54	55-64	65-74	75-84
Number of Students	4	8	10	14	8	6

Soj: -

Weight	+	
24.5 - 34.5	4	
34.5 - 44.5	8	
44.5 - 54.5	ID	
54.5 - 64.5	14	
64.5 - 74.5	8	
74.5 - 84.5	6	

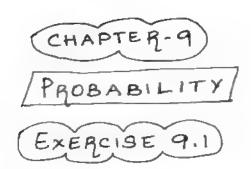
Modal class = 54.5-64.5

$$l = 54.5$$
 $f = 14$ 
 $f_1 = 10$ 
 $f_2 = 8$ 
 $c = 10$ 

 $Mode = l + \left(\frac{f-f_1}{2f-f_1-f_2}\right) \times c$ 

$$= 54.5 + \left[ \frac{14 - 10}{2(14) - 10 - 8} \right] \times 10$$

$$= 54.5 + \left[\frac{4}{28 - 18}\right] \times 10$$



I) you one walking along a street.

If you just choose a stranger
crossing you, what is the probability
that his next birthday will fall
on a Sunday?

S=) NO.07 days in a week / S= goon, mon, Tue, wed, Thur, Fri, Saty n(s)=7

next birthday will fall on a Sunday.

:. 
$$P(A) = \frac{n(A)}{n(s)} = \frac{1}{7}$$

a King or a Queen on a Jack from a deck of cards?

King or Queen or Jack

AUBUC

Let A be the probability of drawing a king

$$P(A) = 4$$

$$P(A) = \frac{P(A)}{P(S)} = \frac{4}{52}$$

$$P(A) = \frac{1}{52}$$

Let B be the probability of drawing a aveen.

$$P(B) = 4$$

$$P(B) = \frac{P(B)}{P(S)} = \frac{4}{52}$$

Let c be the probability of getting a Jack.

$$P(c) = H$$
 $P(c) = \frac{D(c)}{D(s)} = \frac{H}{52}$ 

$$P(AUBUC) = P(A) + P(B) + P(C)$$

$$= \frac{4}{52} + \frac{4}{52} + \frac{4}{52}$$

$$= \frac{4+4+4}{52}$$

$$= 12$$

52

an even number with a single standard dice of six faces?

Let A be the probability of throwing an even number with a single standard dice of six faces.

:. 
$$P(A) = \frac{n(A)}{n(a)} = \frac{3}{6}$$

4) There are 24 balls in a pot. It 3 of them are Red, 5 of them are Blue and the memaining are Green then, what is the probability of picking out (i) a Blue ball (ii) a Red ball and (iii) a Green ball?

Green balls = 24-8 = 16

in Let A be the probability of picking out a Blue ball.

$$P(A) = \frac{n(A)}{n(s)} = \frac{5}{24}$$

$$D(8) = 3$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{3}{24}$$

$$P(c) = \frac{n(c)}{n(s)} = \frac{16}{24}$$

5) when two coins one tossed, what is the probability that two heads one obtained?

heads are obtained.

$$P(A) = \frac{n(A)}{n(3)} = \frac{1}{4}$$

6) Two dice are rolled, find the Probability that the sum is (I equal to 1 (ii) less than 13.

Two Dice:

$$S = \begin{cases} (111) & (112) & (113) & (114) & (115) & (116) \\ (211) & (212) & (213) & (214) & (215) & (216) \\ (311) & (312) & (313) & (314) & (315) & (316) \\ (411) & (412) & (413) & (414) & (415) & (416) \\ (511) & (512) & (513) & (514) & (515) & (516) \\ (611) & (612) & (613) & (614) & (615) & (616) & 6 \\ (611) & (612) & (613) & (614) & (615) & (616) & 6 \\ (612) & (613) & (614) & (615) & (616) & 6 \\ (613) & (612) & (613) & (614) & (615) & (616) & 6 \\ (613) & (612) & (613) & (614) & (615) & (616) & 6 \\ (614) & (612) & (613) & (614) & (615) & (616) & 6 \\ (614) & (612) & (613) & (614) & (615) & (616) & 6 \\ (614) & (612) & (613) & (614) & (615) & (616) &$$

$$(4.1) (4.2) (4.3) (4.4) (4.5) (4.6)$$

$$(5.1) (5.2) (5.3) (5.4) (5.5) (5.6)$$

$$(6.1) (6.2) (6.3) (6.4) (6.5) (6.6) {}_{4}$$

$$n(c) = 36$$

$$P(c) = \frac{n(c)}{n(s)} = \frac{36}{36} = 1$$

1) A manufacturer tested 7000 LED Lights at random and found that 25 of them were defective. If a LED light is selected at random, what is the probability that the selected LED light is a defective one.

(defective-25)

n(s) = 7000 (LED Lights)

Let A be the Posobability that the Selected LED light is a defective

$$n(A) = 25$$

$$P(A) = n(A) = 25$$

$$n(S) = 7000$$

8) In a football match, a goal keeper of a team can stop the goal, 32 times out of 40 attempts topied by a team. Find the poobability that the oppenent team can convert the attempt into

a goal.

Let A be the probability that the opponent team can convert the attempt into a goal.

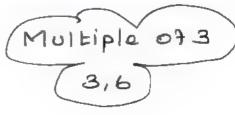
$$N(A) = 40 - 32 = 8$$

$$P(A) = \frac{D(A)}{D(S)} = \frac{8}{40}$$

9) What is the probability that the spinner will not land on a multiple of 3?

spinnen will not land on a multiple

$$P(A) = \frac{n(A)}{n(s)} = \frac{6}{8}$$



10) Frame two problems in calculating Probability based on the Spinner Shown here.

(i) Let A be the probability of not

Multiple 072

$$P(A) = \frac{D(A)}{D(3)} = \frac{H}{8}$$

$$P(A) = \underline{n(A)} = \underline{H}$$

(ii) Let B be the probability of

$$n(B) = 2$$

$$P(B) = \frac{n(B)}{n(B)} = \frac{2}{8}$$

1) A company manufactures 10000
Laptops in 6 months. Out of which
25 of them are found to be defective.
When you choose one Laptop from
the manufactured, what is the
Probability that selected Laptop is
a good one.

: Good Laptops = 10,000-25

## = 9975

Let A be the probability that the selected Laptop is a good one.

$$P(A) = \frac{n(A)}{n(3)} = \frac{9975}{10000}$$

2) In a survey of 400 youngsters aged 16-20 years, it was found that 191 have their voter ID card. It a youngster is selected at random, find the probability that the youngster does not have their voter ID-card.

youngstee does not have their votes

: 
$$P(A) = \frac{n(A)}{n(3)} = \frac{209}{400}$$

3) The Probability of guessing the connect answer to a certain question is  $\frac{x}{3}$ . If the probability of not guessing the connect answer is  $\frac{x}{3}$ , then find the value of x.

$$\Rightarrow$$
  $P(A) = \frac{x}{3}$ 

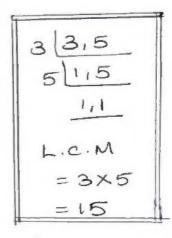
P(not guessing the connect answer) =  $\frac{x}{5}$ =)  $P(A') = \frac{x}{5}$ 

We know,

$$P(A) + P(A') = 1$$

$$\frac{x}{3} + \frac{x}{5} = 1$$

$$\frac{5x + 3x}{15} = 1$$



10

$$\frac{8x}{15} = 1$$

$$8x = 15$$

$$x = 15$$

$$x = 15$$

4) If a probability of a player winning a particular tennis match is 0.72. What is the probability of the player loosing the match?

P (not winning the match) = ?

We know,

0 910

0.72 (-)

X. 98

0.28

5) 1500 families were surveyed and following data was neconded about their maids at houses.

Tupe of maids	Only Part time	Only full time	both
No. of families	860	370	250

m

A family is selected at random. Find the probability that the family selected has (i) Both types of maids.

(ii) Part time maids (iii) No maids.

family selected has both types of maids.

.. 
$$P(A) = n(A) = 250$$
 $n(3) = 1500$ 

(ii) Let B be the probability that the family selected has part time maids.

:. 
$$P(B) = \frac{n(B)}{n(S)} = 860$$

(iii) Let c be the probability that the family selected has no maids.

$$n(c) = 1500 - (860 + 370 + 250)$$

$$n(c) = 1500 - 1480$$

$$P(c) = \frac{D(c)}{D(s)} = \frac{20}{1500}$$